

Chiral modes in optics and electronics of 2D systems – Aussois, November 26-28, 2018



TOPOLOGICAL PHOTONICS WITH MICROWAVES

Fabrice Mortessagne



Waves in Complex Systems team

- Flexible experimental platforms in microwaves or optics (and a hint of acoustics)
- Random Matrix Theory, effective Hamiltonian formalism, numerical simulations
- Complex geometries : multimode optical fibres, 2D or 3D microwave cavities
- (dis)ordered lattices : coupled μ wave resonators, photo-induced/laser-written photonic structures
- Wave chaos – Anderson localization
- Artificial Dirac materials
- Quantum fluids of light
- Topological photonics



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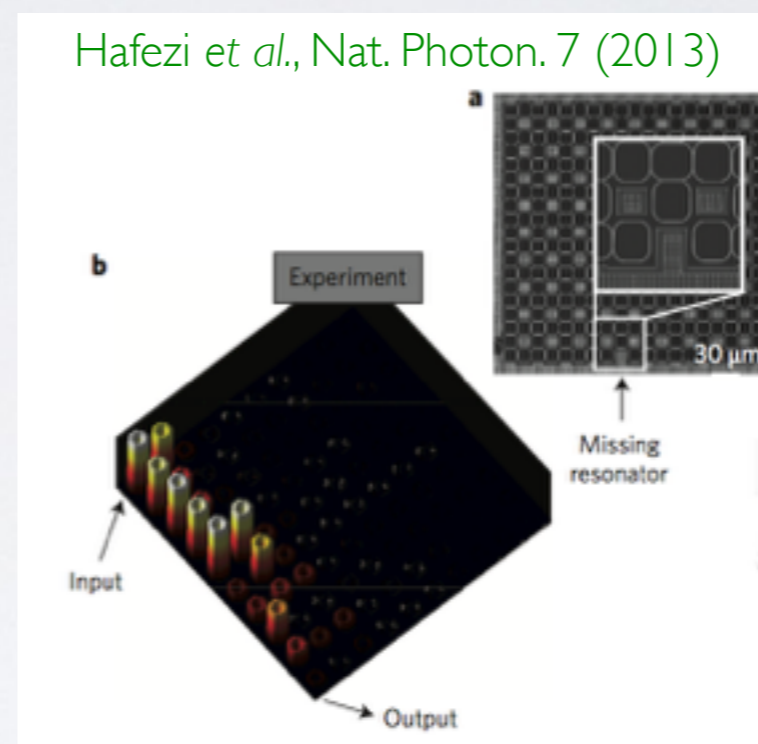


Topological photonics

This field aims to explore the physics of topological phases of matter in a novel optical context.

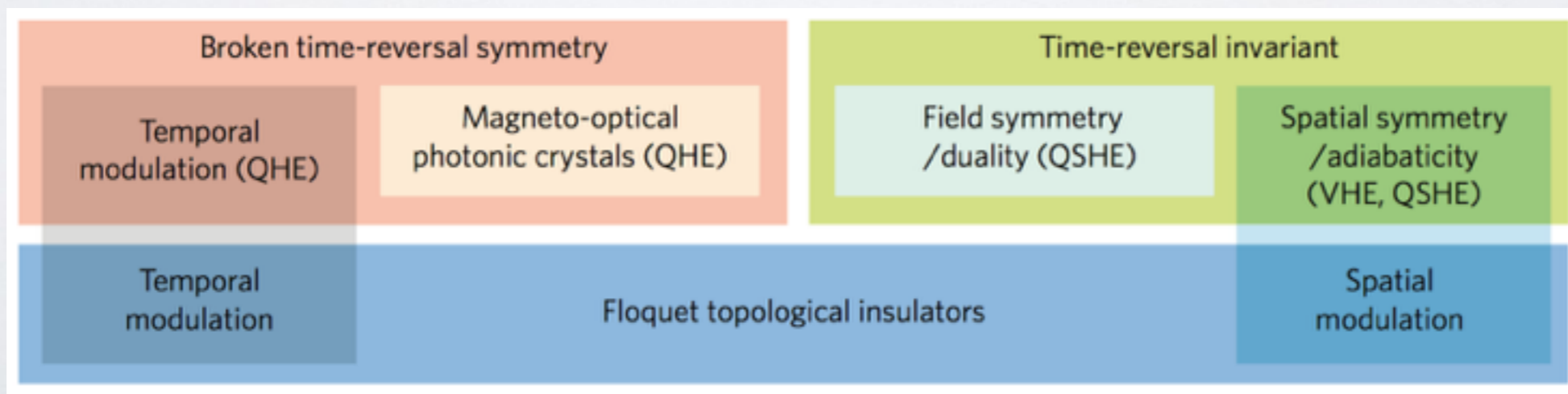
T. Ozawa *et al.* arXiv 1802.04173

- 2008: First theoretical prediction (Haldane & Raghu)
- 2009: First experimental realization (Wang *et al.*, MIT)
- since there: Different strategies to emulate topological phases with photons



Chiral edge state in a lattice of coupled ring resonators on a silicon chip.

Pseudospins given by clockwise and anticlockwise modes.



Khanikaev & Shvets, Nat. Photon. 11, 763 (2017)

Recall yesterday's talks

Outline

1. Microwave realization of tight-binding model

dielectric resonators, TE mode, evanescent coupling, LDOS & eigenstates

2. SSH chain: Control of topological interface states

zero-mode, selective enhancement, non-linear absorption, reflective limiter

3. 2D lattices : Lieb (and Penrose)

partial symmetry breaking, (not so) flat band, zero-mode, gap labeling (naive picture)

Experimental setup

- Vectorial Network Analyzer (@ 6~7 GHz): complex scattering matrix;
- dielectric resonators sandwiched between metallic plates;
- 'kink' and 'loop' antennas excite TE polarization:

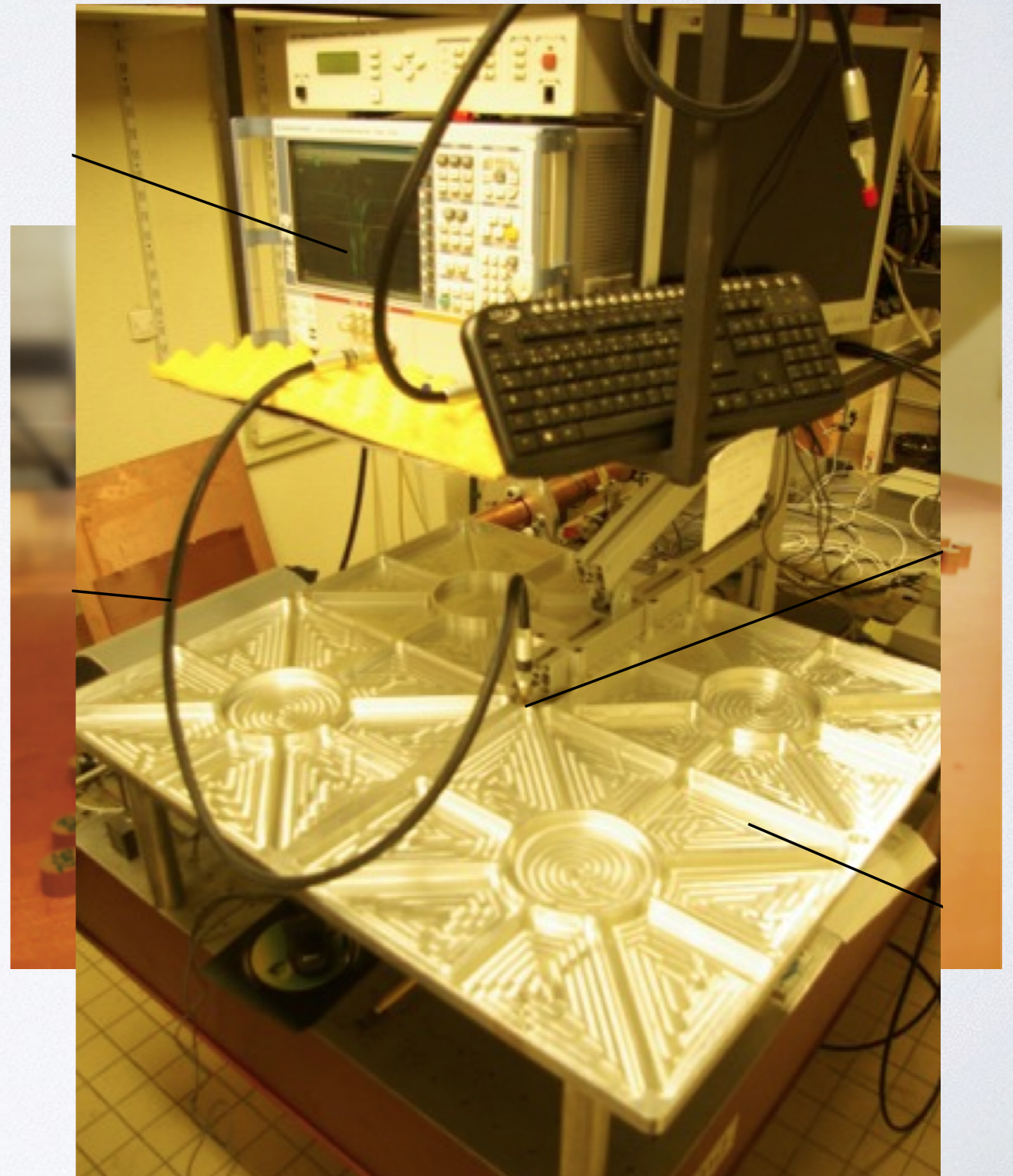
$$\psi(\vec{r}) = B_z(\vec{r})$$



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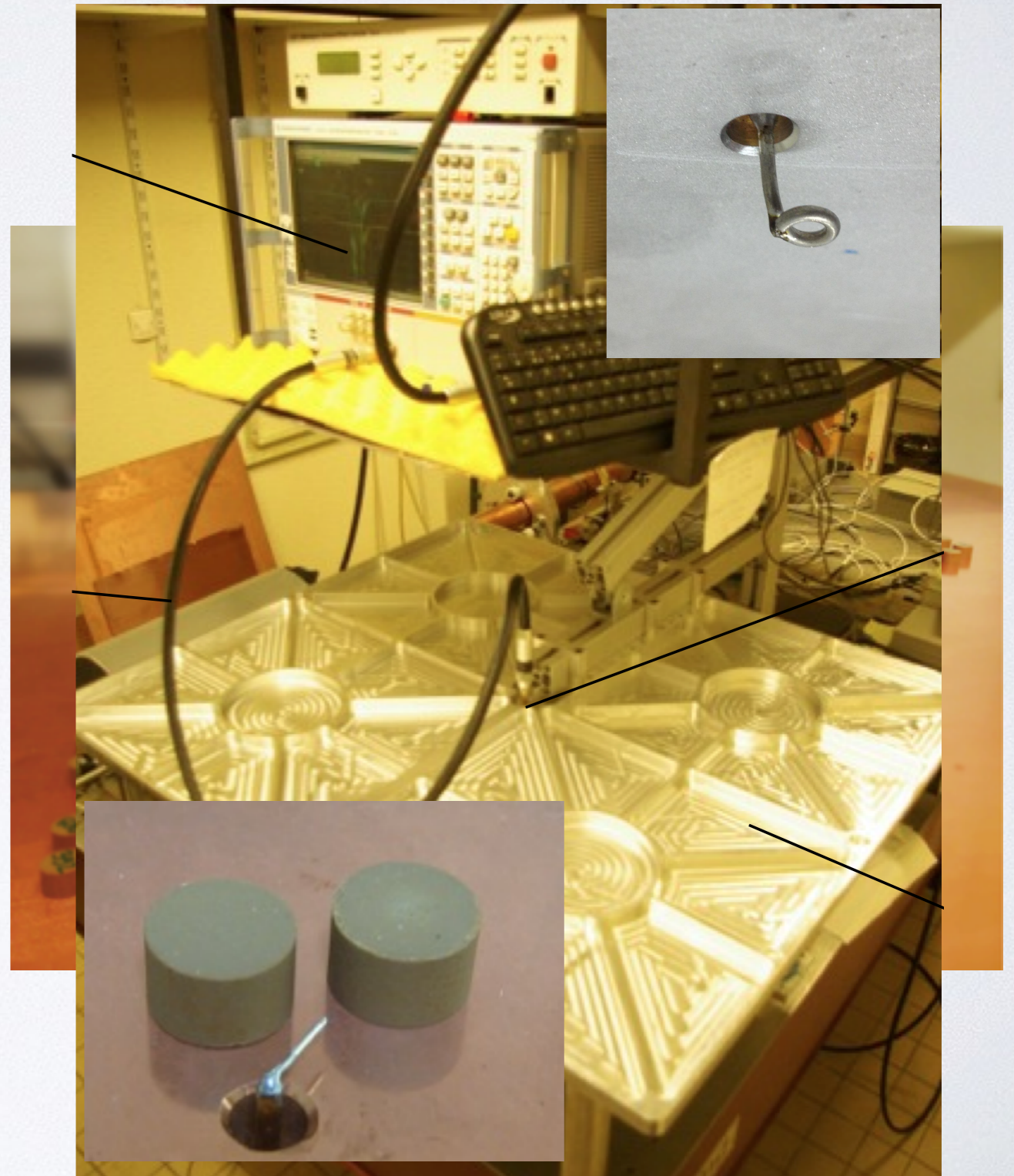
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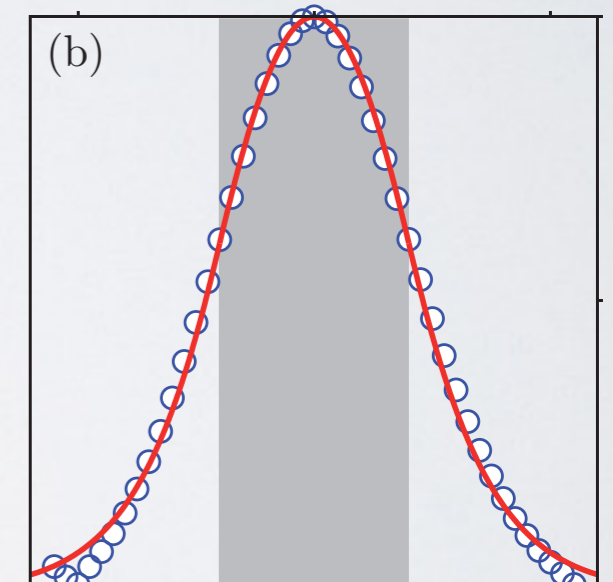
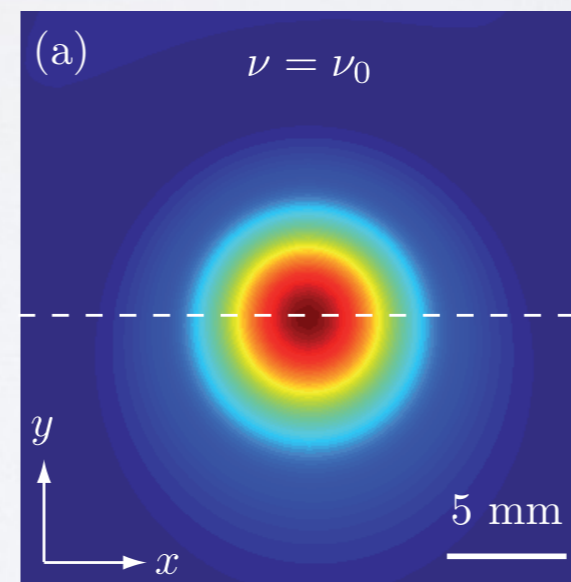
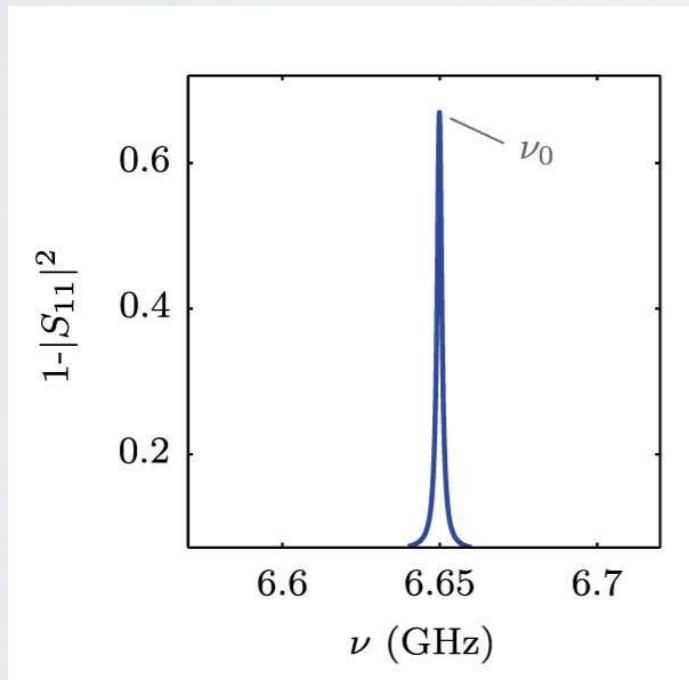
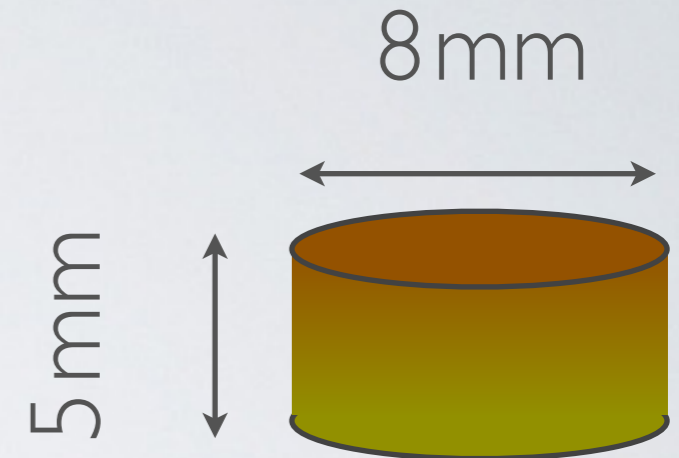
$$\psi(\vec{r}) = B_z(\vec{r})$$



Microwave resonator

Dielectric ceramic (ZrSnTiO):

- high permittivity: $\epsilon = 37$
- low loss: $Q \simeq 7000$



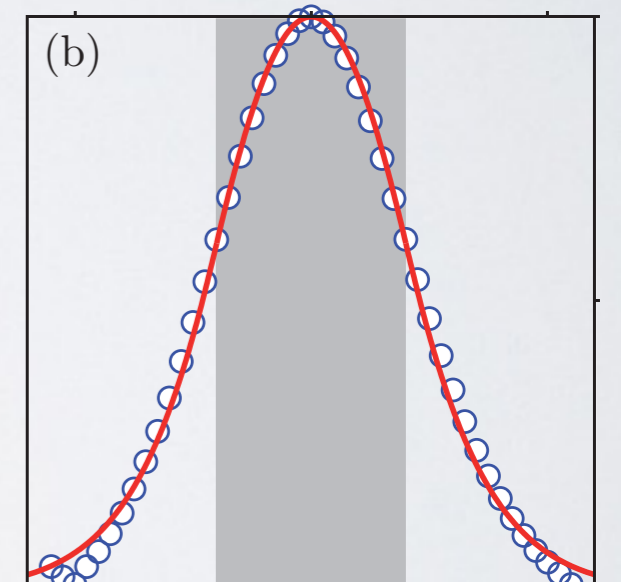
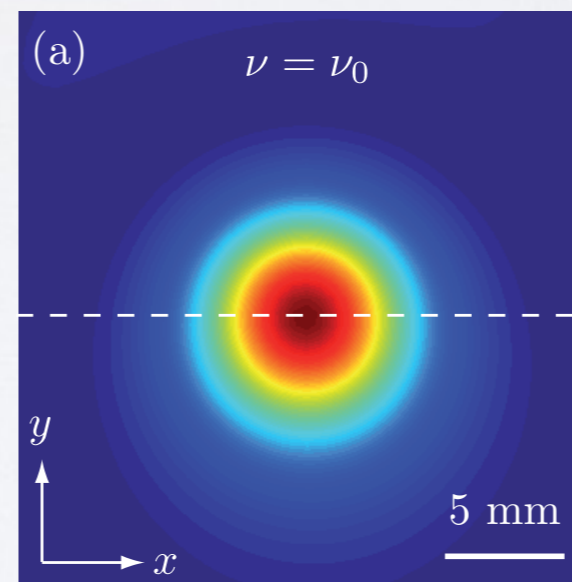
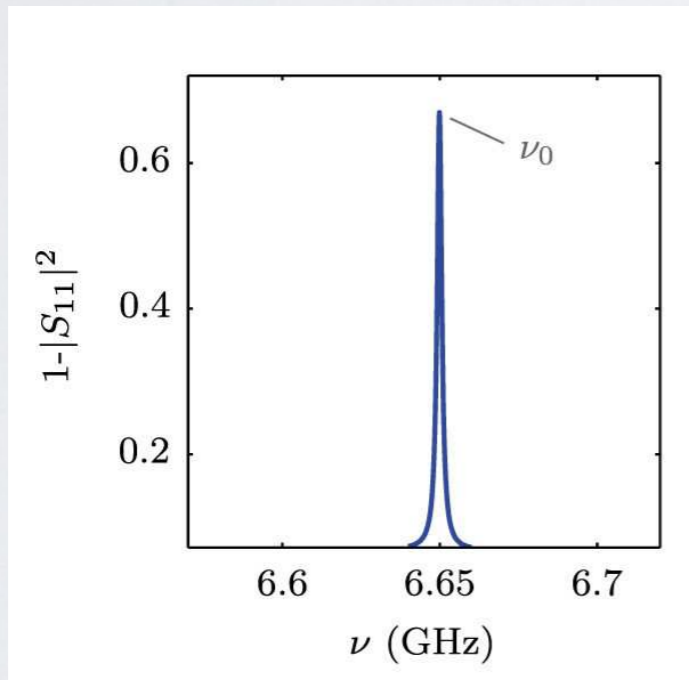
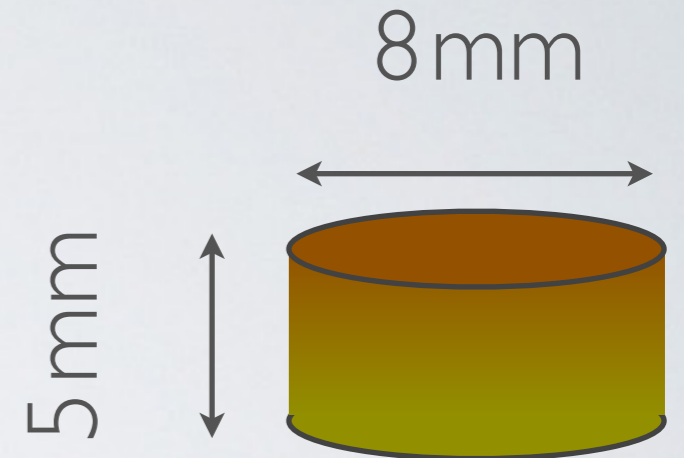
- TE_1 Mie resonance
@ 6.65 GHz

- Energy essentially inside
- Evanescent field outside

Microwave resonator

Dielectric ceramic (ZrSnTiO):

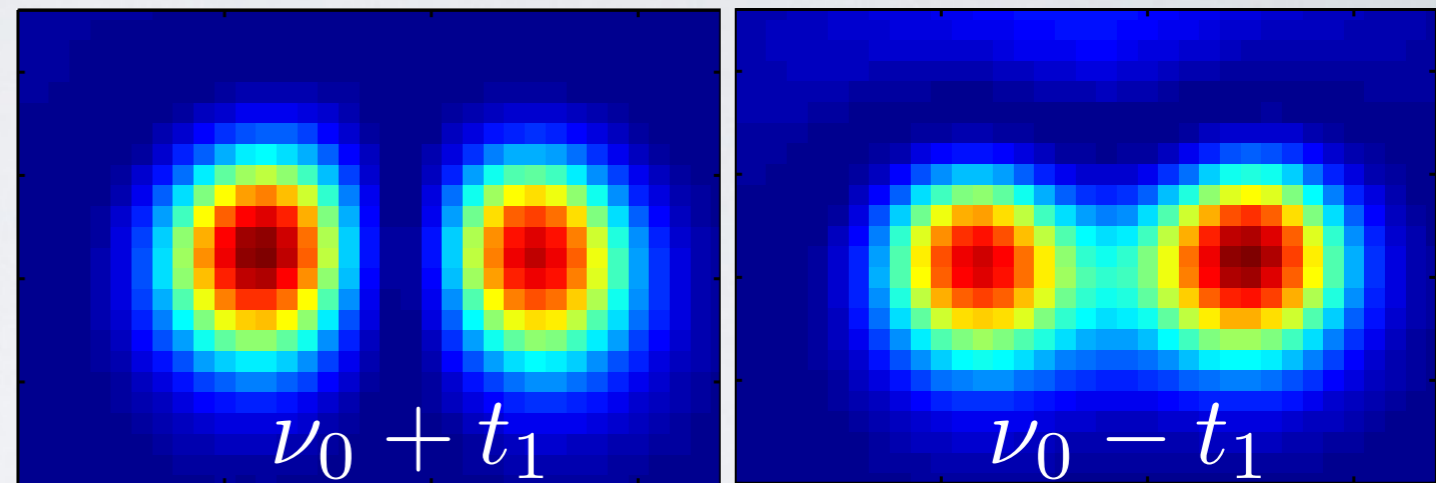
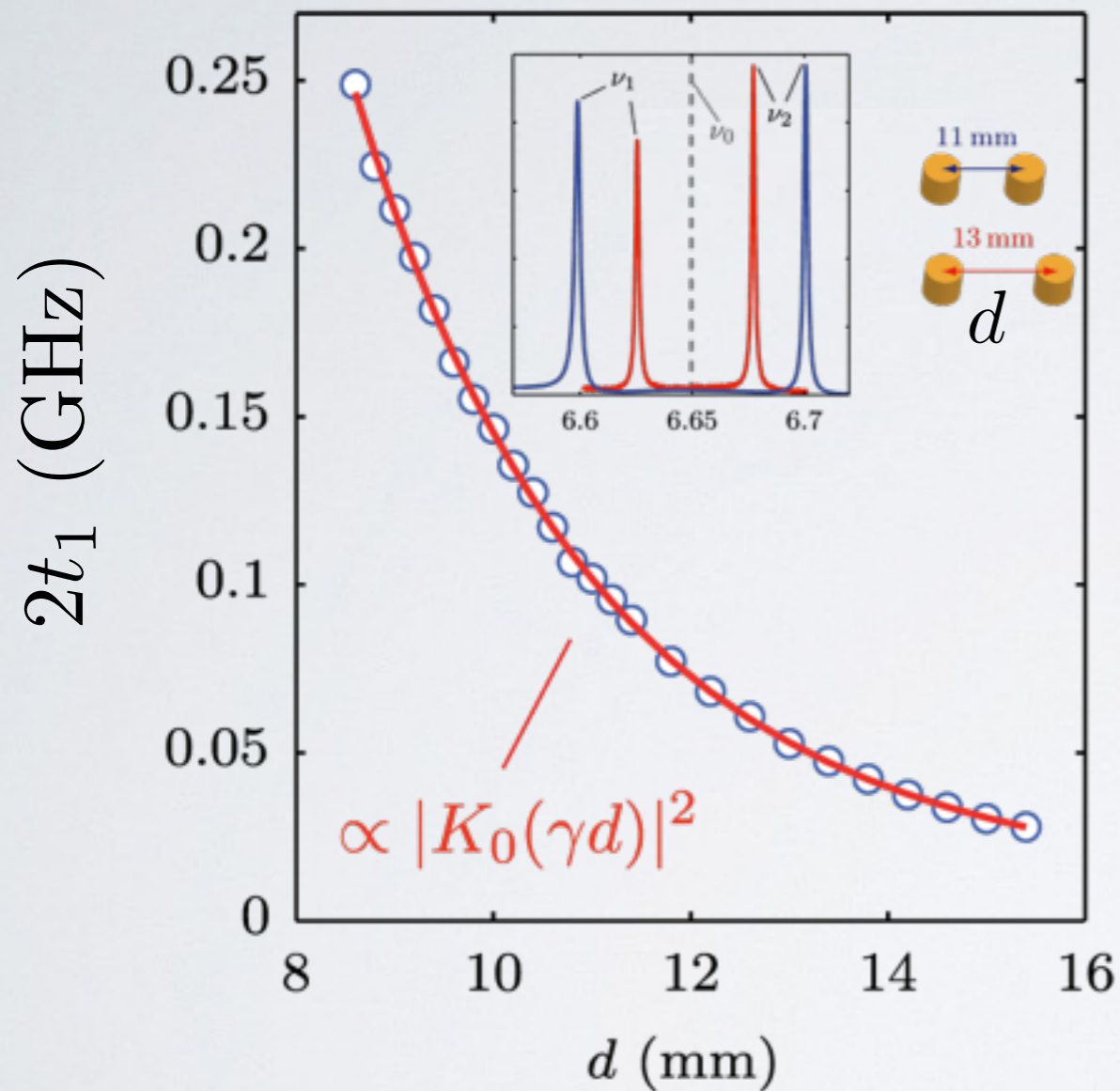
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- low loss: $Q \simeq 7000$



- TE₁ Mie resonance @ 6.65 GHz

$$B_z(\vec{r}, z) = B_0 \sin\left(\frac{\pi}{h}z\right) \times \begin{cases} J_0(\gamma_j \vec{r}) \\ \alpha K_0(\gamma_k \vec{r}) \end{cases}$$

Tight-binding coupling



$$H(d) = \begin{pmatrix} \nu_0 & -t_1(d) \\ -t_1(d) & \nu_0 \end{pmatrix}$$

$$t_1(d) \propto -|K_0(d/2\ell)|^2$$

$$\ell \simeq 3 \text{ mm}$$

Building blocks of artificial molecules, (quasi-)crystals, disordered lattices... (well controlled metamaterials)

LDoS & eigenstates

A direct access to the density of states and intensity of the eigenstates through:

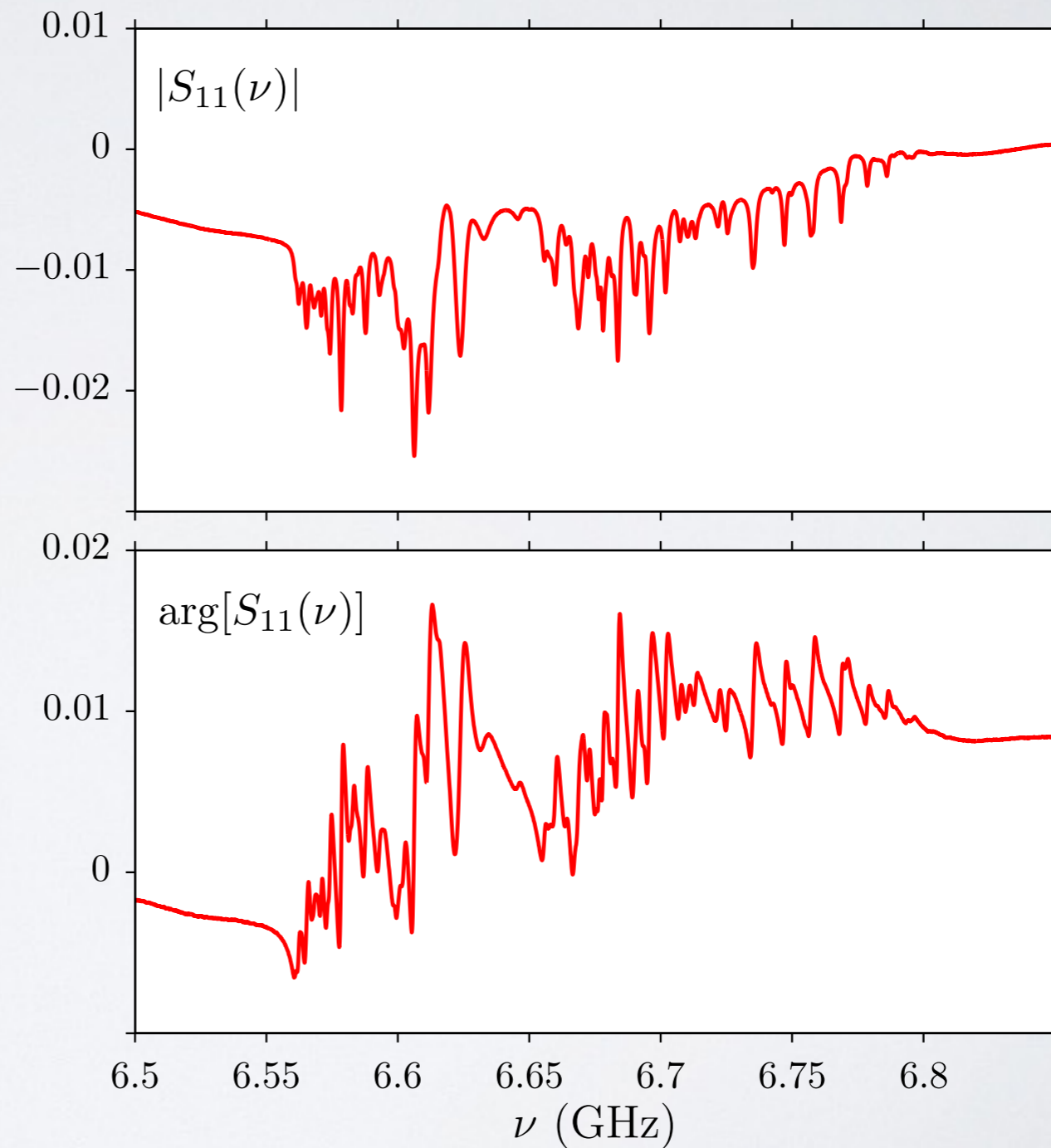
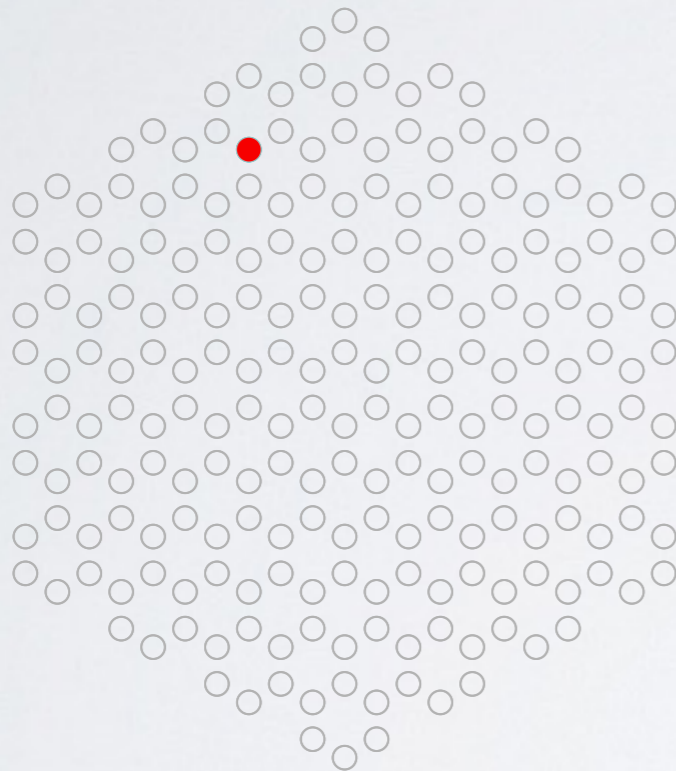
$$g(\mathbf{r}_1, \nu) = |S_{11}(\nu)|^2 \varphi'_{11}(\nu) \quad \arg[S_{11}(\nu)] = \varphi_{11}(\nu)$$

$$g(\mathbf{r}_1, \nu) \simeq \frac{\sigma}{\Gamma} \sum_n |\Psi_n(\mathbf{r}_1)|^2 \delta(\nu - \nu_n)$$

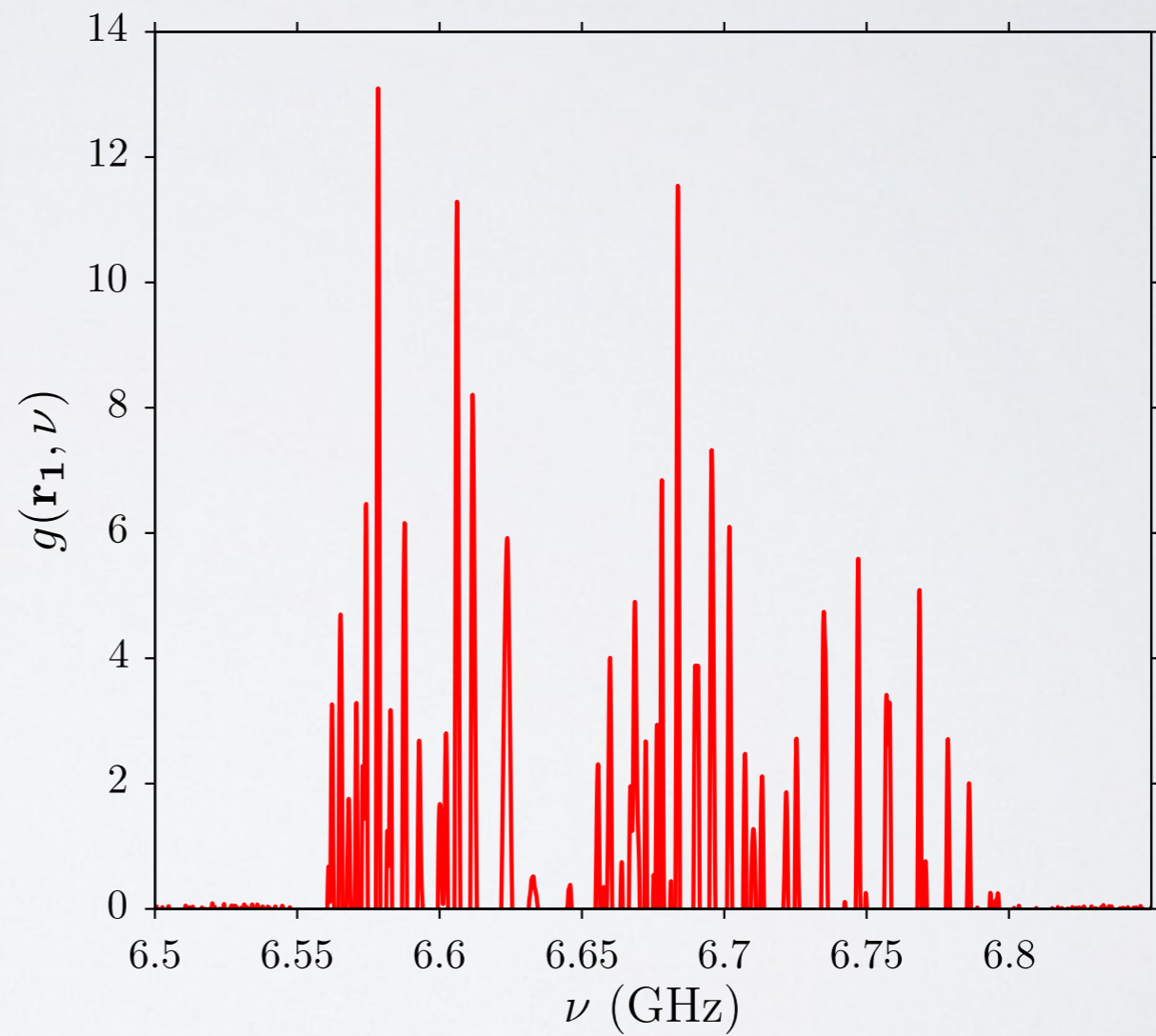
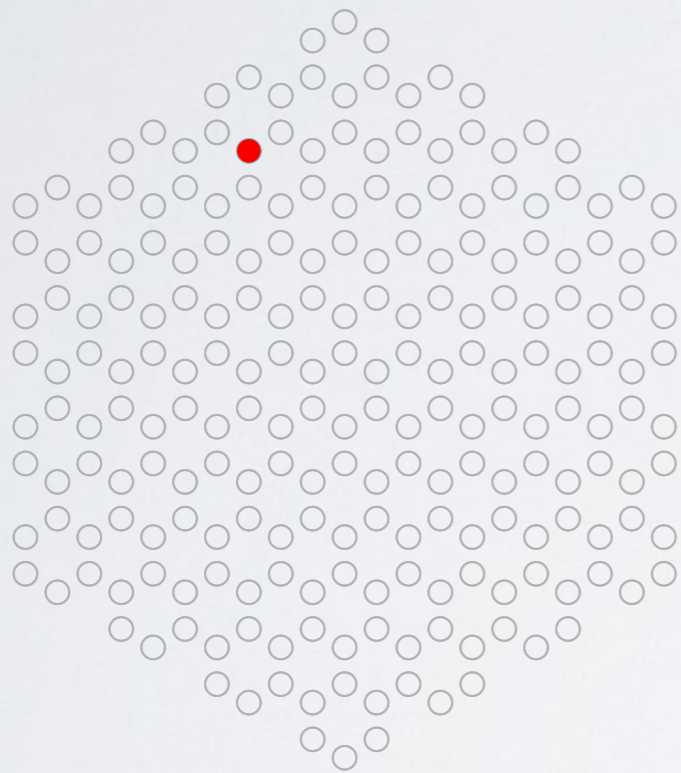
Local Density of States, DoS by averaging

for a given eigenfrequency: measure the local intensity

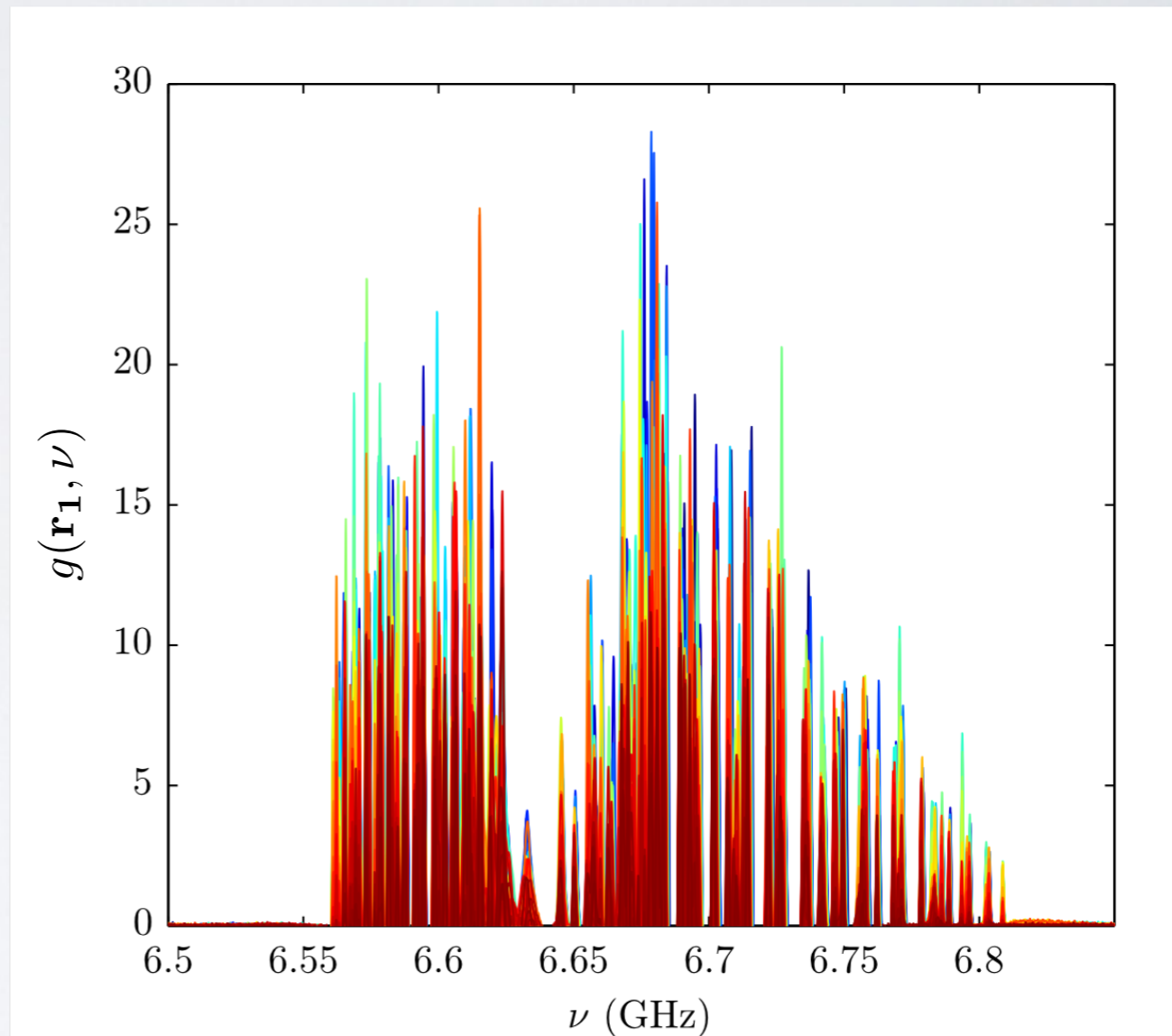
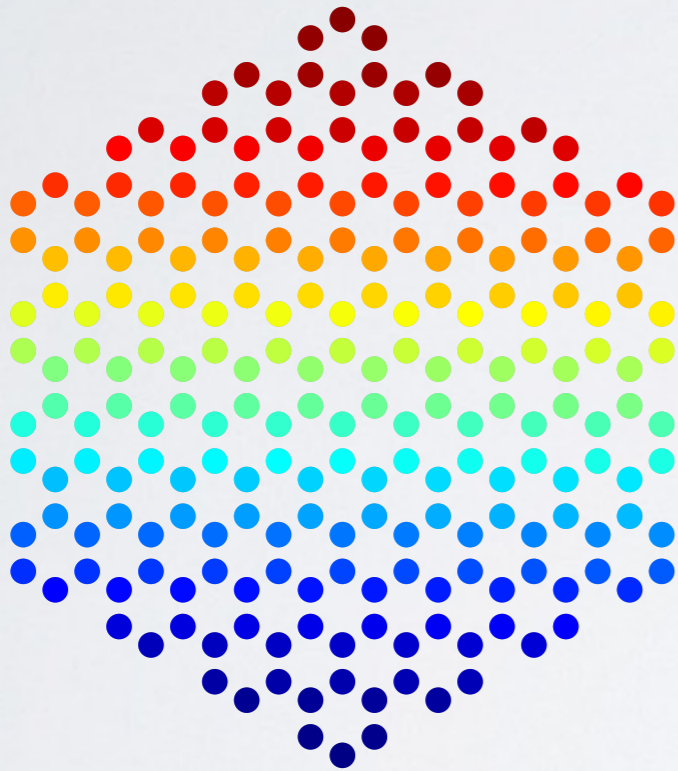
(Local) Density of States



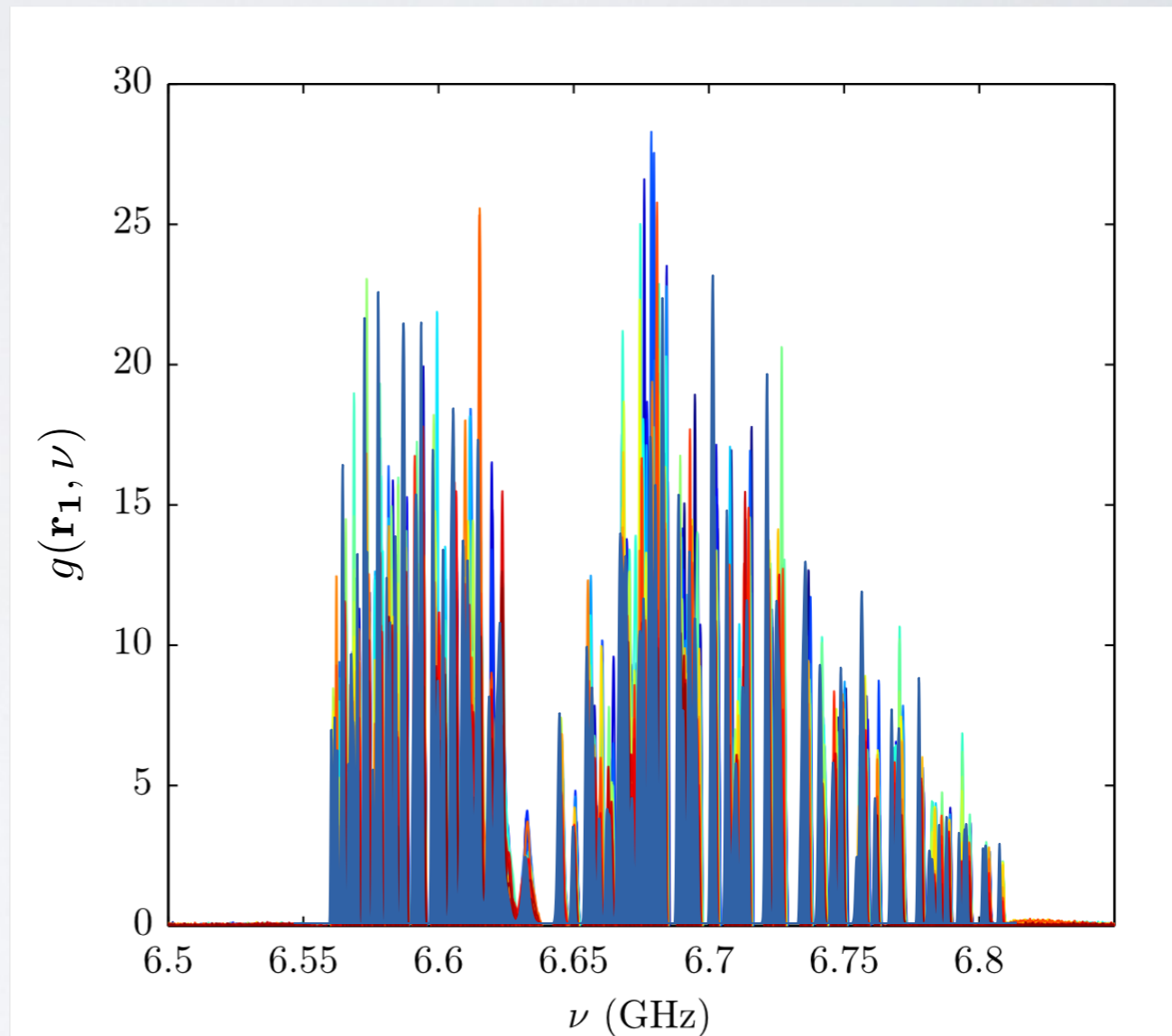
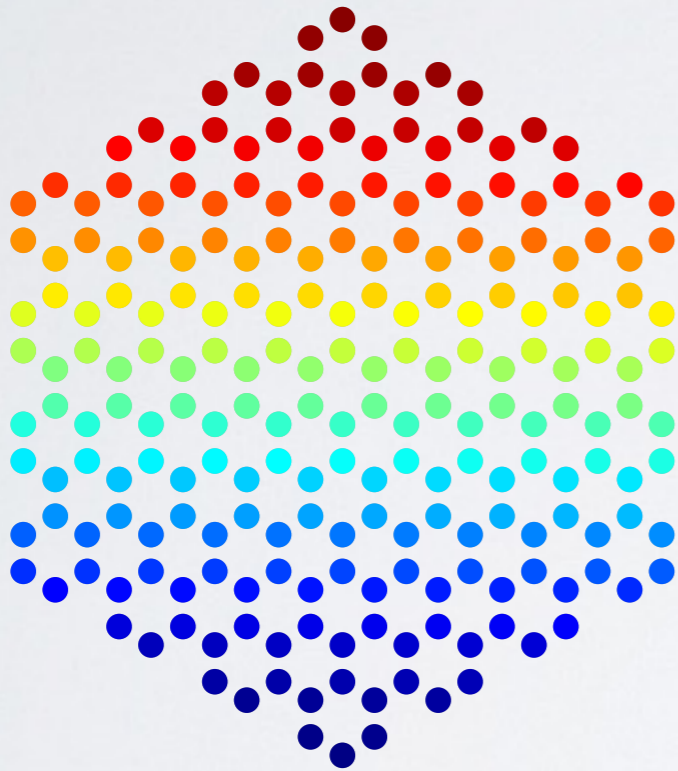
(Local) Density of States



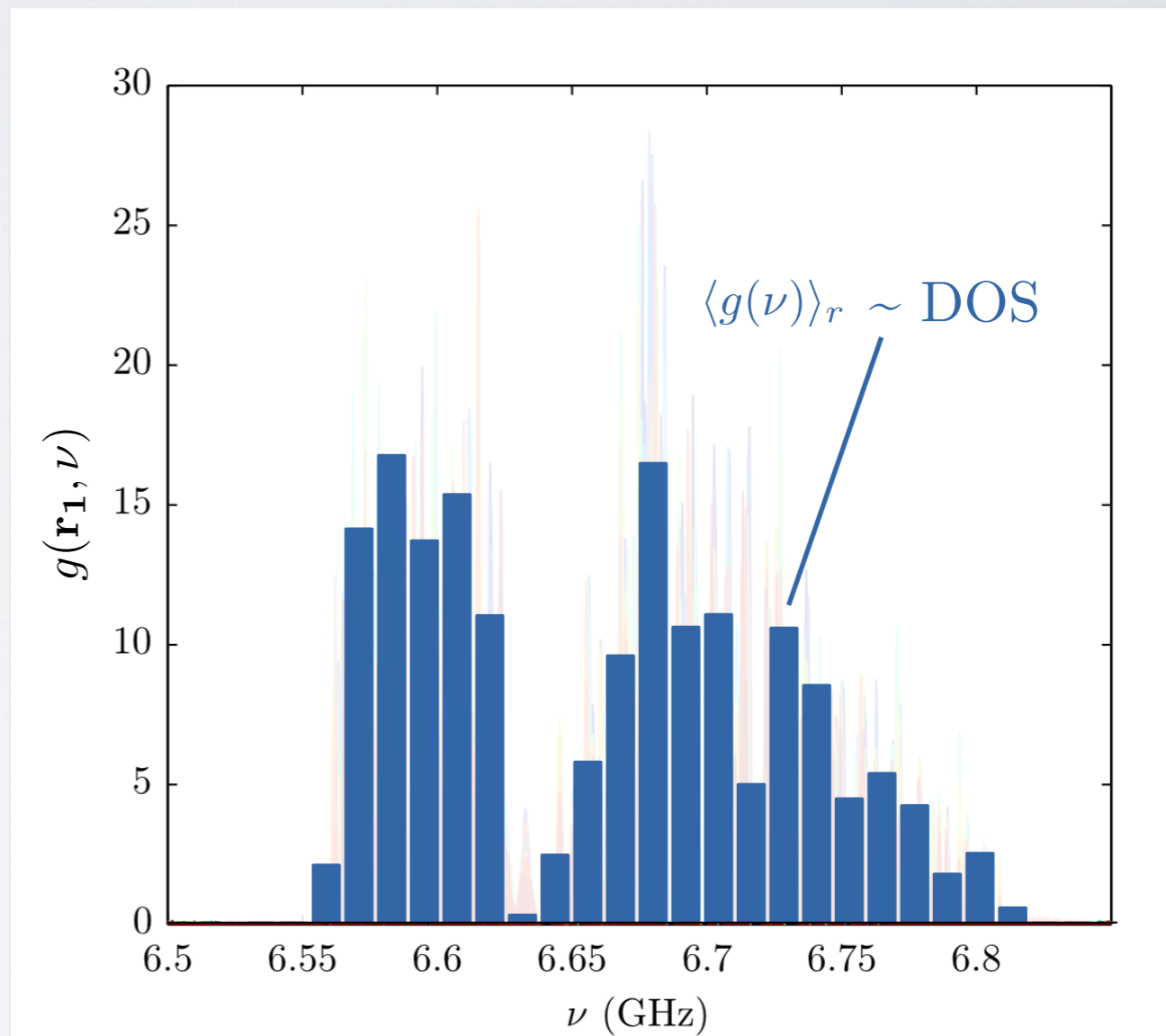
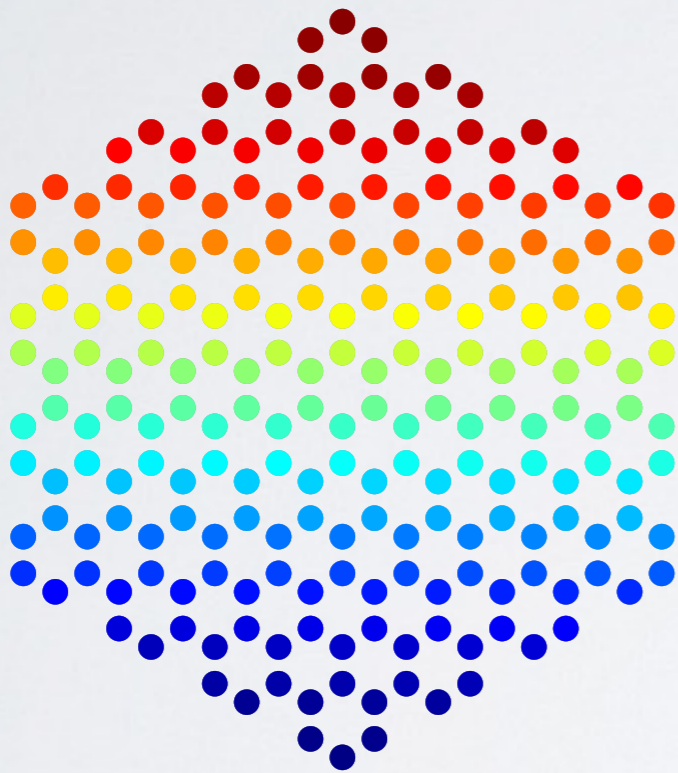
(Local) Density of States



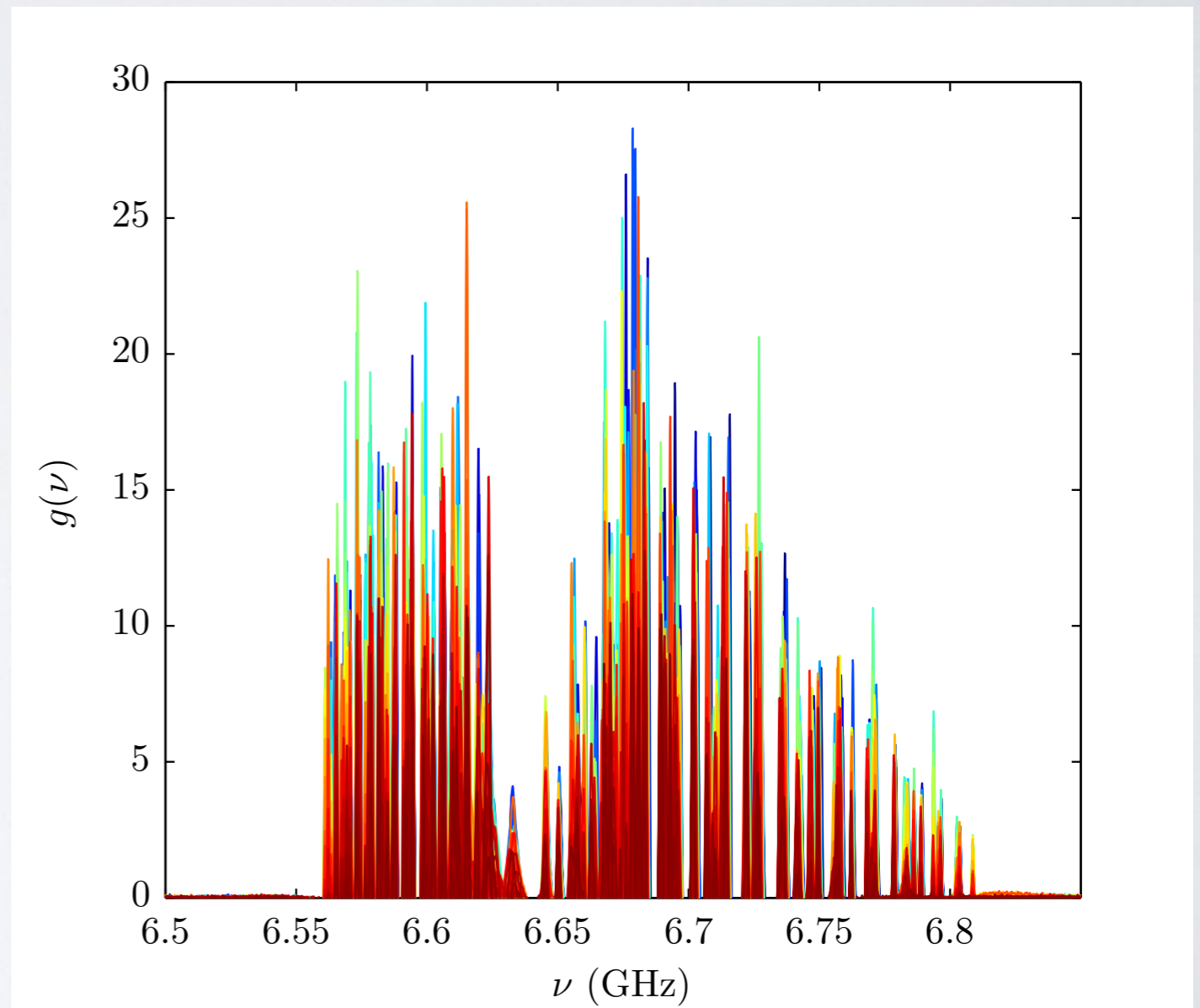
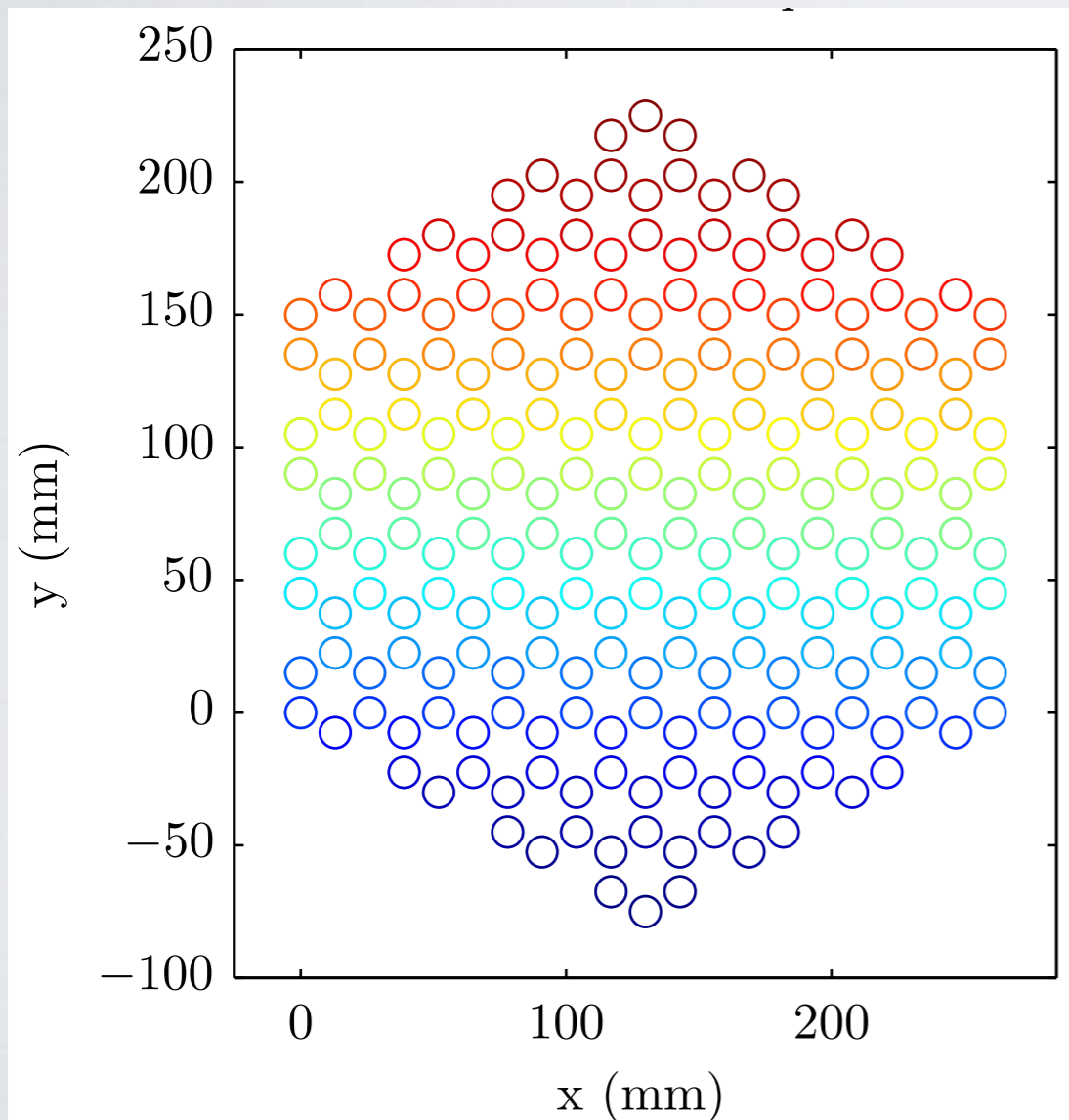
(Local) Density of States



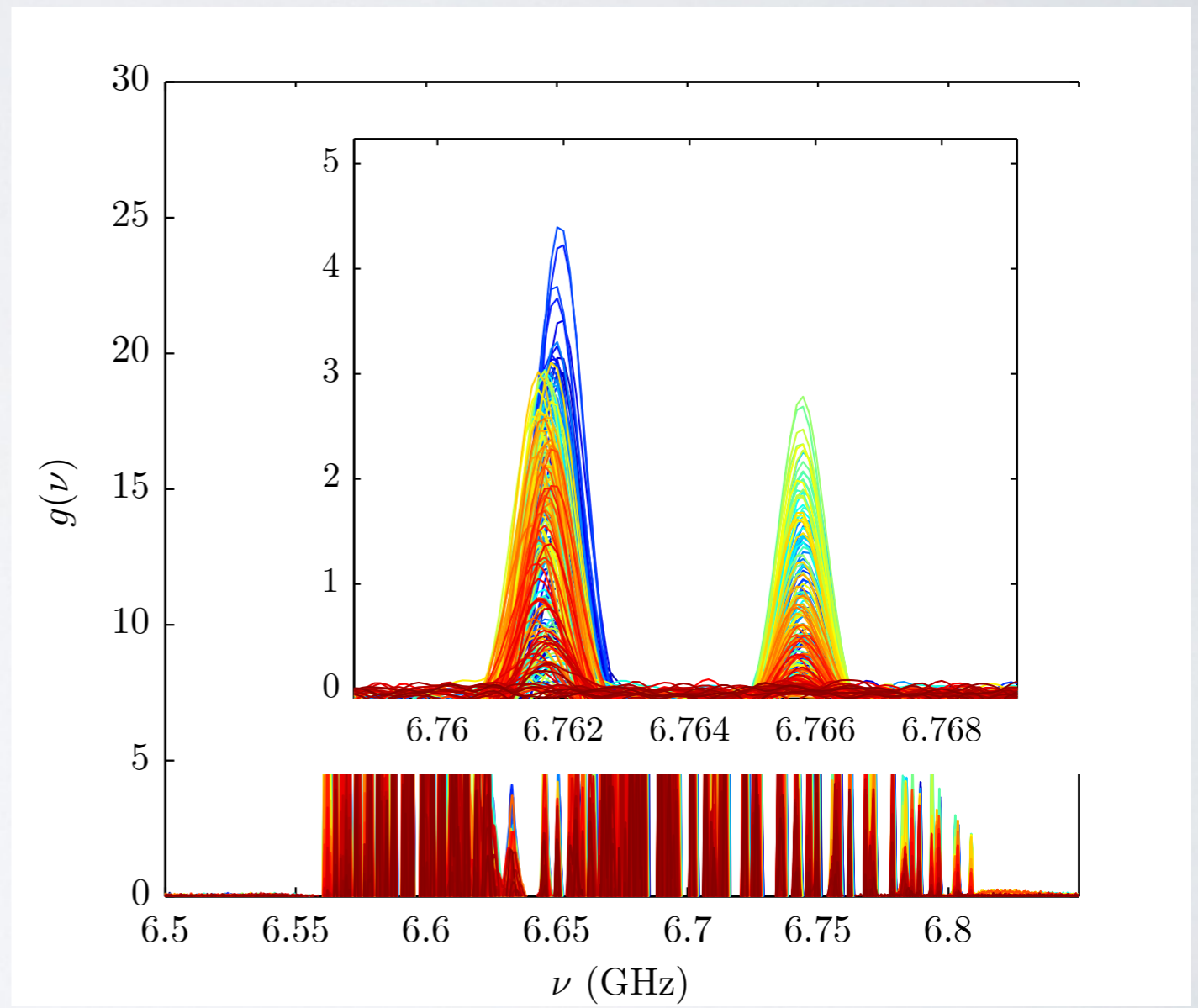
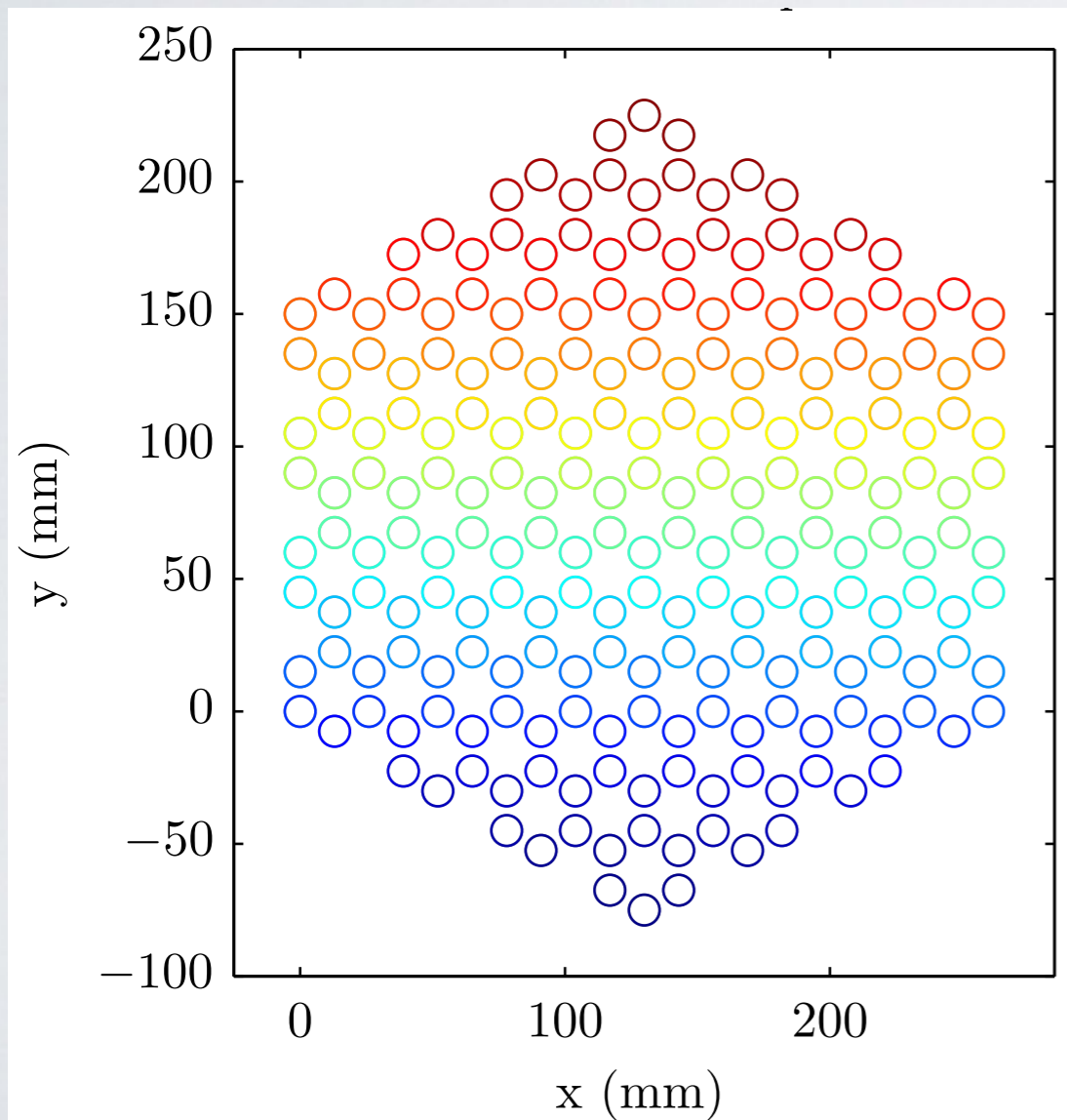
(Local) Density of States



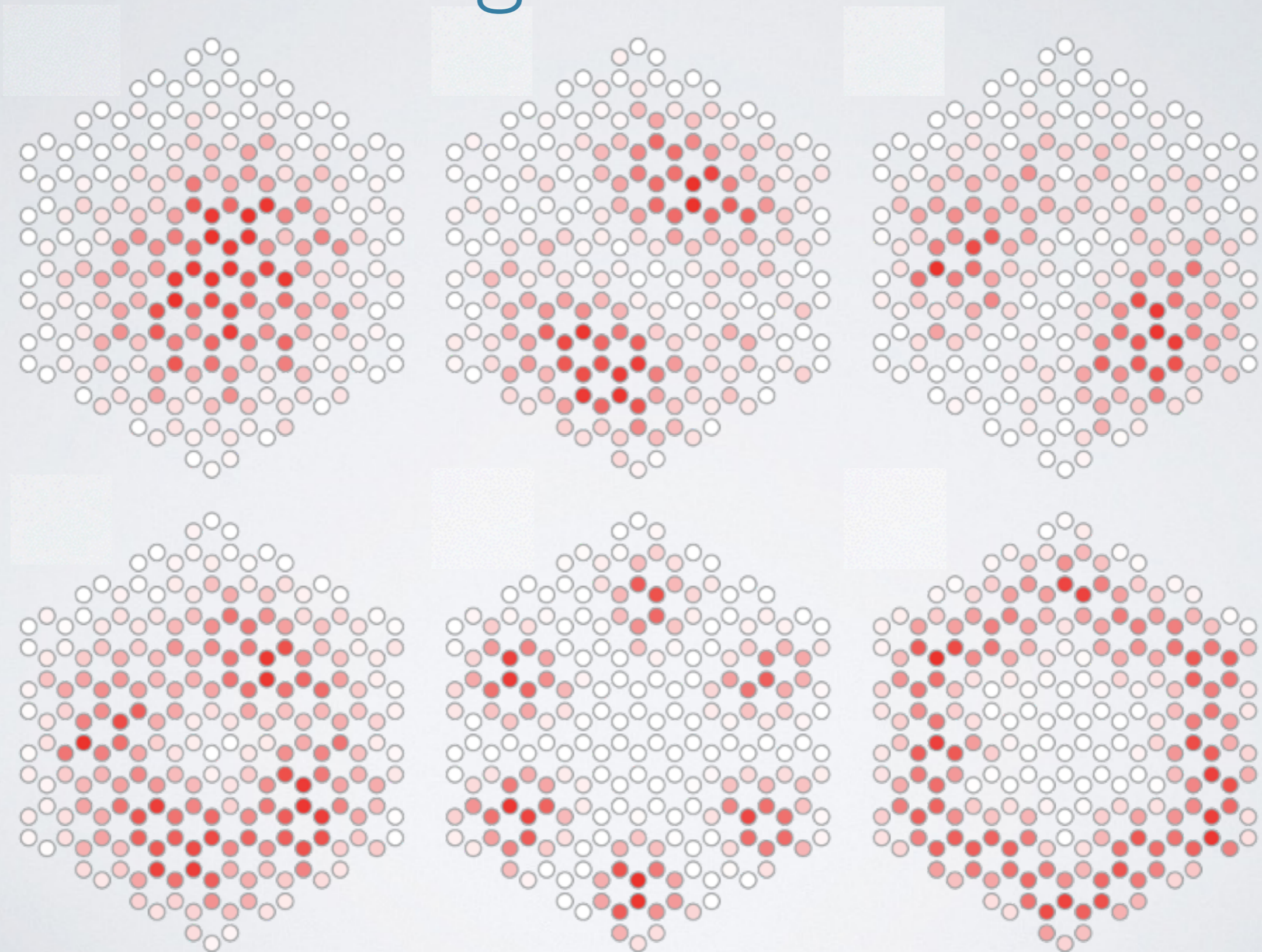
Eigenstates



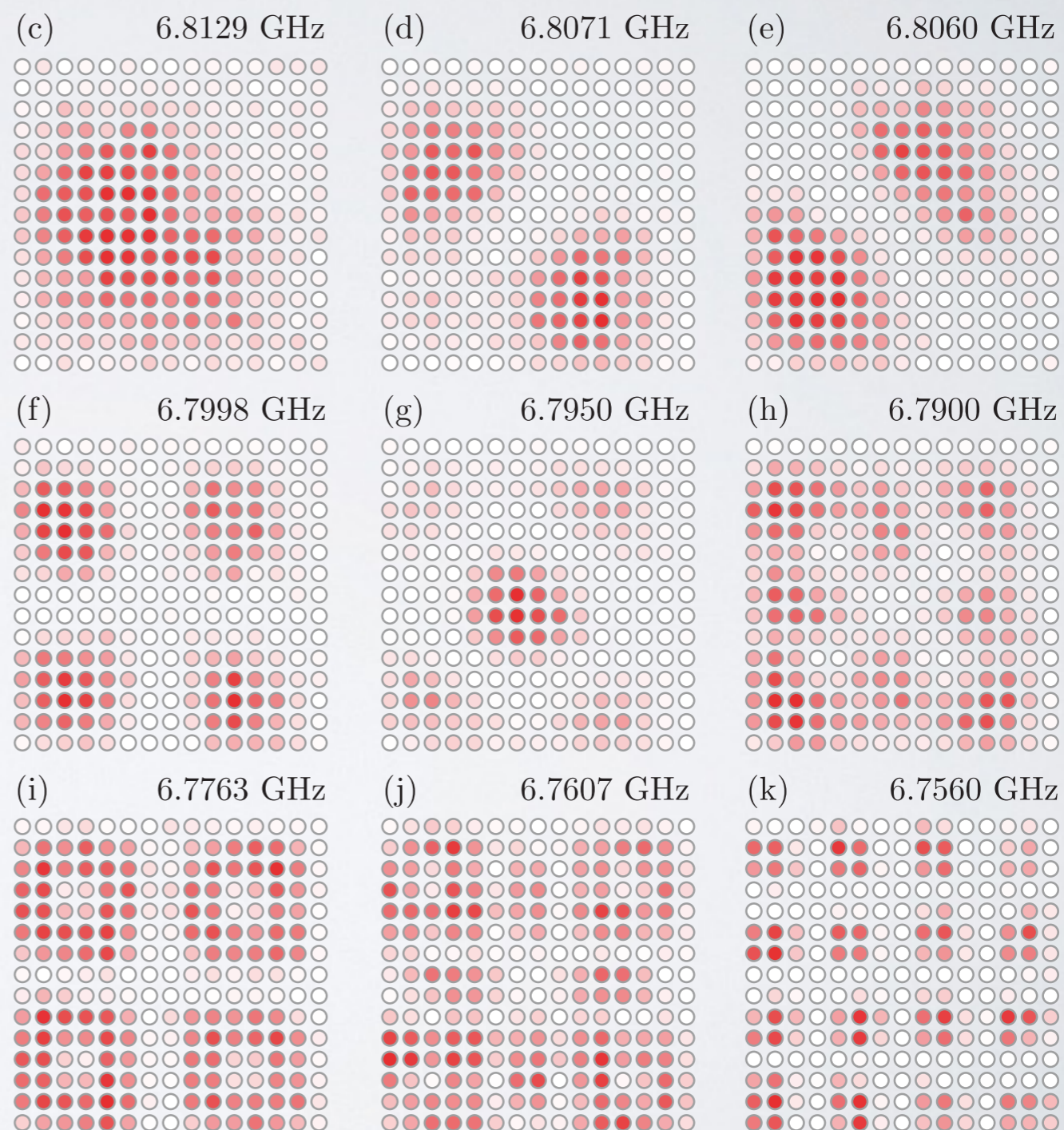
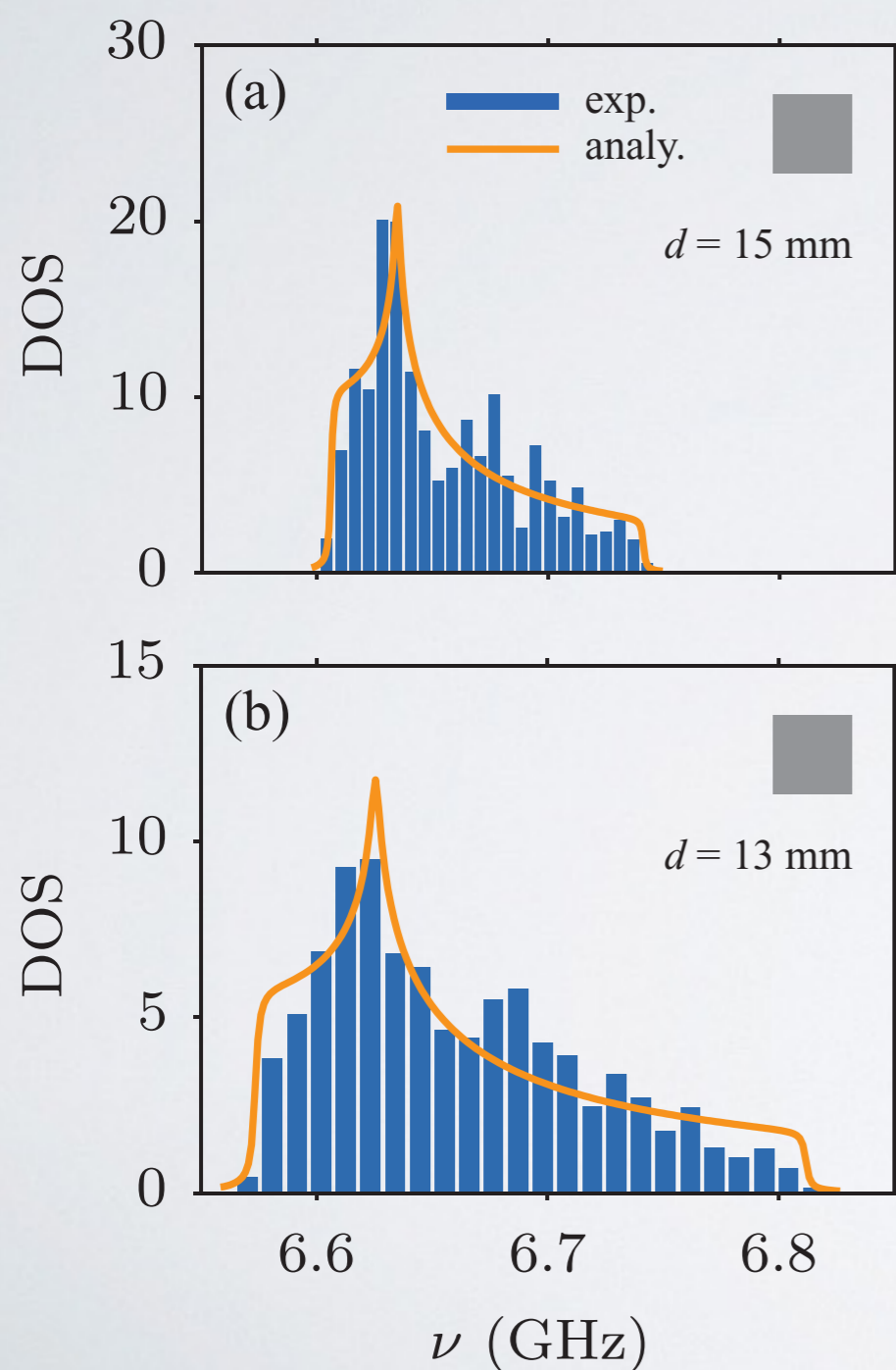
Eigenstates



Eigenstates



A flexible and versatile experimental platform



Outline

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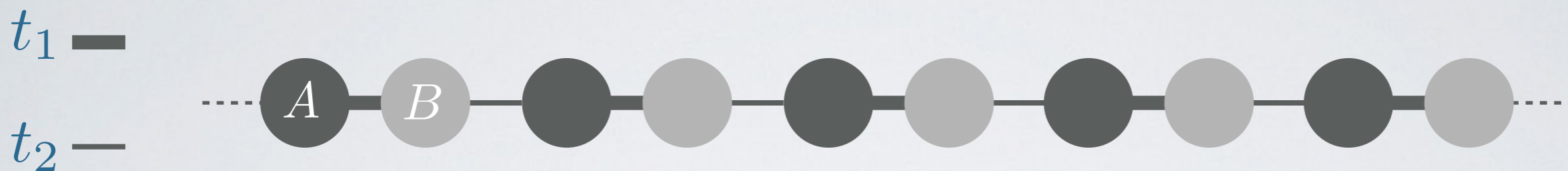
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zero-mode, selective enhancement, non-linear absorption, reflective limiter

3. 2D lattices : Lieb (and Penrose)

partial symmetry breaking, (not so) flat band, zero-mode, gap labeling (naive picture)

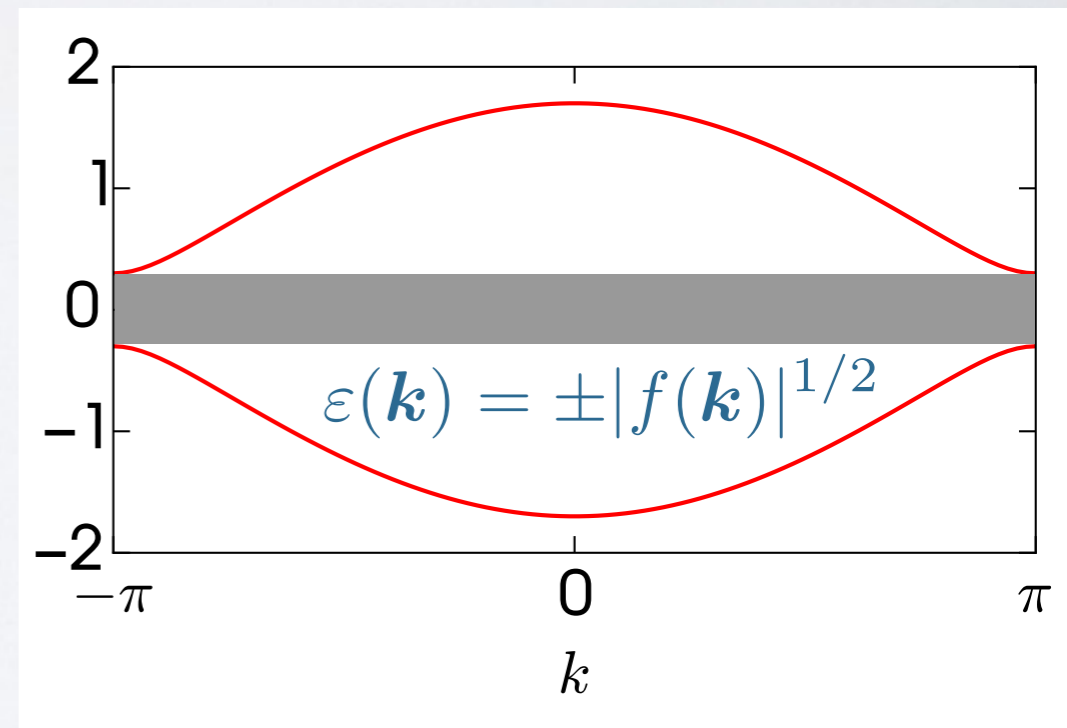
The simplest topological system



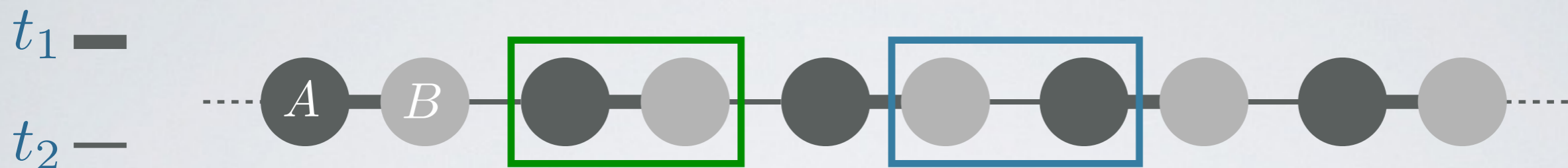
Bloch Hamiltonian:
$$\mathcal{H}_{\mathbf{k}} = \begin{pmatrix} 0 & f^*(\mathbf{k}) \\ f(\mathbf{k}) & 0 \end{pmatrix}$$

Eigenstates:
$$\psi_{\mathbf{k}}^{\pm}(\mathbf{r}) = \frac{1}{\sqrt{2}} \begin{pmatrix} \pm 1 \\ e^{i\phi_{\mathbf{k}}} \end{pmatrix} e^{i\mathbf{k}\cdot\mathbf{r}}$$

Topological quantity:
$$\phi_{\mathbf{k}} = \arg[f(\mathbf{k})]$$



The simplest topological system



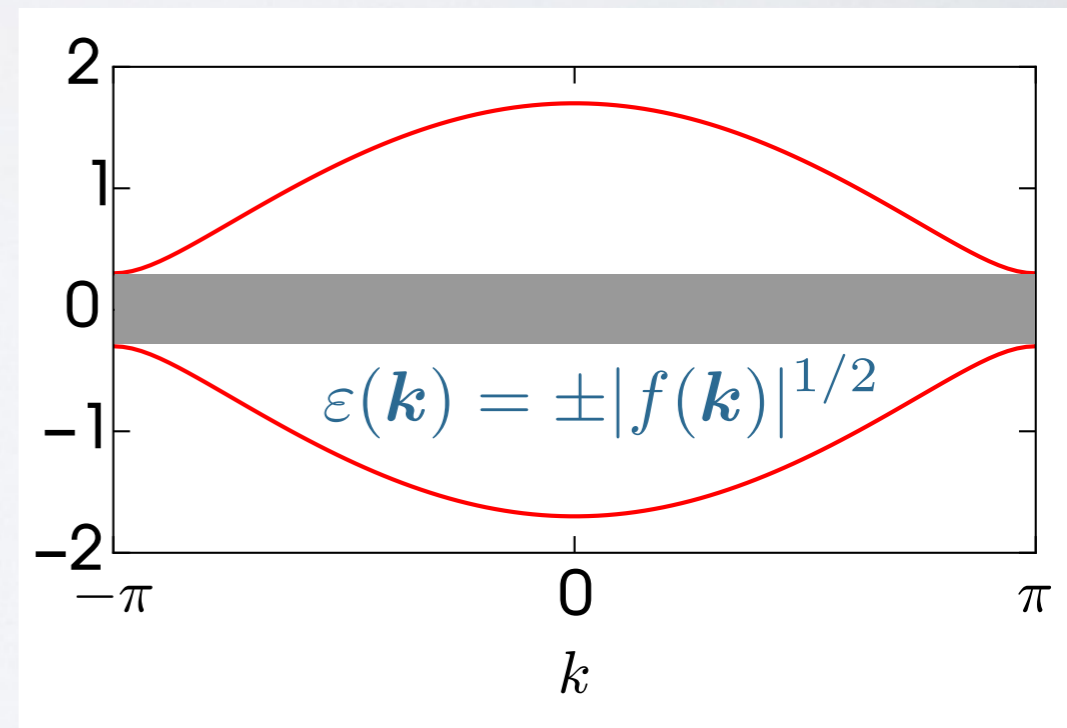
$$f_{\alpha}(\mathbf{k}) = t_1 + t_2 e^{i\mathbf{k}}$$

$$f_{\beta}(\mathbf{k}) = t_2 + t_1 e^{i\mathbf{k}}$$

Bloch Hamiltonian:
$$\mathcal{H}_{\mathbf{k}} = \begin{pmatrix} 0 & f_{\beta}^*(\mathbf{k}) \\ f_{\alpha}(\mathbf{k}) & 0 \end{pmatrix}$$

Eigenstates:
$$\psi_{\mathbf{k}}^{\pm}(\mathbf{r}) = \frac{1}{\sqrt{2}} \begin{pmatrix} \pm 1 \\ e^{i\phi_{\mathbf{k}}} \end{pmatrix} e^{i\mathbf{k} \cdot \mathbf{r}}$$

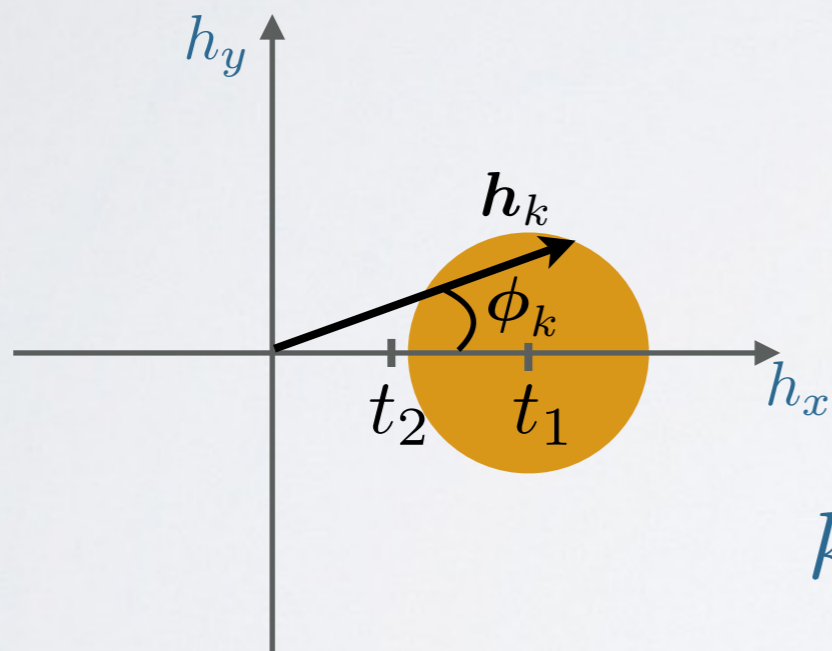
Topological quantity:
$$\phi_{\mathbf{k}} = \arg[f(\mathbf{k})]$$



Two topological phases

$$\mathcal{H}_{\alpha,\beta;\mathbf{k}} = \mathbf{h}_{\alpha,\beta} \cdot \boldsymbol{\sigma} \quad \text{with} \quad \mathbf{h}_{\alpha} = \begin{pmatrix} t_1 + t_2 \cos(k) \\ t_2 \sin(k) \\ 0 \end{pmatrix} \quad \mathbf{h}_{\beta} = \begin{pmatrix} t_2 + t_1 \cos(k) \\ t_1 \sin(k) \\ 0 \end{pmatrix}$$

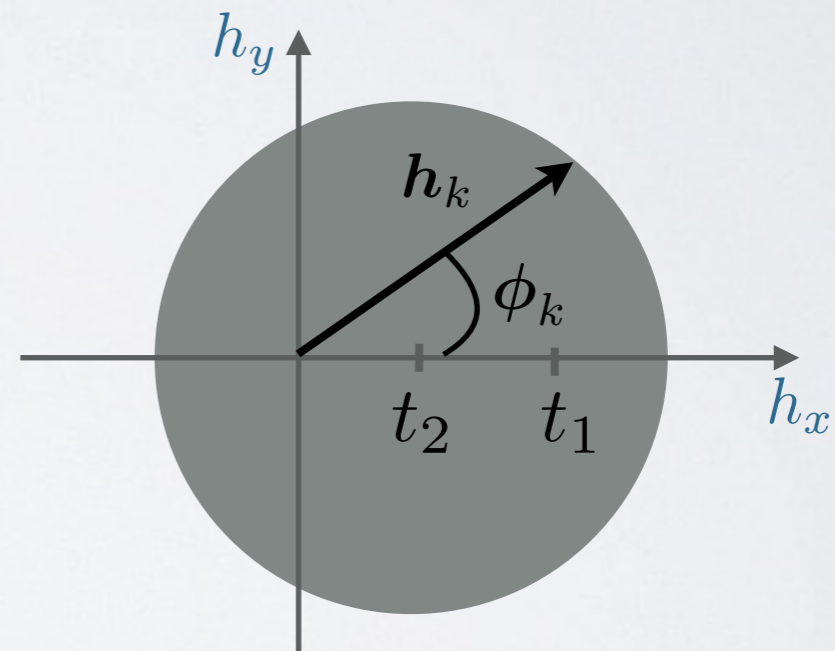
$$(\alpha) : (h_x - t_1)^2 + h_y^2 = t_2^2$$



$$k \in [-\pi, \pi]$$

winding number = 0, $\mathcal{Z} = 0$

$$(\beta) : (h_x - t_2)^2 + h_y^2 = t_1^2$$



winding number = 1, $\mathcal{Z} = \pi$

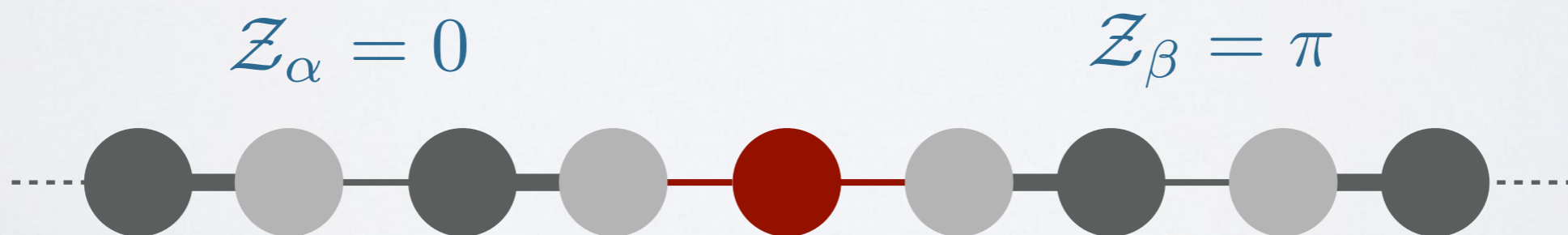
Zak phase corresponds to the Berry phase accumulated by the wavefunction along a path exploring the Brillouin zone.

Topological interface state

In a semi-infinite system, the existence of **edge states** is determined by the topological property of the **bulk wavefunction**:

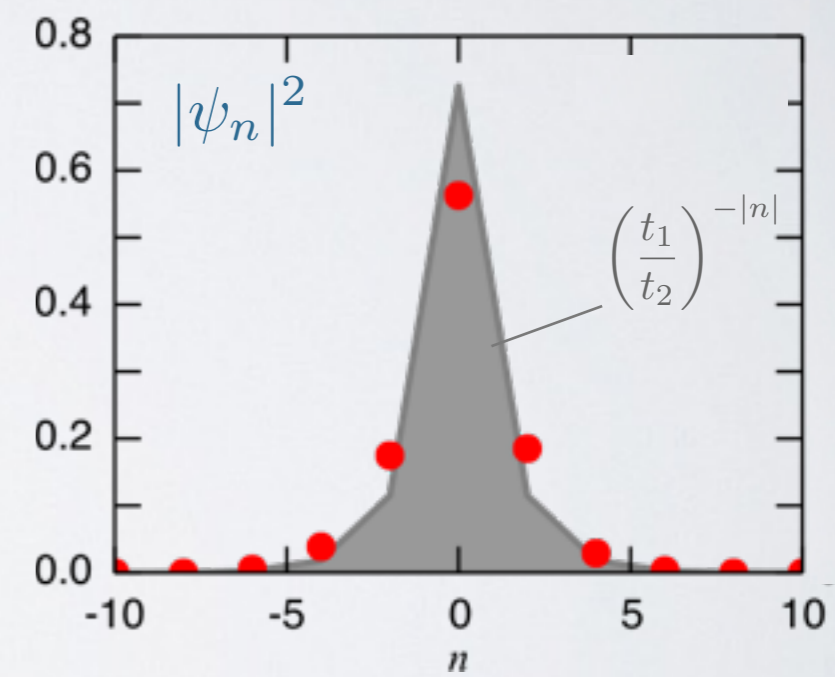
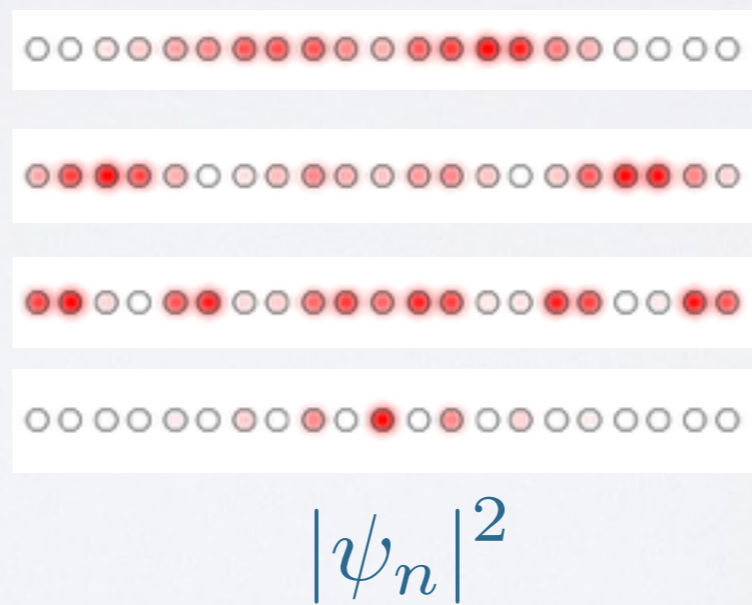
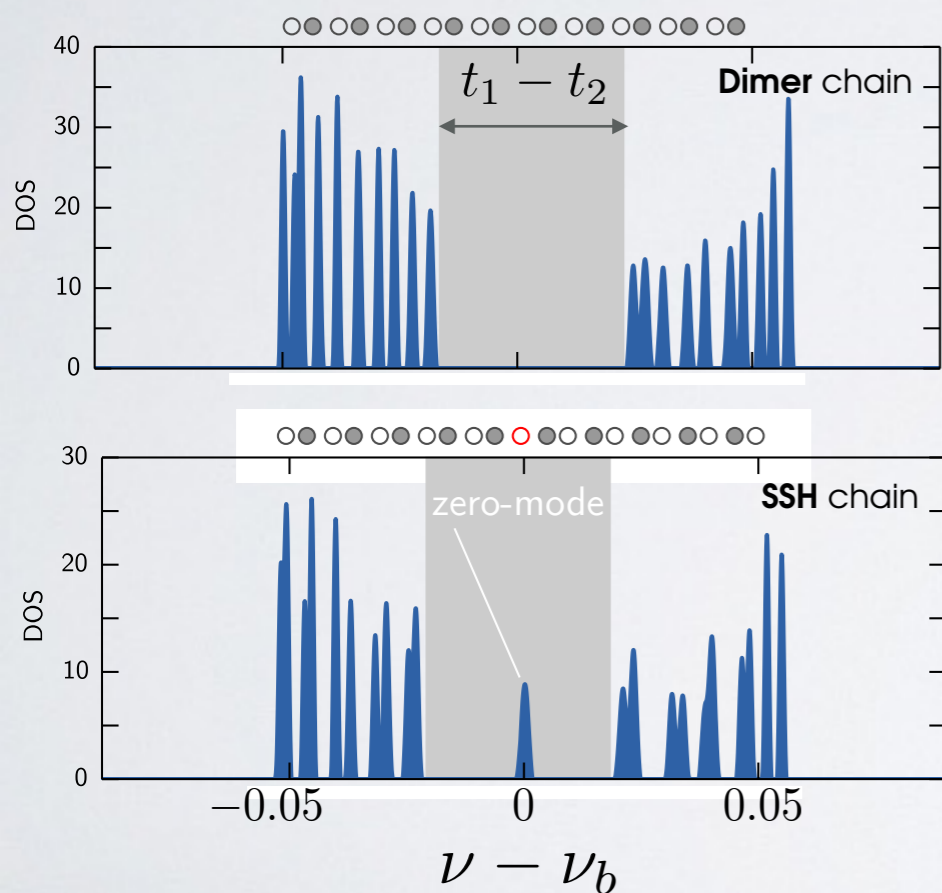
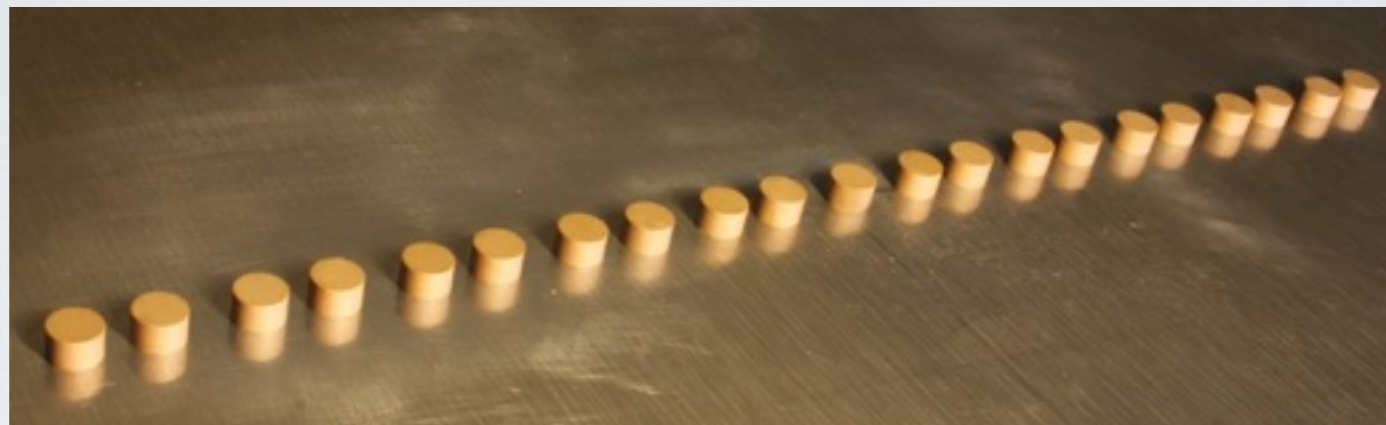


Interface between 2 distinct topological phases:



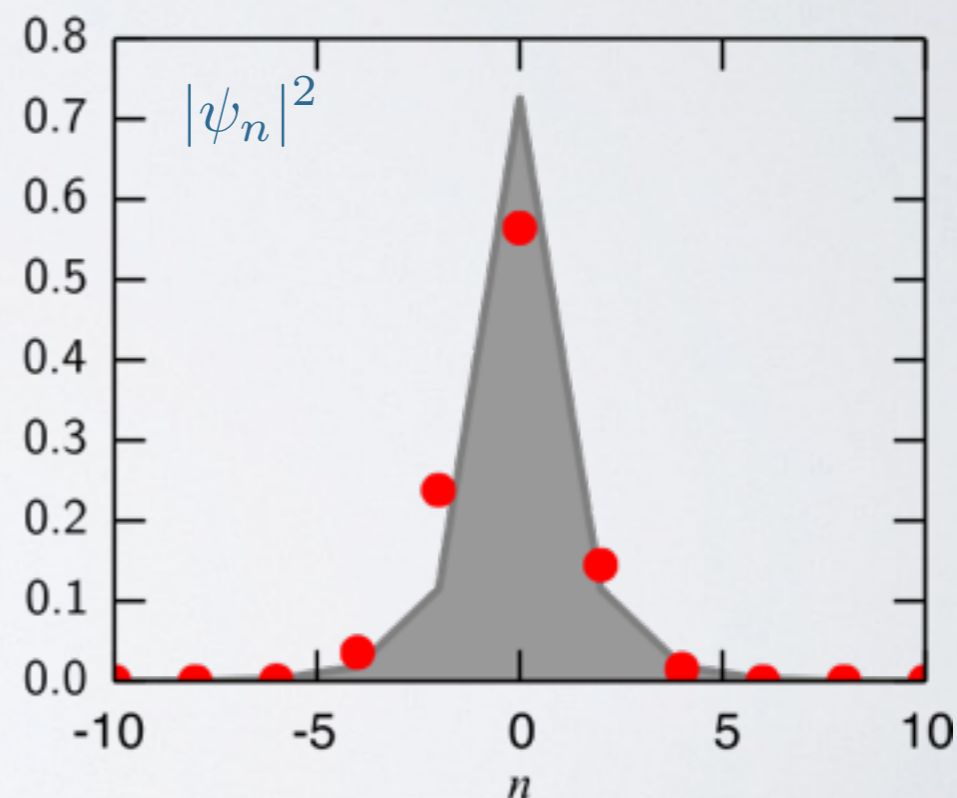
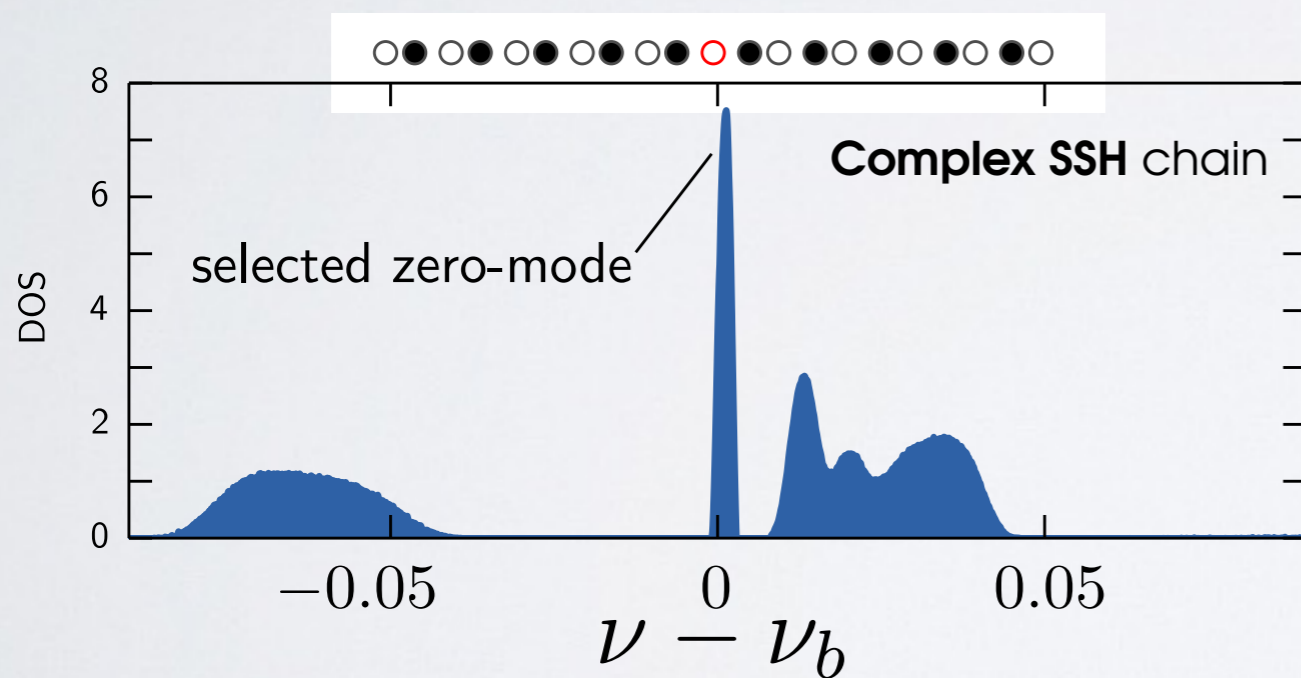
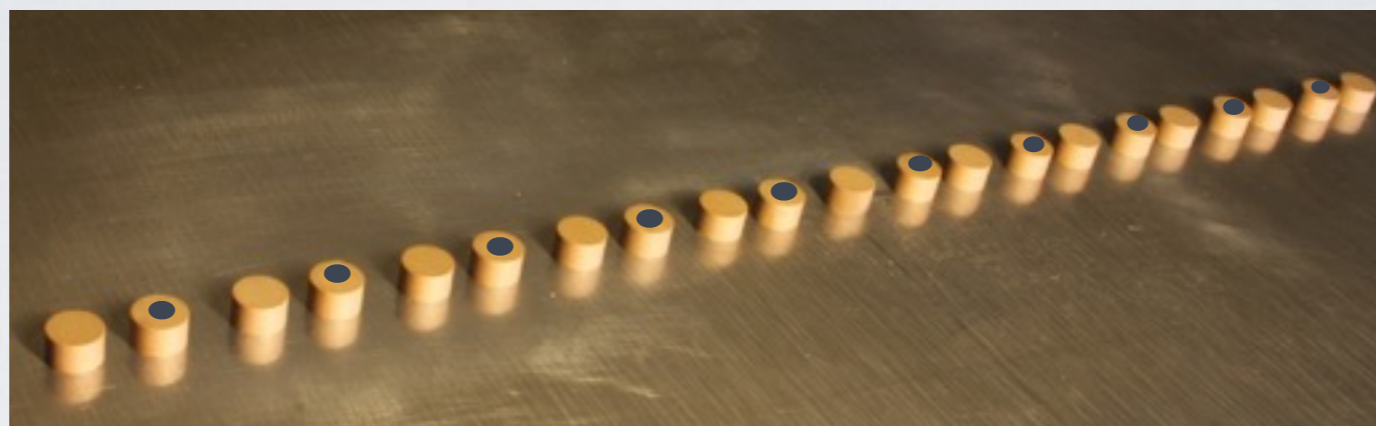
mid-gap topological interface state (zero-mode)

Microwaves realization



- the defect breaks the sublattice (chiral) symmetry
- the interface state is spectrally protected and spatially confined

Selective enhancement by losses

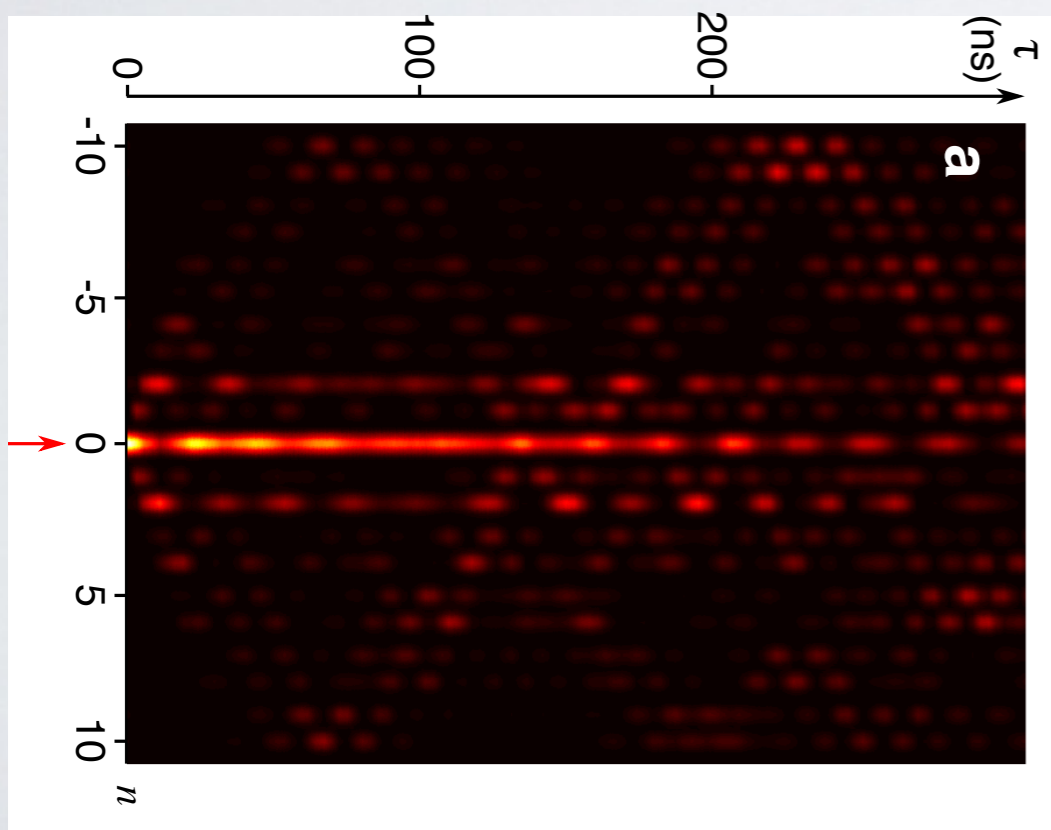
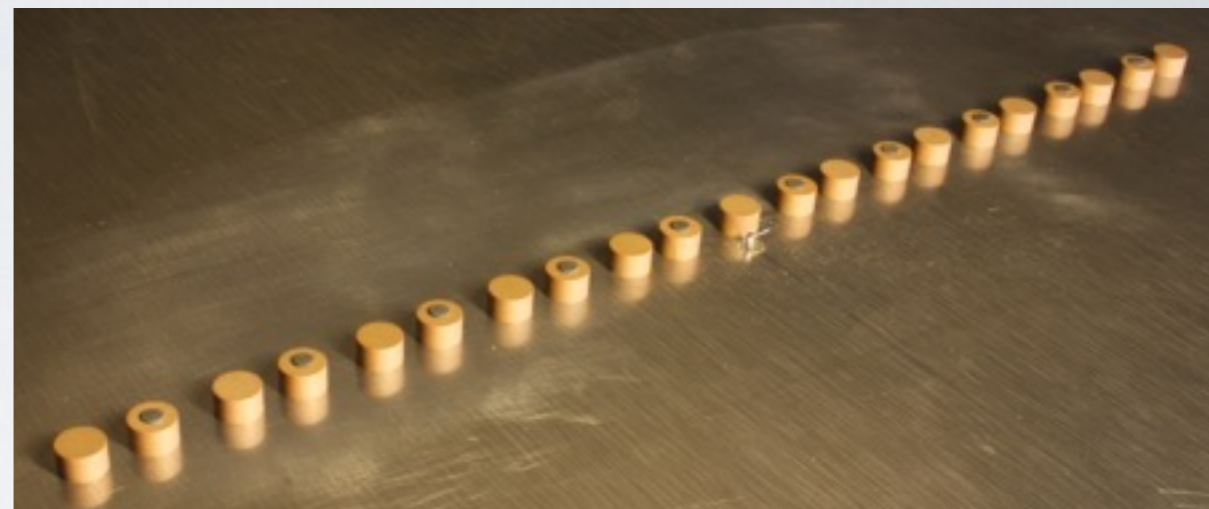


- losses on the B-sublattice through elastomer patches breaks T-symmetry
- the topological state is spectrally and spatially unaffected

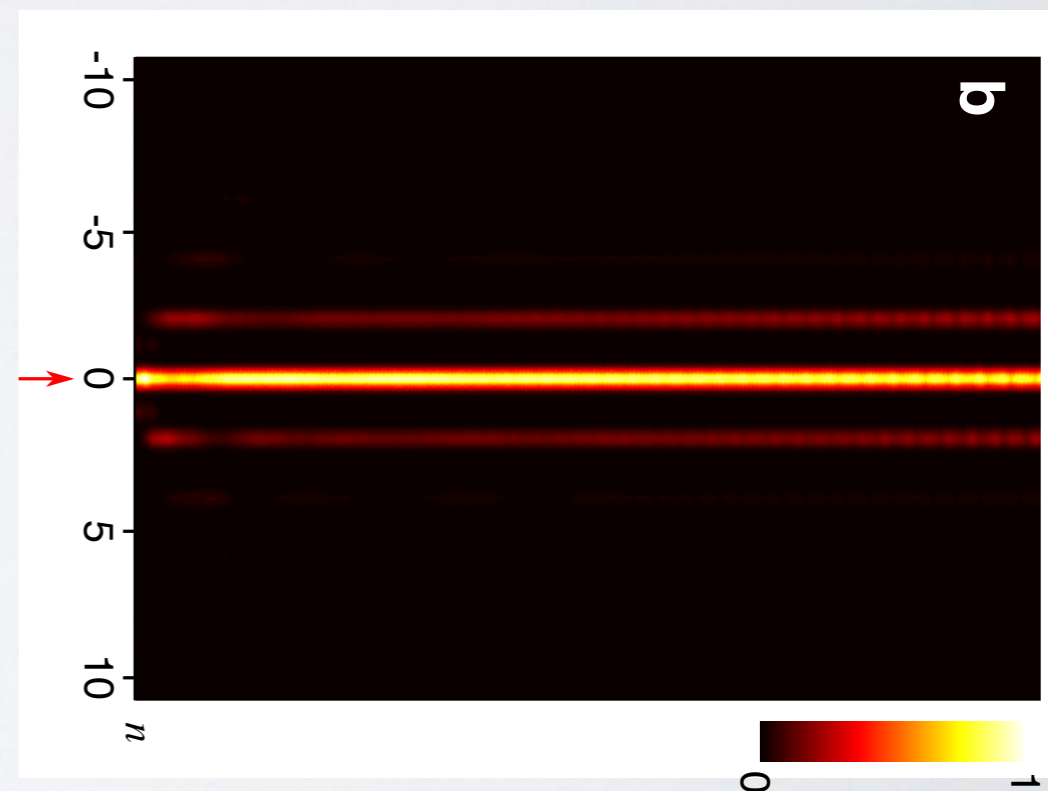
Loss-assisted propagation

transmissions between the defect resonator and all the others :

$$S_{12}(\vec{r}_i, \vec{r}_d; \nu) \xrightarrow{FT} s_i(t)$$



without absorption, diffraction and interferences spoil the propagation

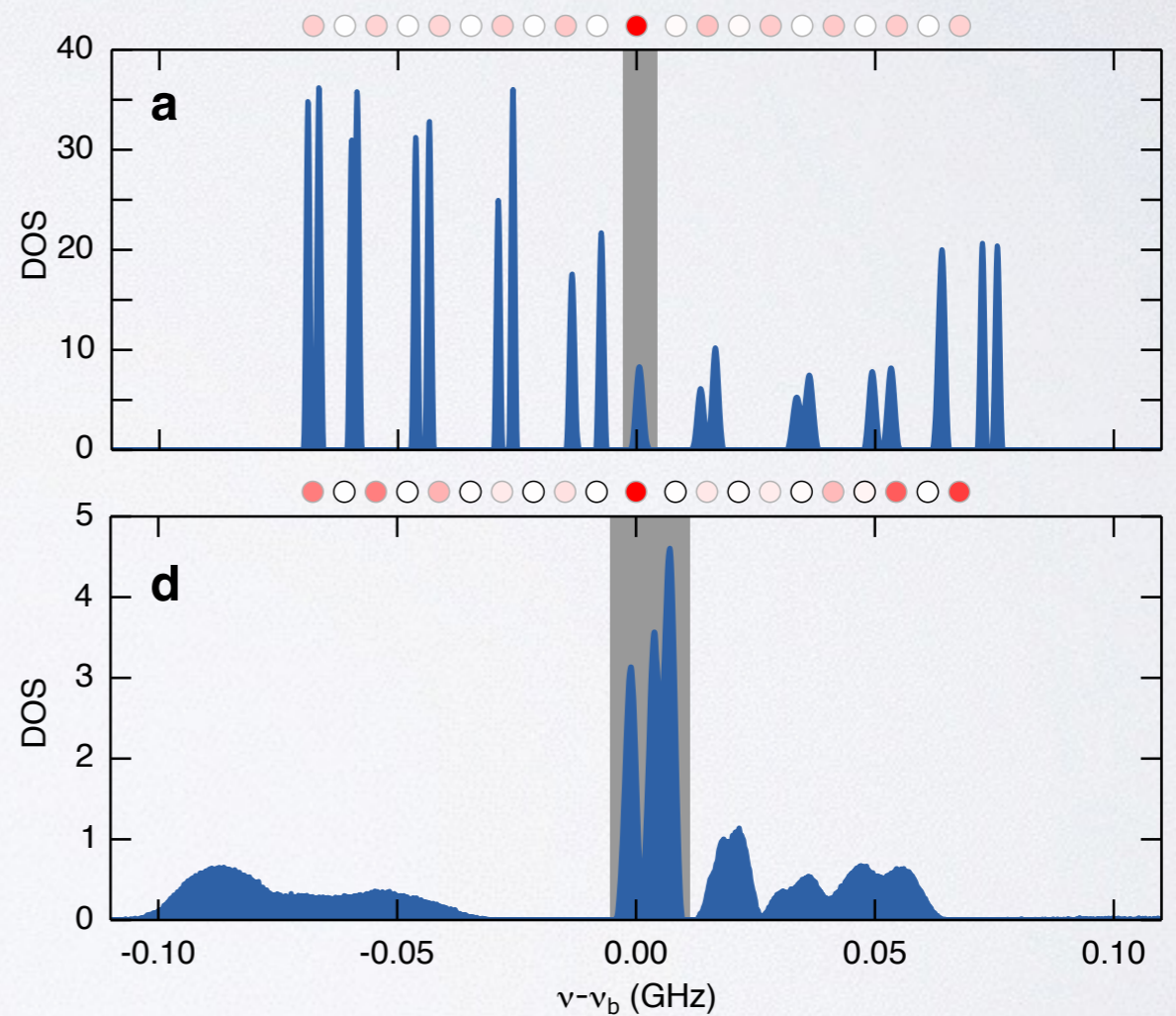


with absorption, the enhanced defect mode dominates the propagation

Topology is crucial

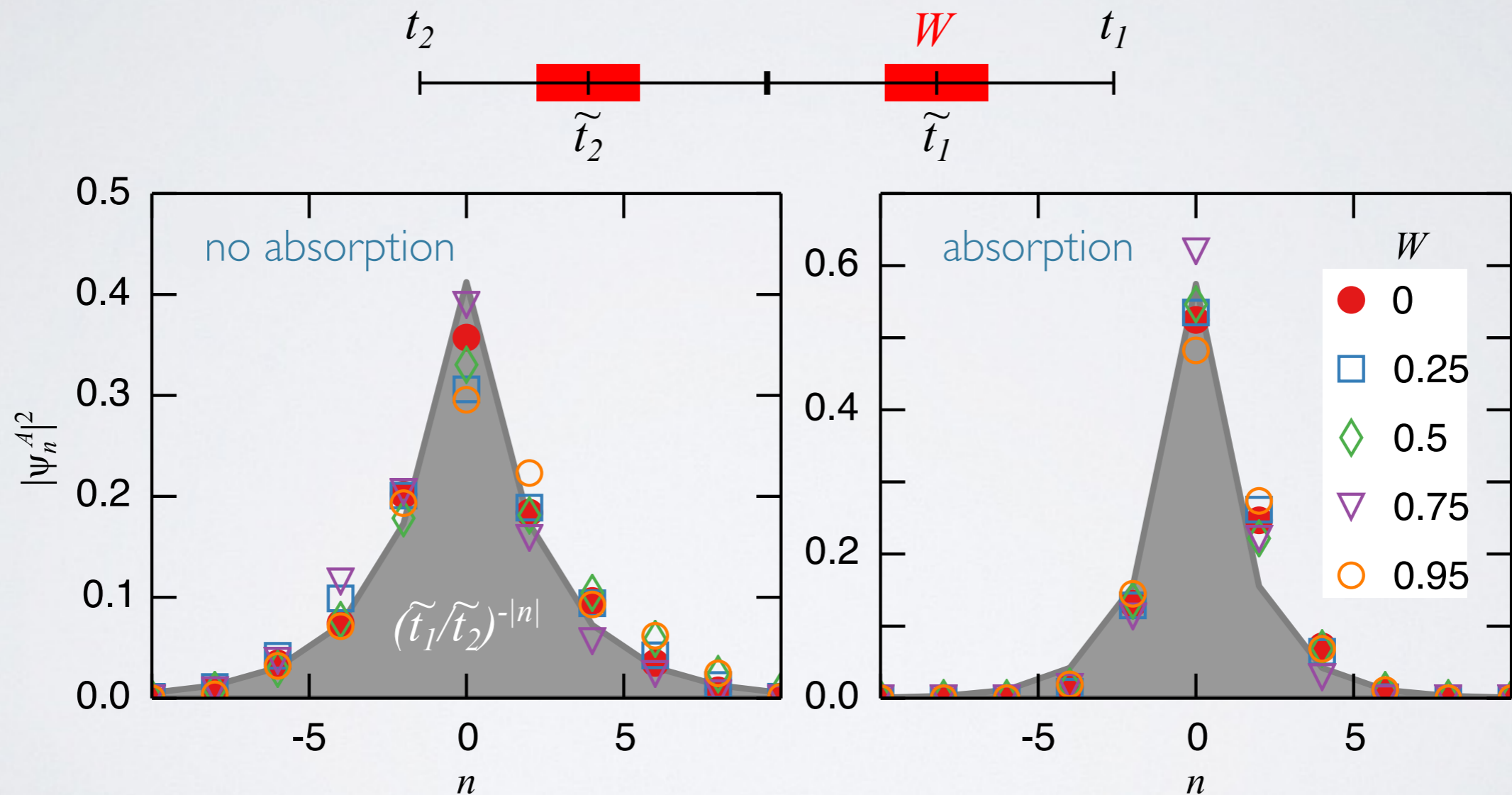
regular chain with central defect:

- localized absorption or disorder hybridizes defect and extended states
- no spectral and spatial topological protections



Robust to disorder

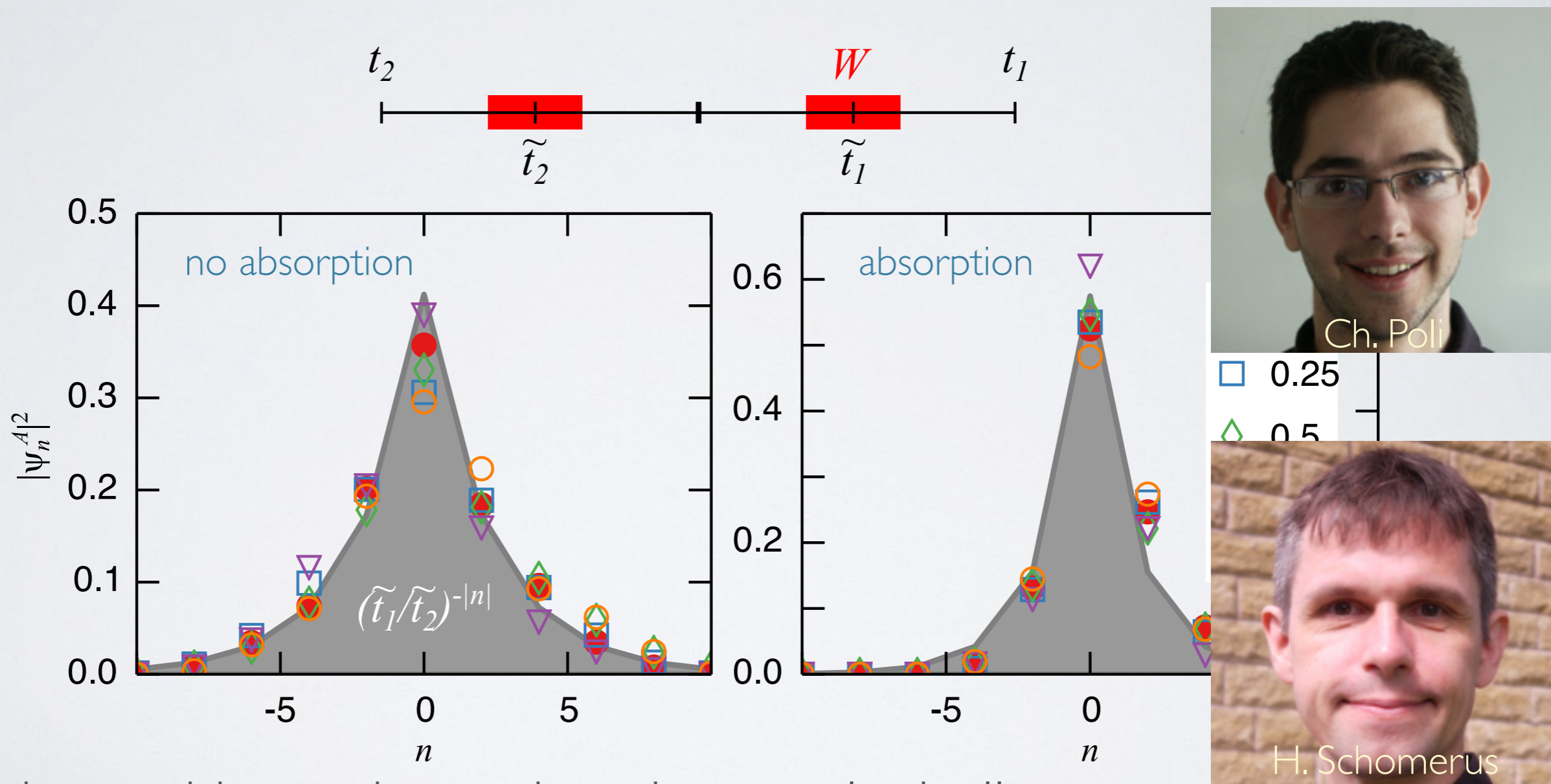
random couplings which preserve the dimer structure



with or without absorption, the topologically protected defect mode is insensitive to structural disorder

Robust to disorder

random couplings which preserve the dimer structure

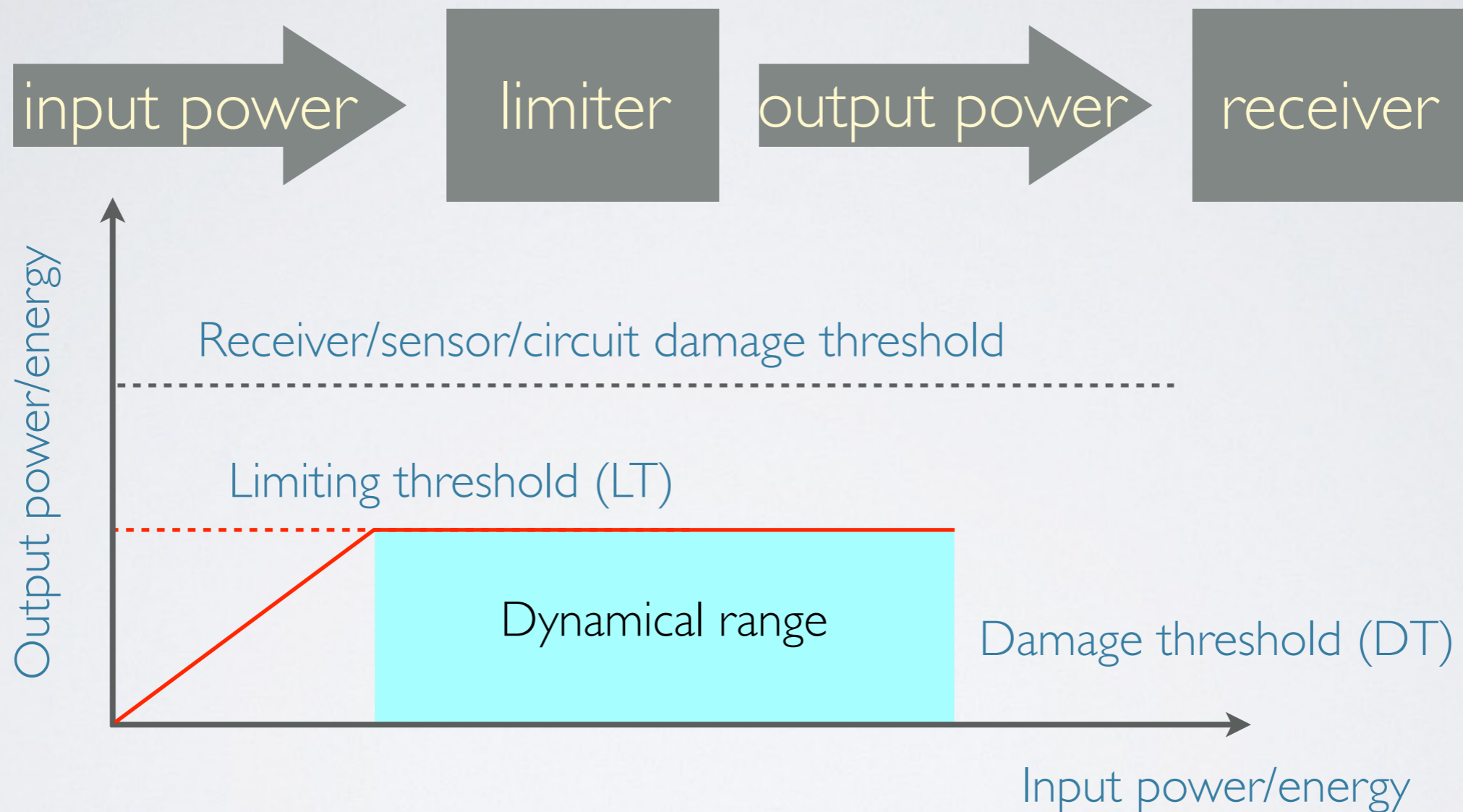


with or without absorption, the topologically protected defect mode is insensitive to structural disorder

Optical limitation

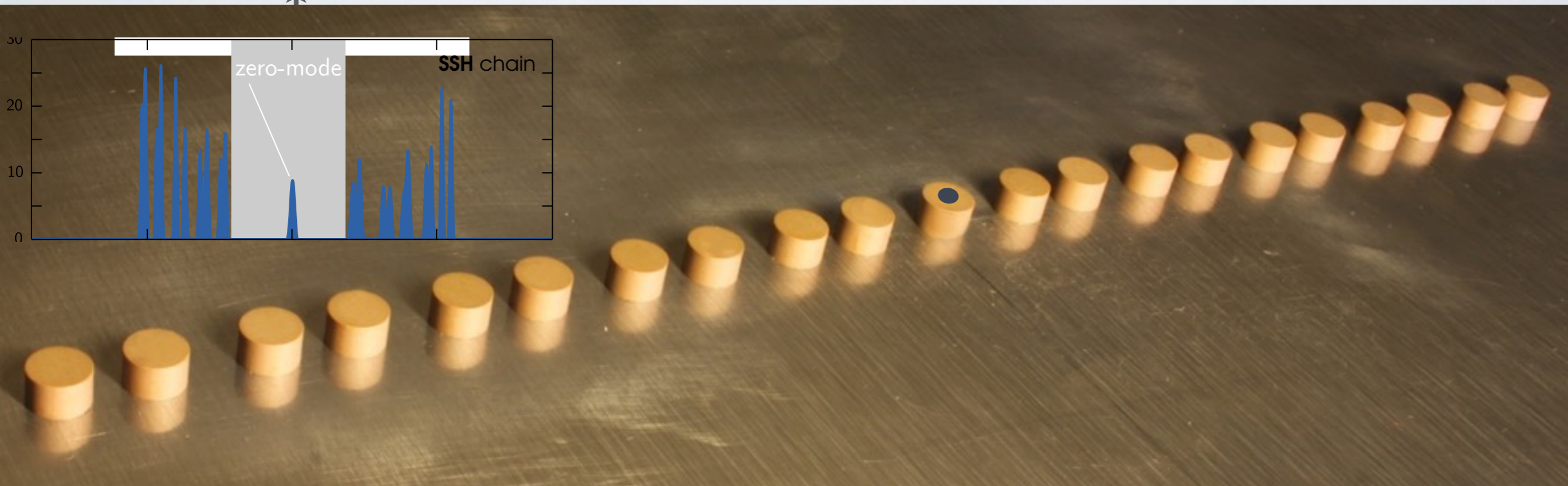
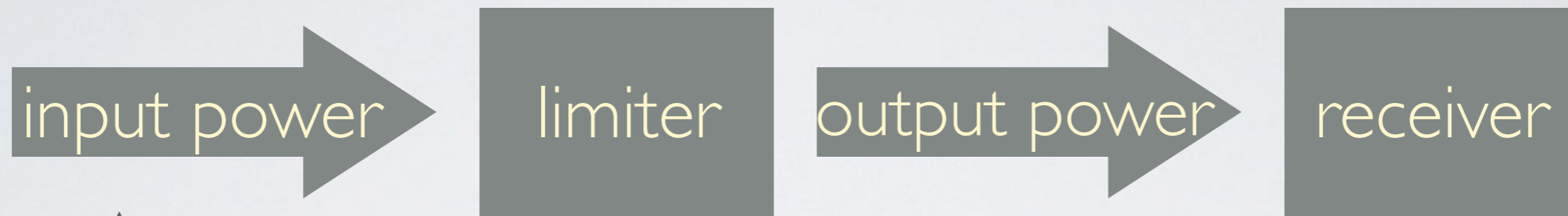


Ideal optical limiter



The larger the dynamical range, the better the limitation.

Ideal optical limiter



The larger the dynamical range, the better the limitation.

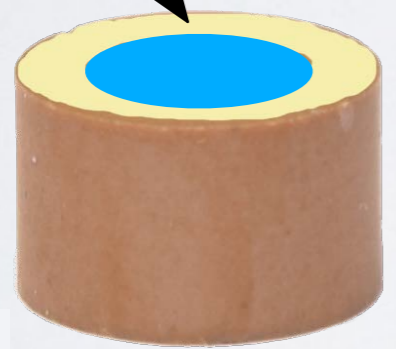
New concept: Topological reflective limiter

Non linear absorption

Losses depend on the strength of the incident radiation

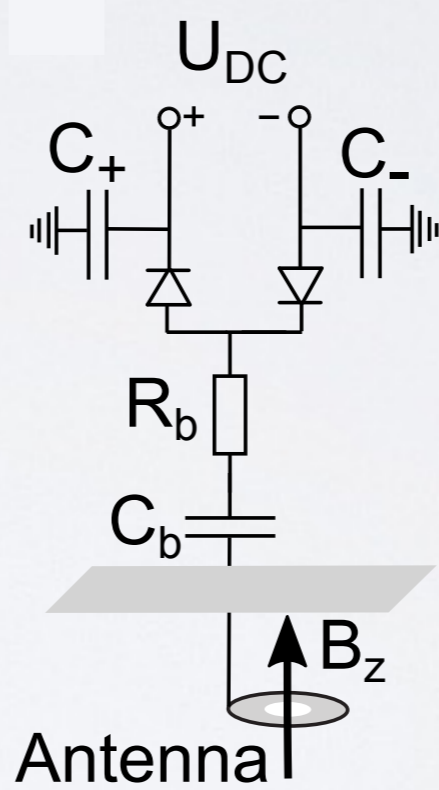
Self-regulated losses

VO₂-Layer



Material with a dielectric to metallic phase transition at some critical temperature.

Reconfigurable losses

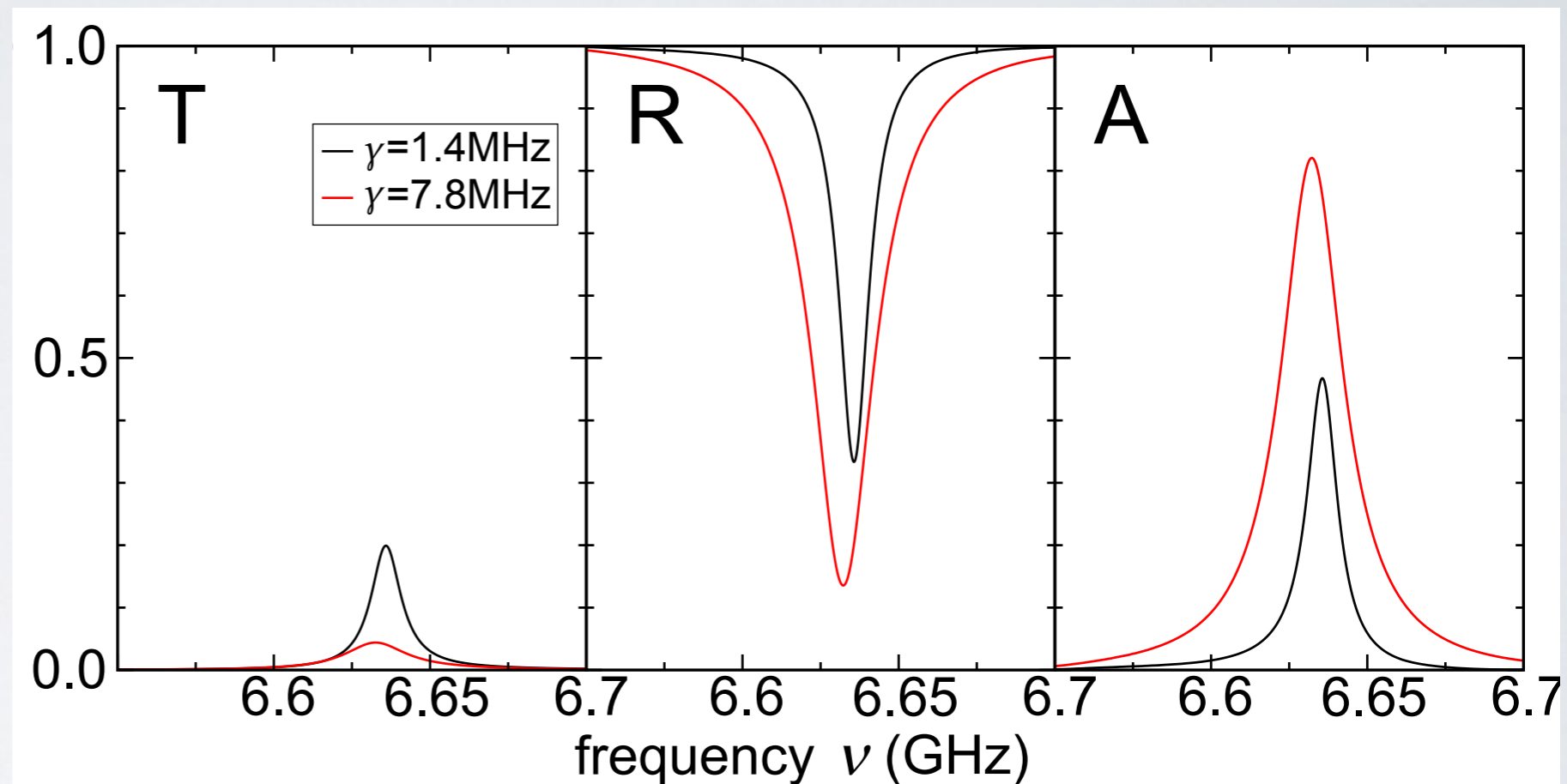
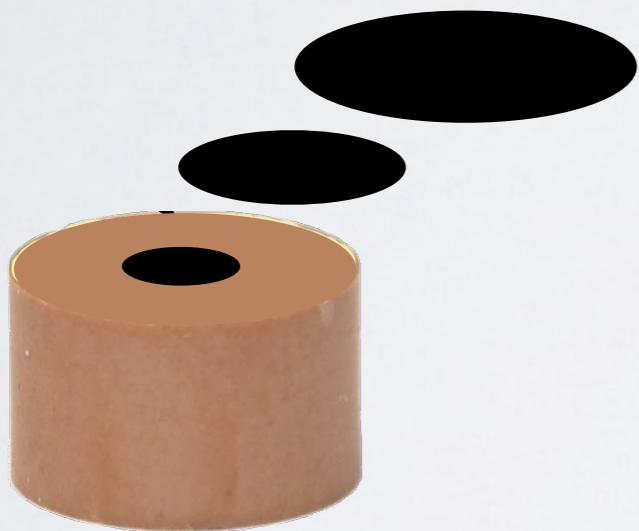


Fast diode providing reconfigurability of the limiting threshold via an externally tuned DC voltage.



Lossy resonator

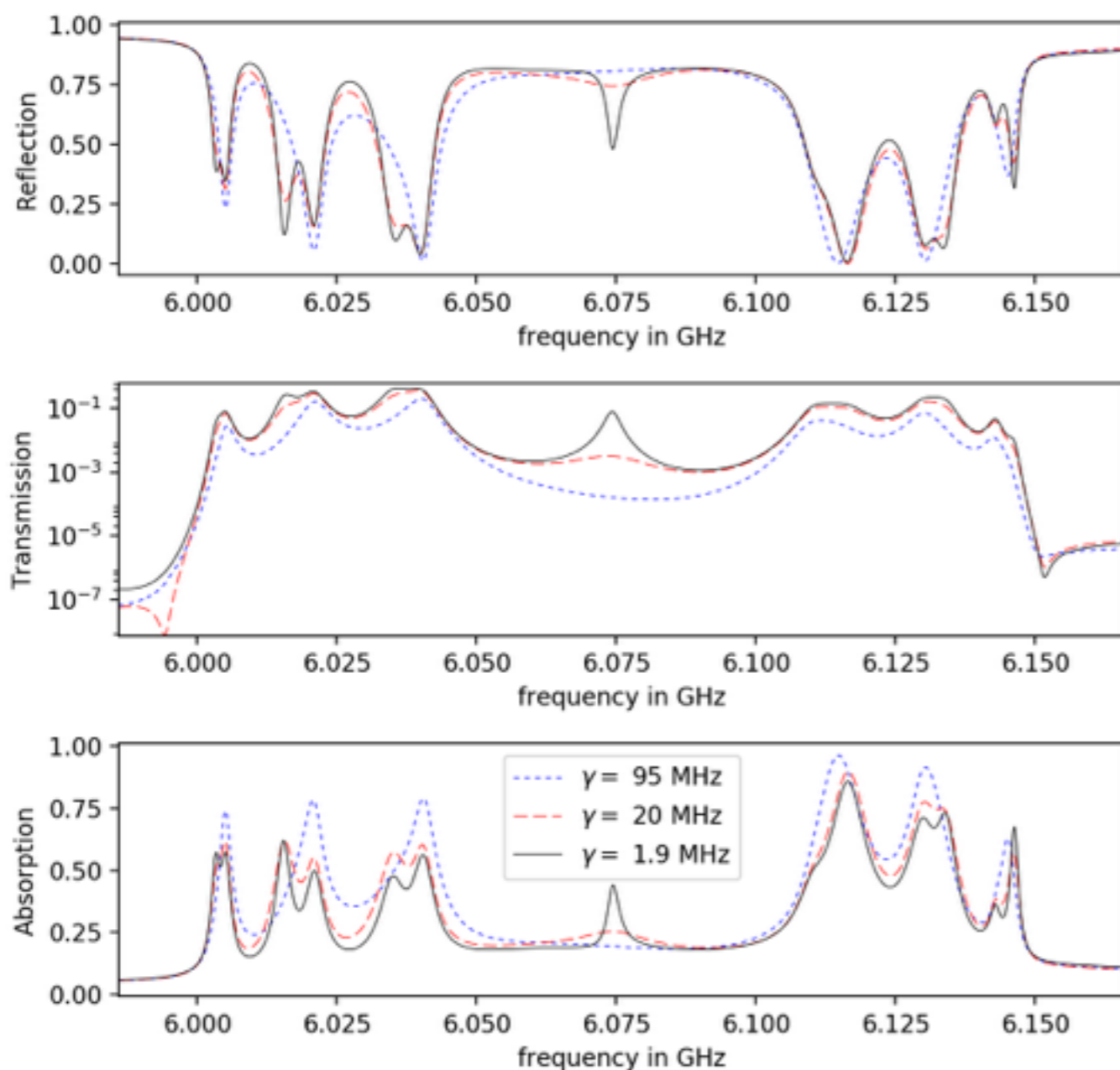
Varying the size of the absorbing patch:



Focus on demonstrating the effect of losses at the defect resonator on the transport properties.

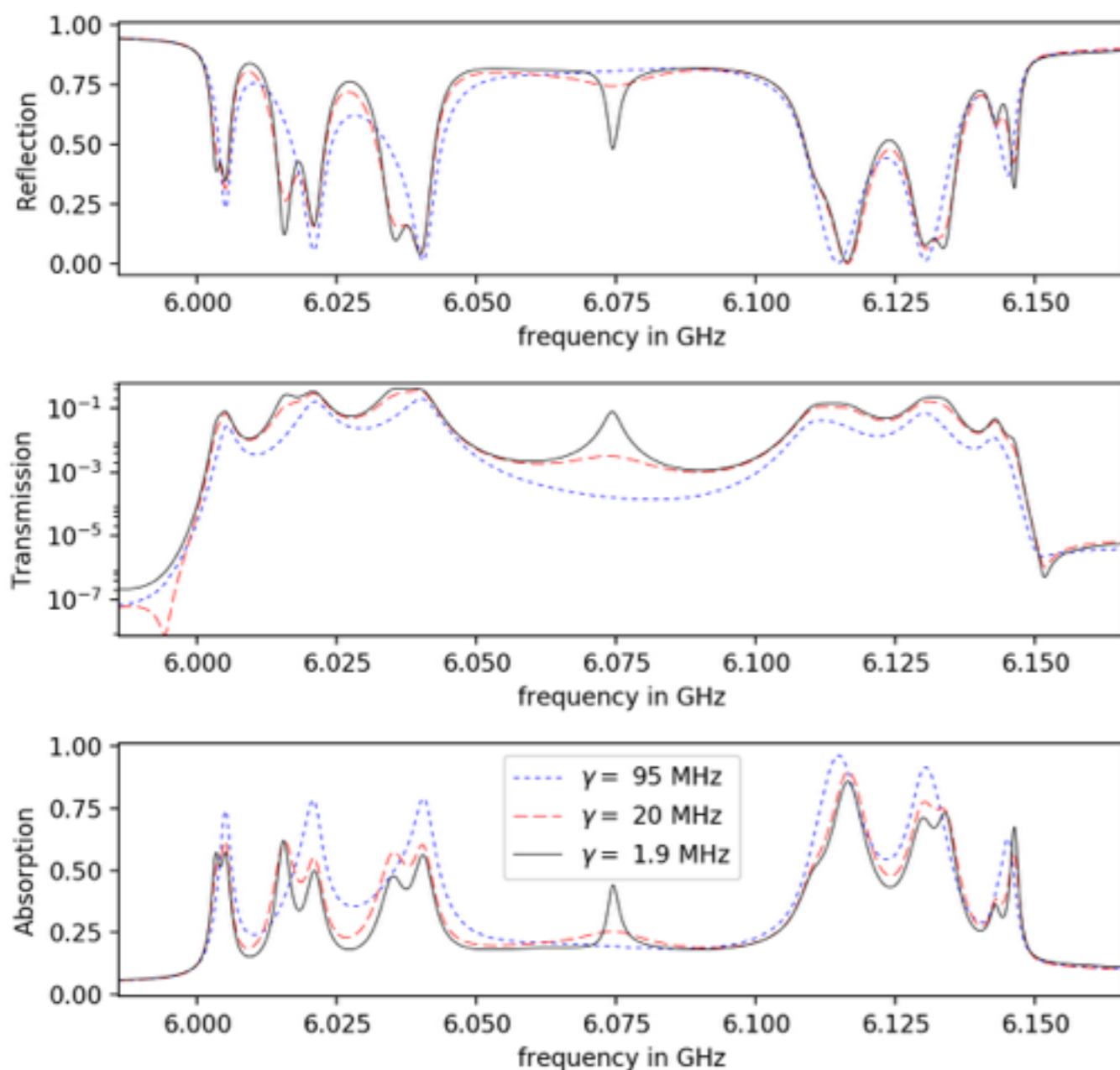
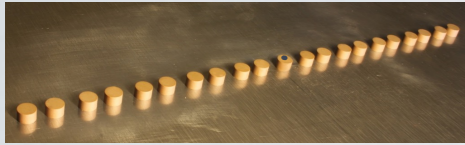
Standalone lossy resonator acts as a sacrificial limiter.

Topology-assisted reflective limiter



- As losses increase the transmission goes down and absorption goes down, meaning that the reflection goes up.
- The topological structure does not overheat because it ‘protects’ the lossy defect by decreasing the value of the field intensity as losses are increasing.

Topology-assisted reflective limiter



- As losses increase, the transmission goes down and absorption goes up, meaning that the field intensity goes up.

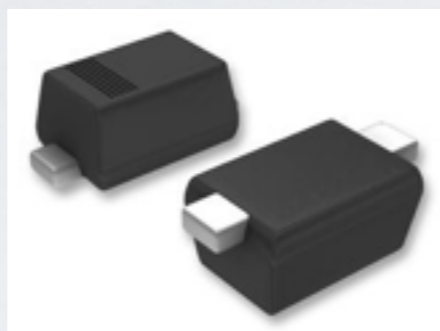


- The topological structure does not overlap with the topological band, 'protects' the low-loss band, and decreasing the loss by decreasing the field intensity and increasing the field intensity and increasing.

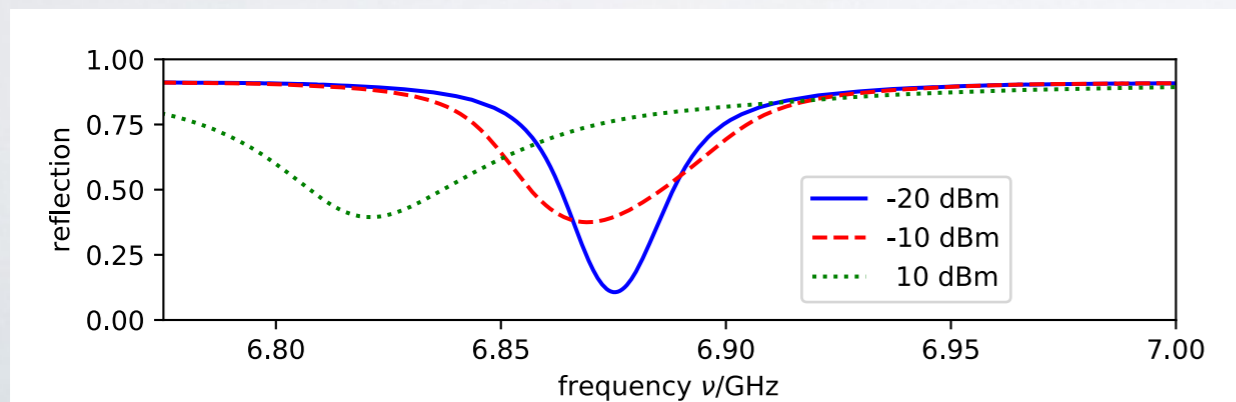
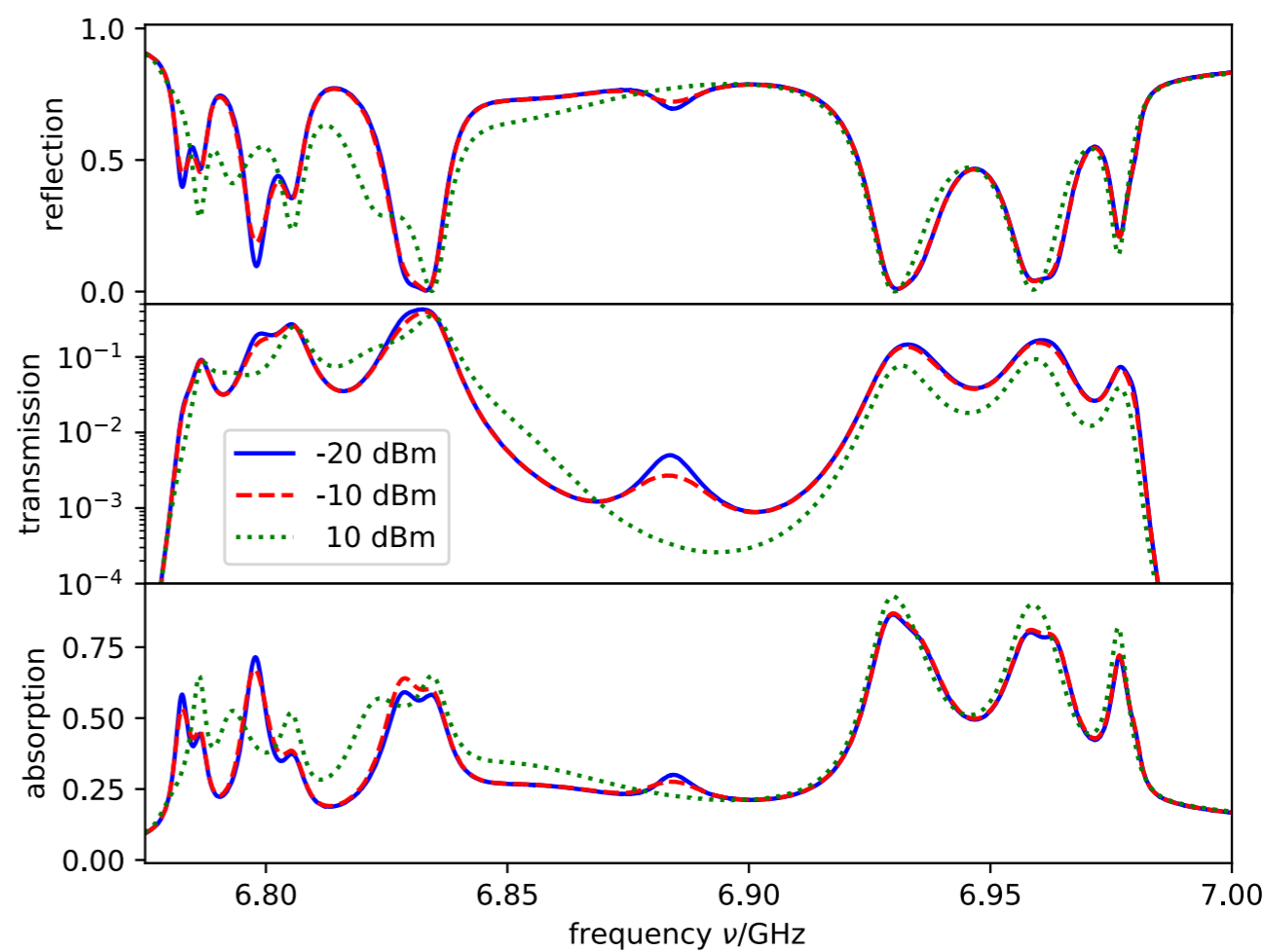


Genuine non-linear losses

Silicon Schottky diode
(Skyworks SMS7630)



Preliminary results: It works !



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dielectric resonators, TE mode, evanescent coupling, LDOS & eigenstates

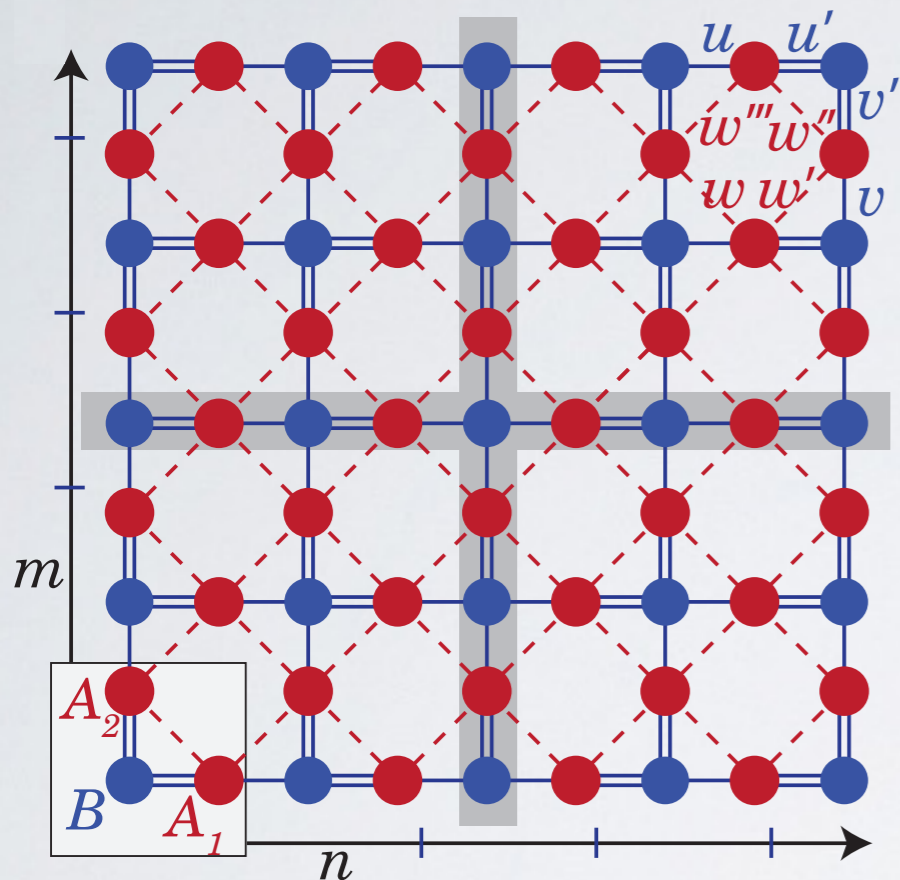
2. SSH chain: Control of topological interface states

zero-mode, selective enhancement, non-linear absorption, reflective limiter

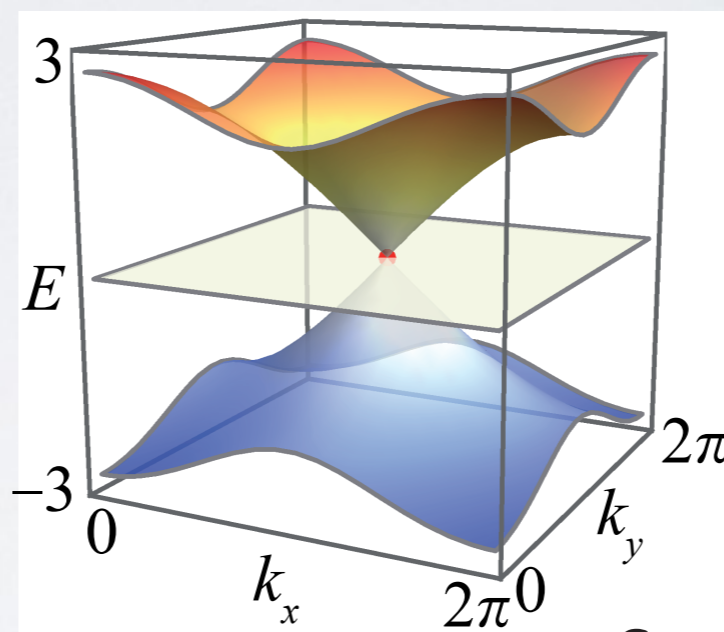
3. 2D lattices : Lieb (and Penrose)

partial symmetry breaking, (not so) flat band, zero-mode, gap labeling (naive picture)

Lieb lattice

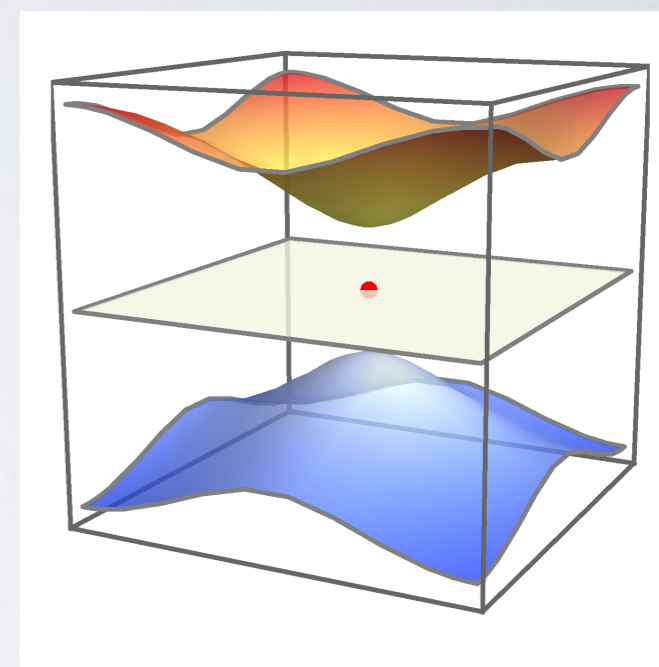


uniform couplings:
topologically boring...



$$u = u' = v = v' \quad w^{(i)} = 0$$

more interesting
when dimerized:



$$2u = 2v = u' = v' \quad w^{(i)} = 0$$

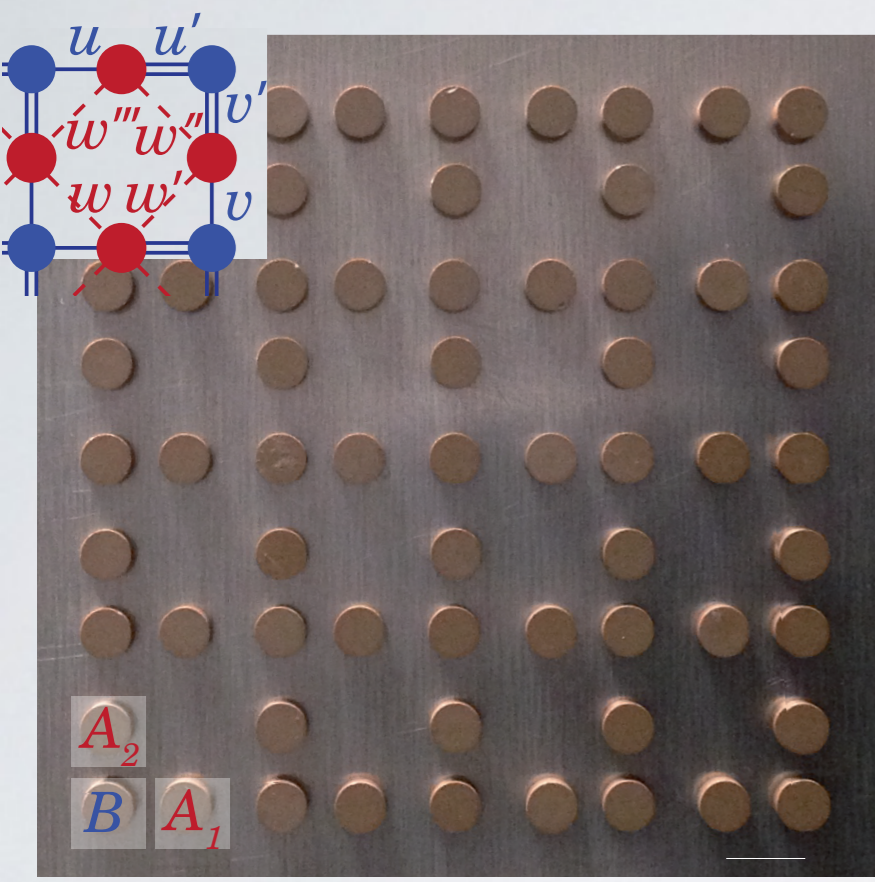
Global chiral symmetry:

$$H_{\text{TB}}(\vec{k}) = \begin{pmatrix} 0 & t_{AB}(\vec{k}) \\ t_{BA}(\vec{k}) & 0 \end{pmatrix}$$

$$\sigma_z H_{\text{TB}}(\vec{k}) \sigma_z = -H_{\text{TB}}(\vec{k})$$

- flat band on the majority sublattice
- with an appropriate choice of boundary conditions: one extra zero-mode on the minority sublattice (B sites)... but still degenerated with the flat band.

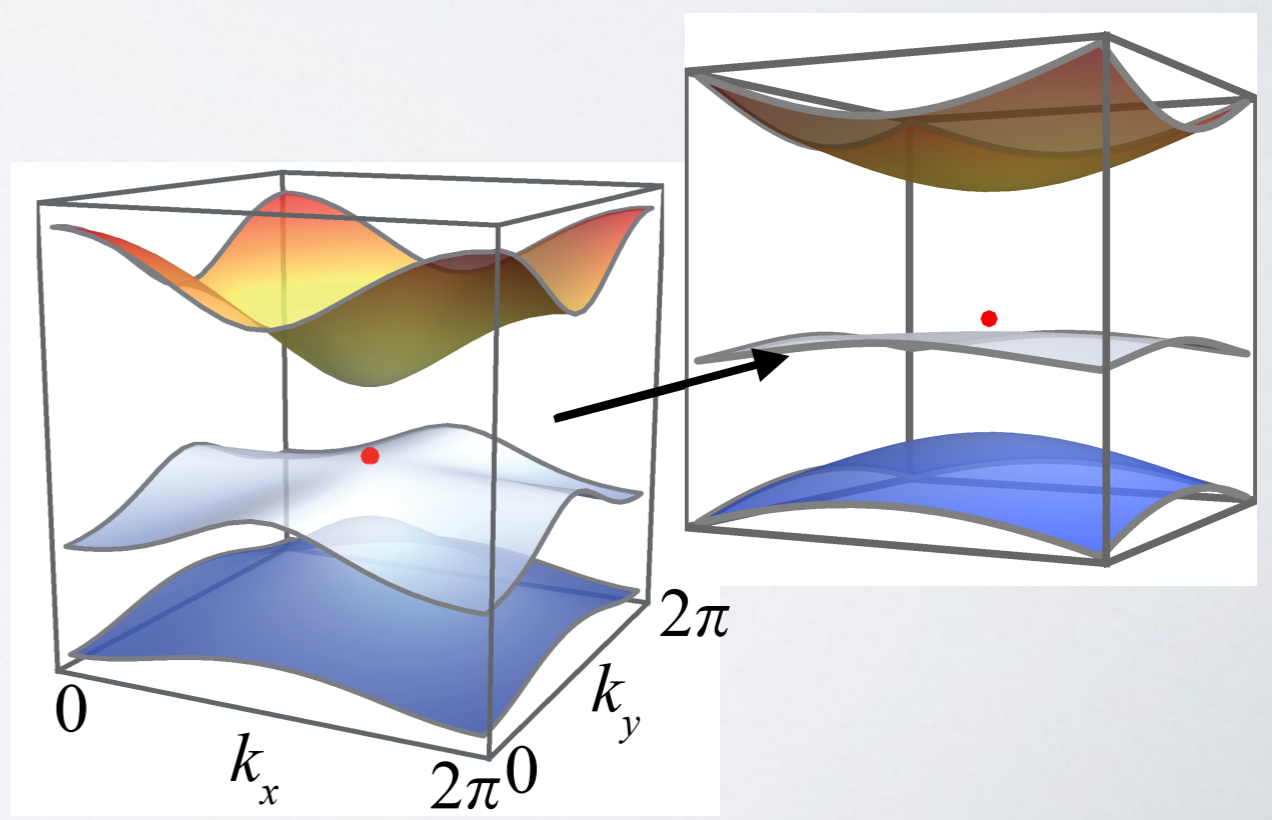
Partial chiral symmetry



In the experiment, next-nearest neighbor couplings are effective: $w'' > w' = w''' > w$

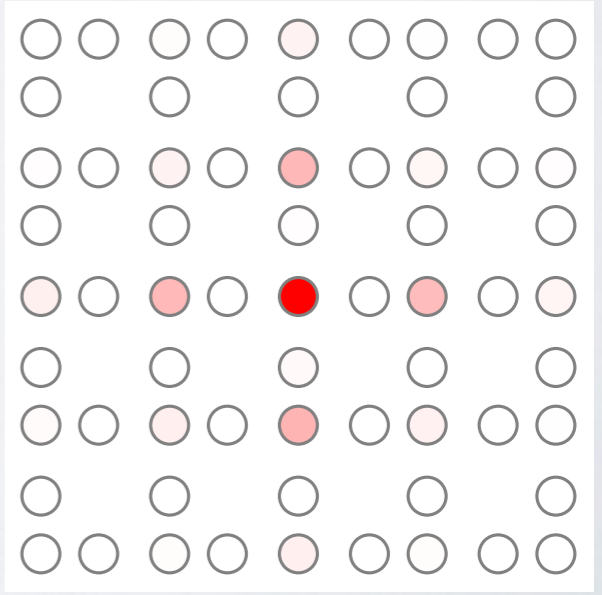
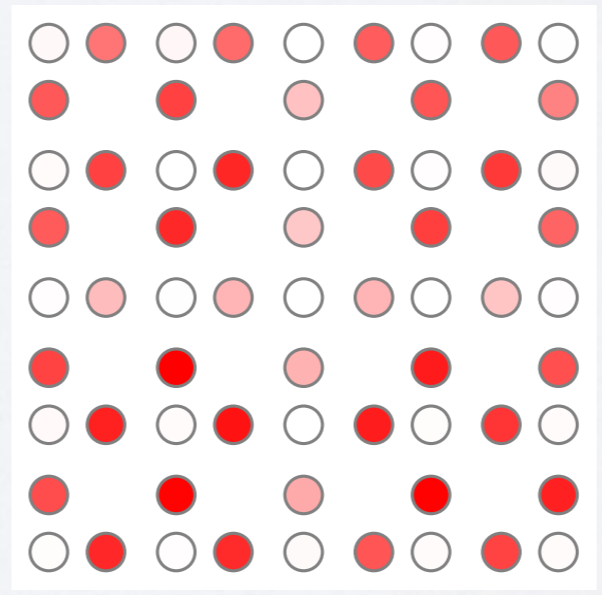
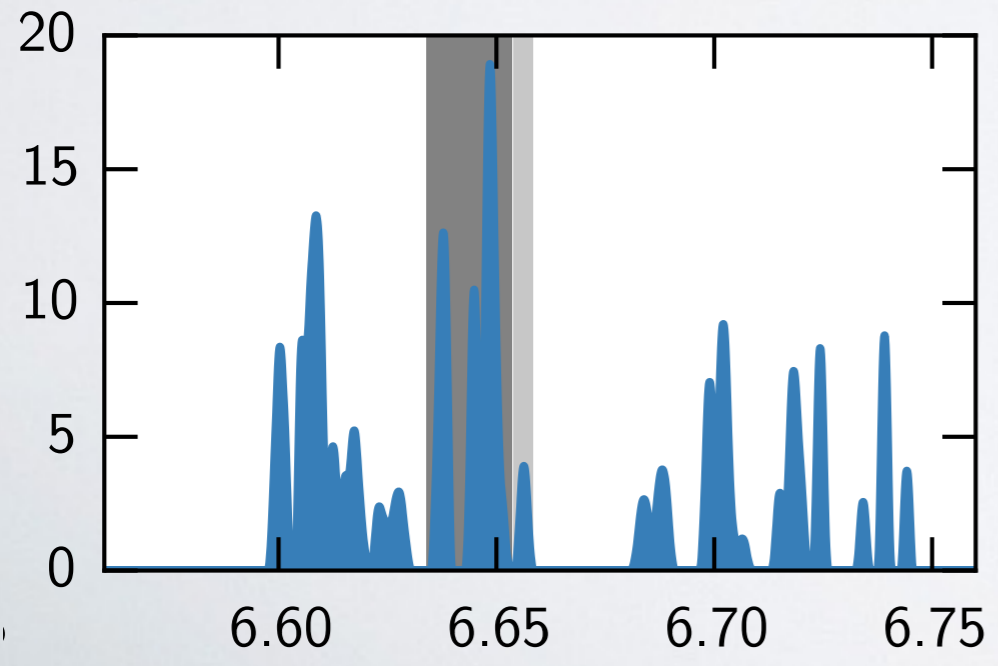
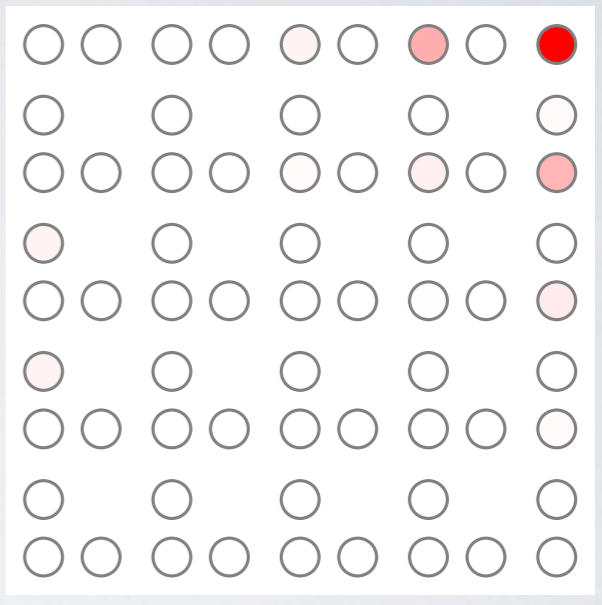
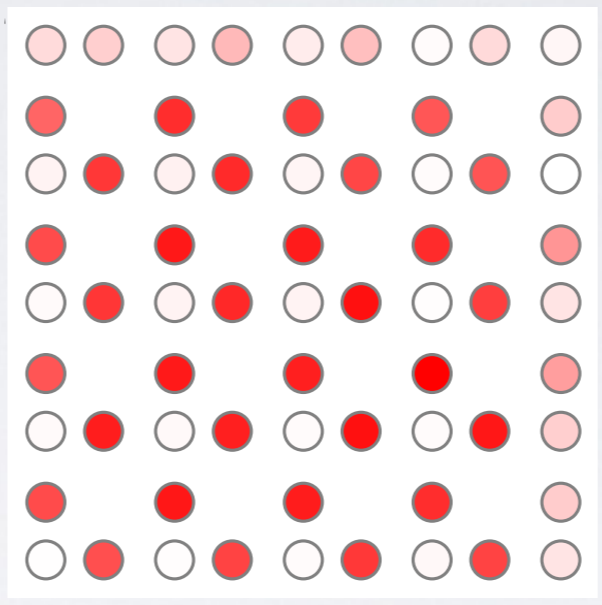
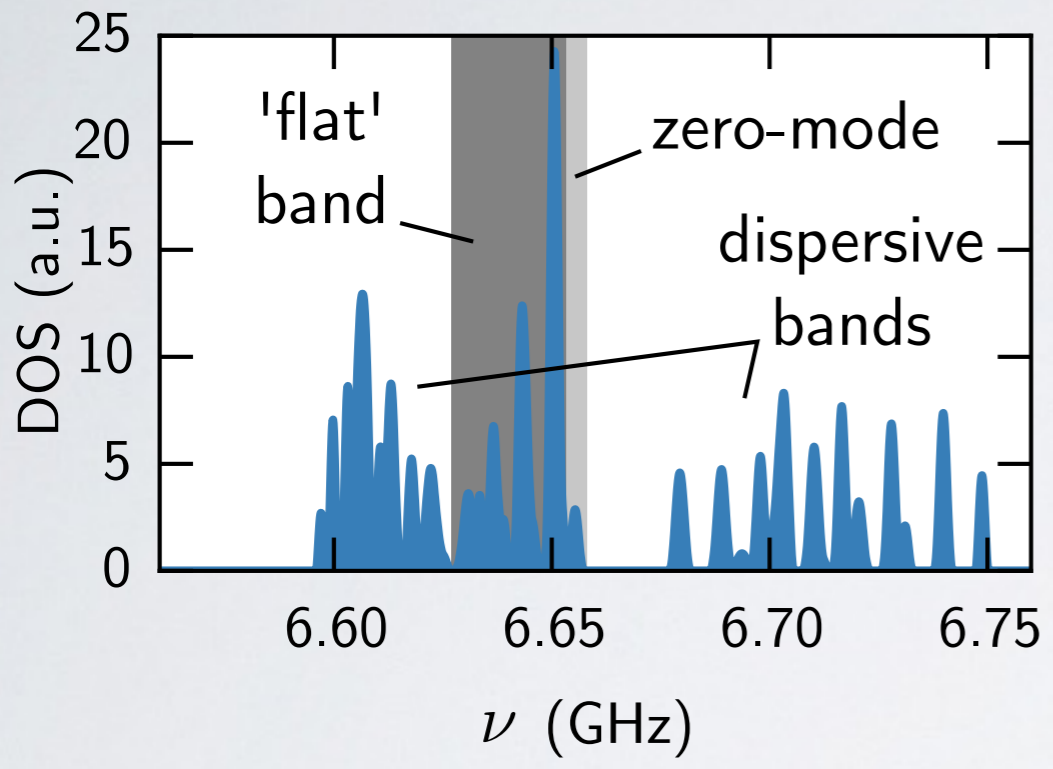
$$H_{\text{TB}}(\vec{k}) = \begin{pmatrix} t_{AA}(\vec{k}) & t_{AB}(\vec{k}) \\ t_{BA}(\vec{k}) & 0 \end{pmatrix}$$

$$[\sigma_z H_{\text{TB}}(\vec{k}) \sigma_z]_{BB} = [-H_{\text{TB}}(\vec{k})]_{BB}$$



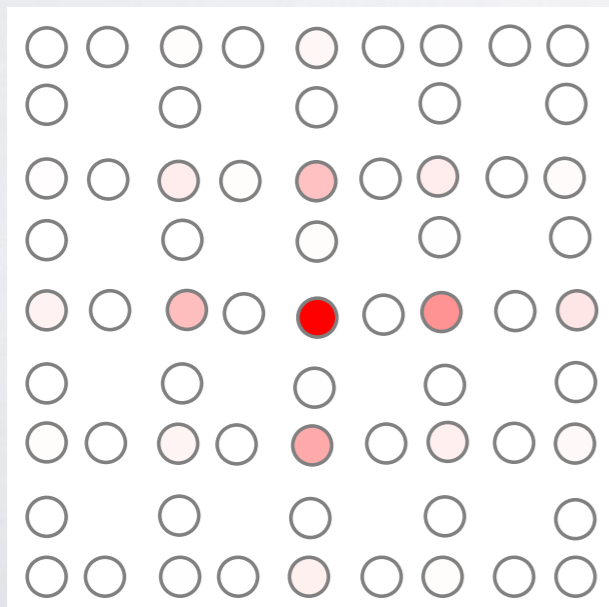
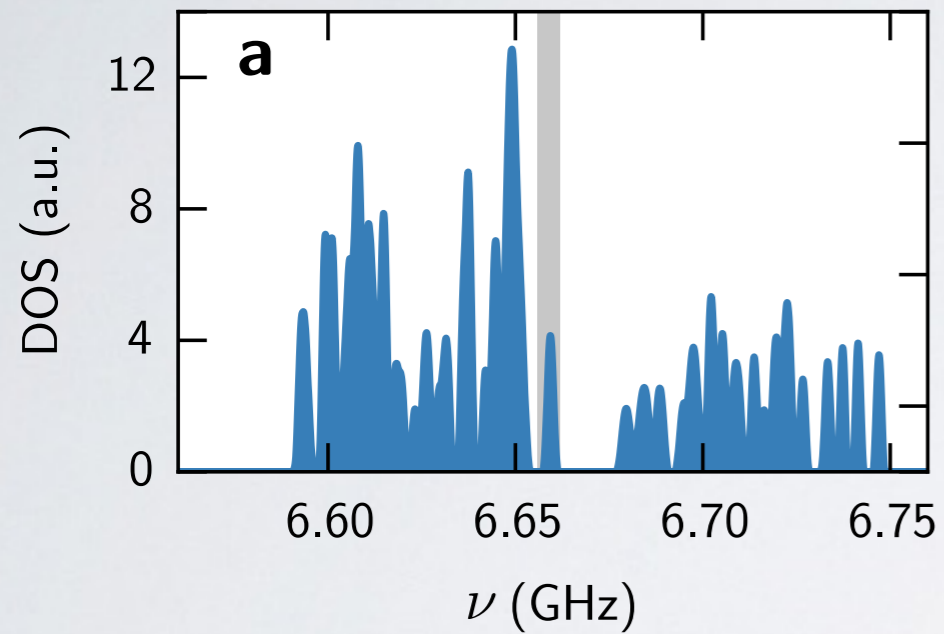
- the chiral symmetry of the majority sublattice is broken
- the flat band becomes dispersive
- the zero-mode is lifted away

Engineering of defect states

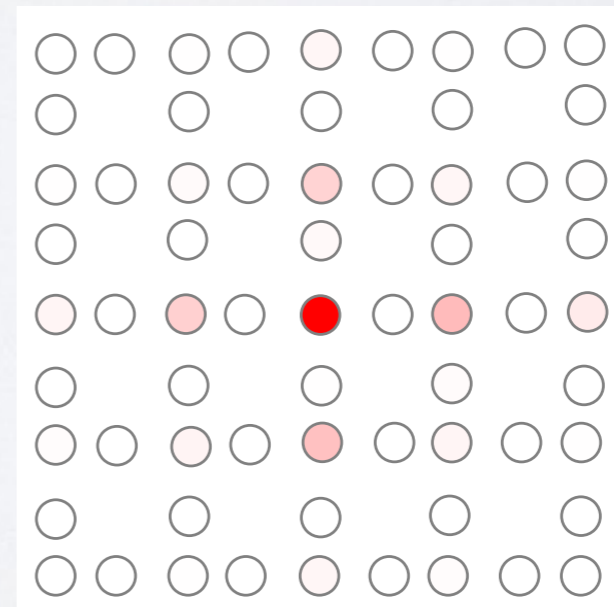
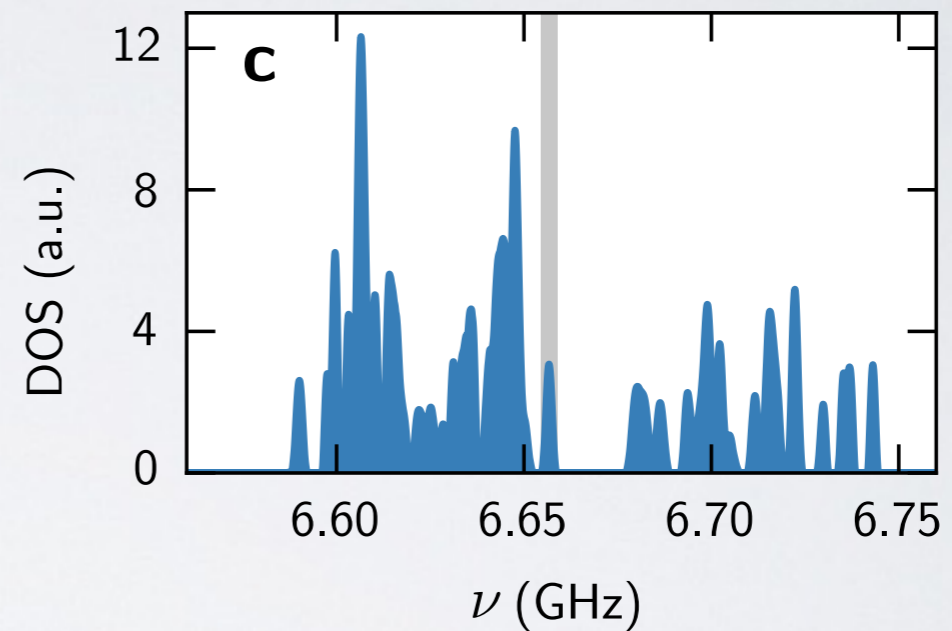


Topological protection

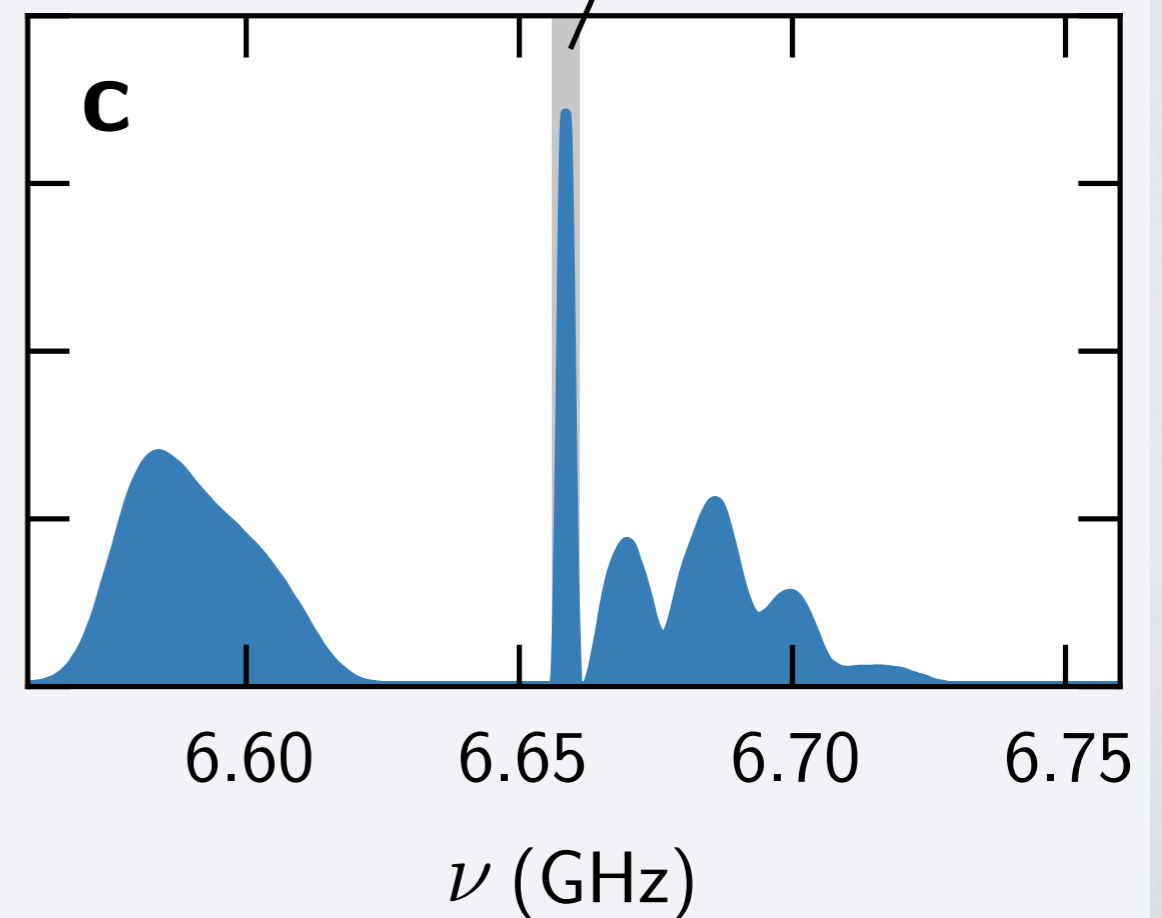
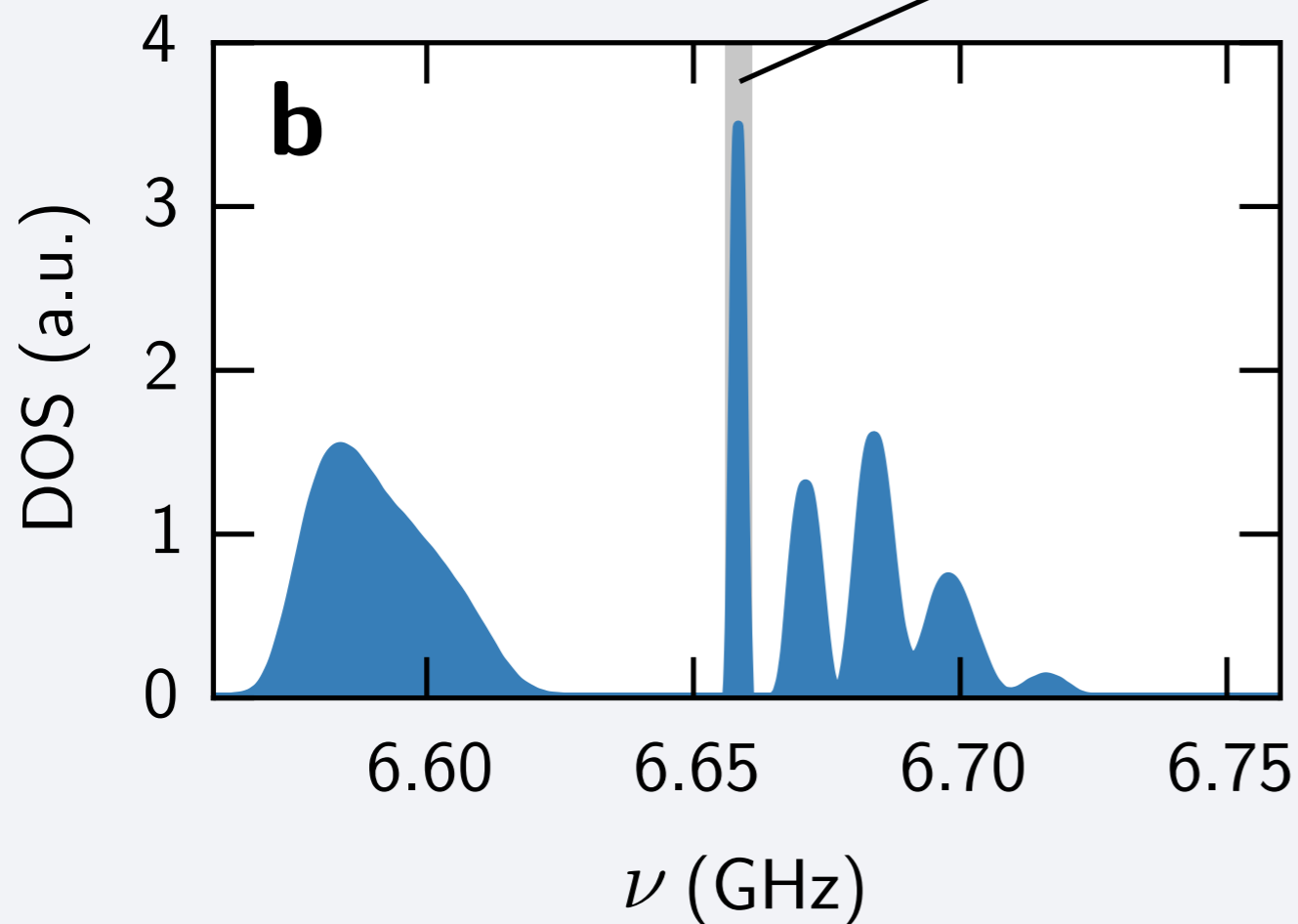
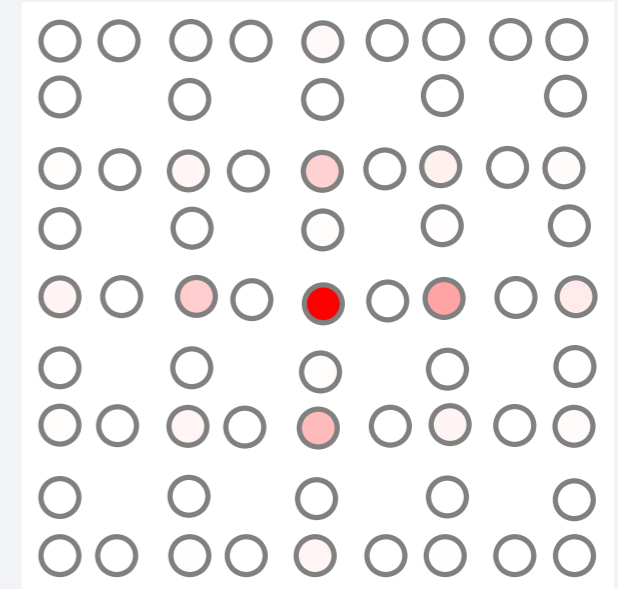
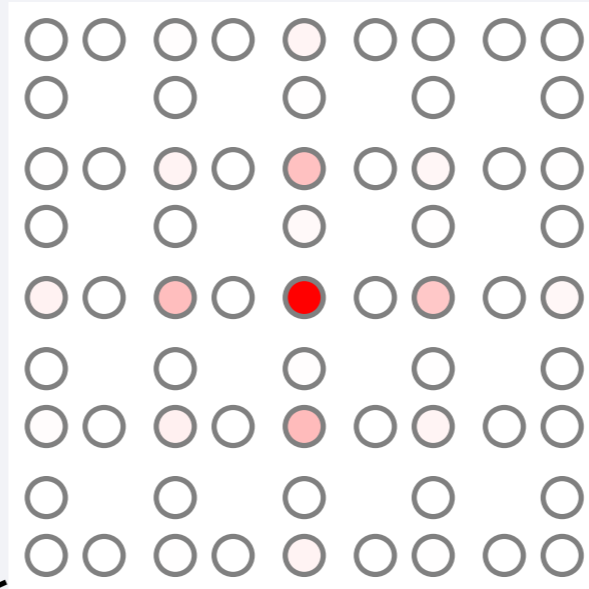
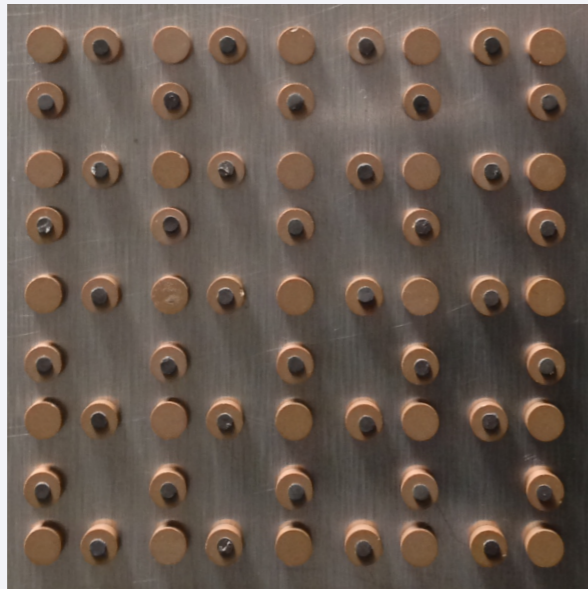
constrained disorder



generic disorder

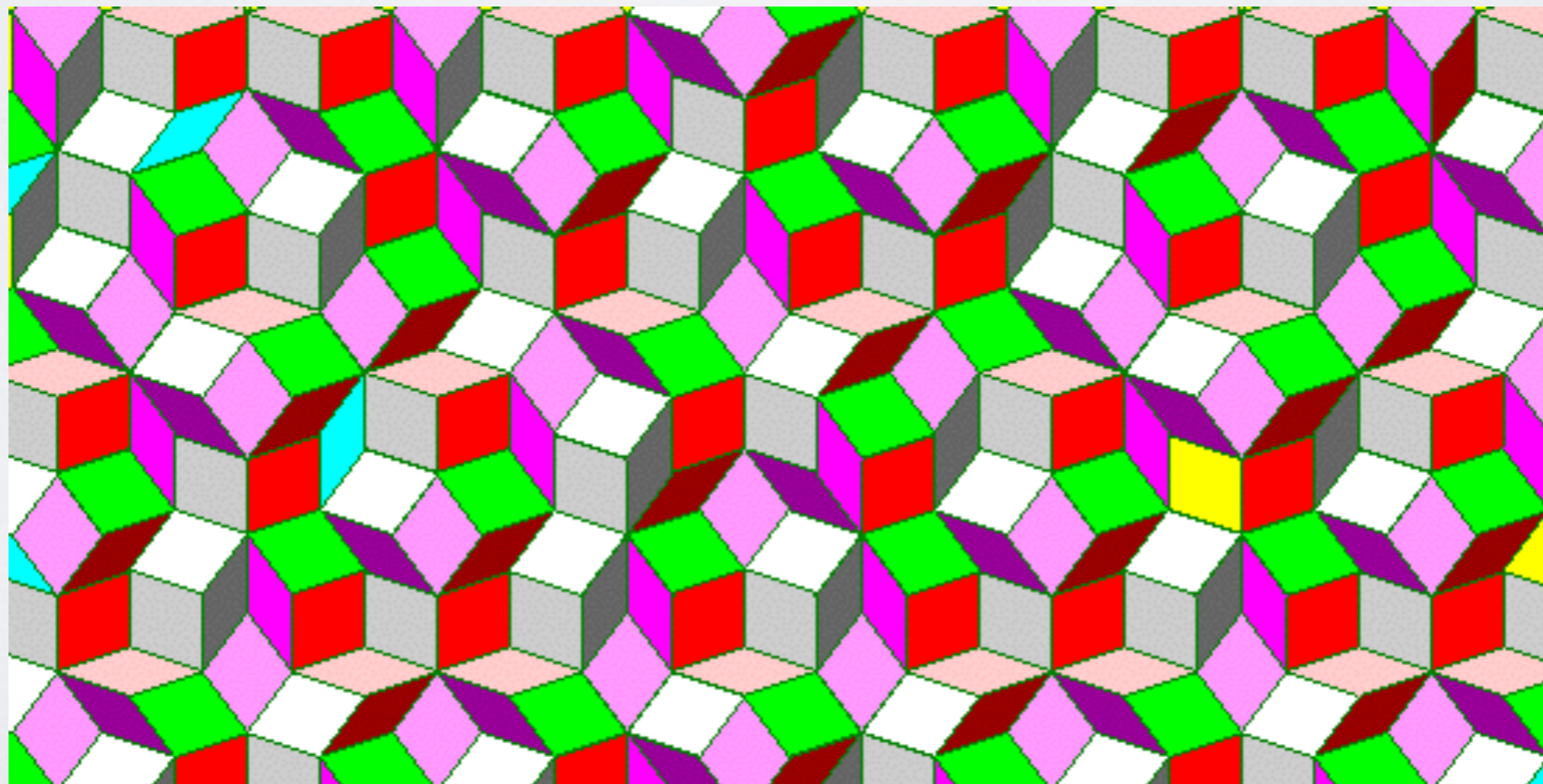


Selective enhancement

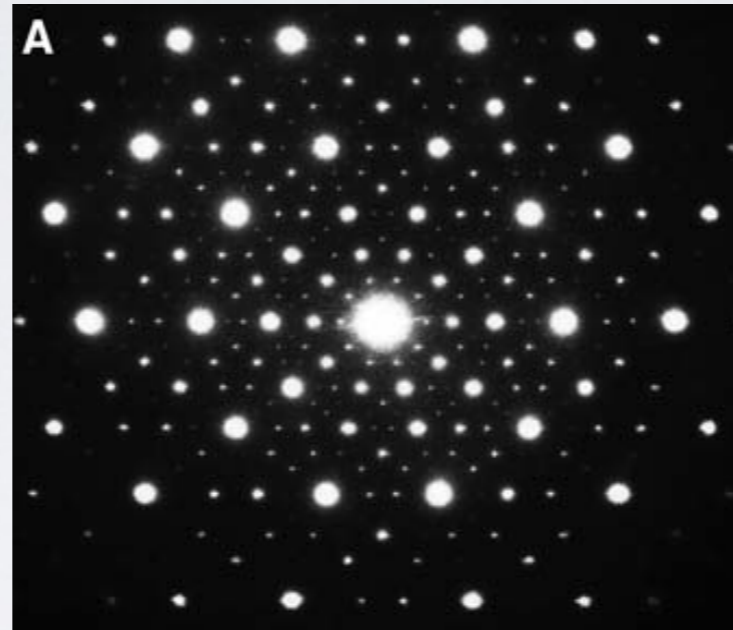
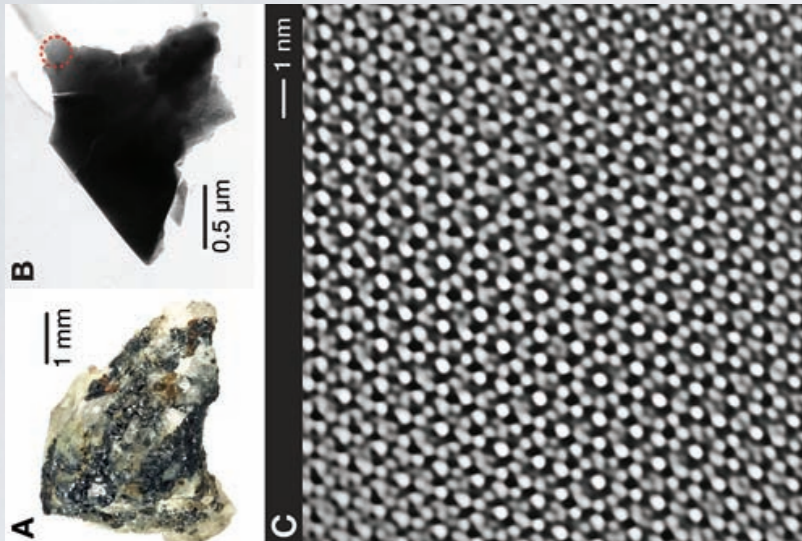
a

Intriguing quasicrystal

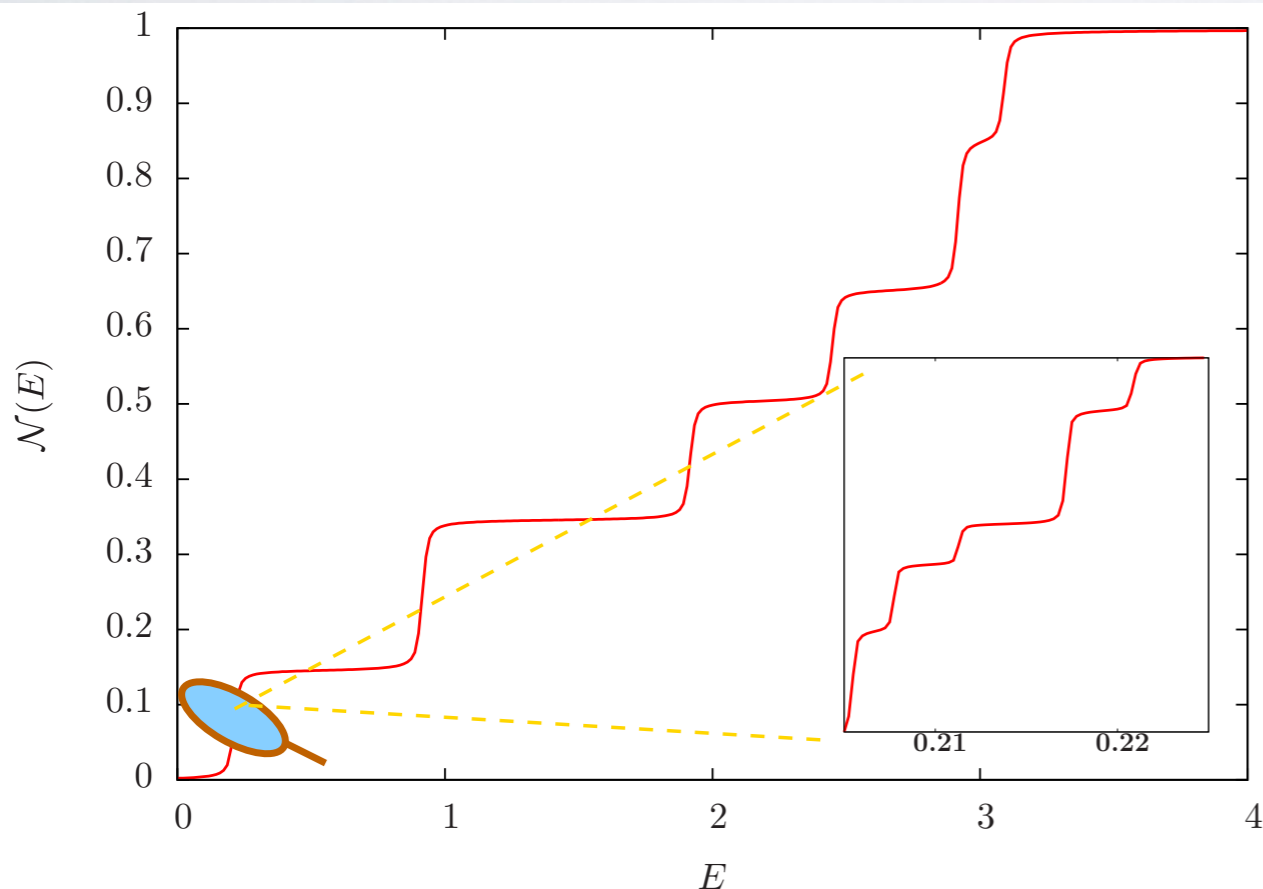
In a quasiperiodic crystal, the atomic positions along each symmetry axis are described by a sum of two or more periodic functions whose wavelengths have an irrational ratio (Bindi *et al.*)



Intriguing quasicrystal



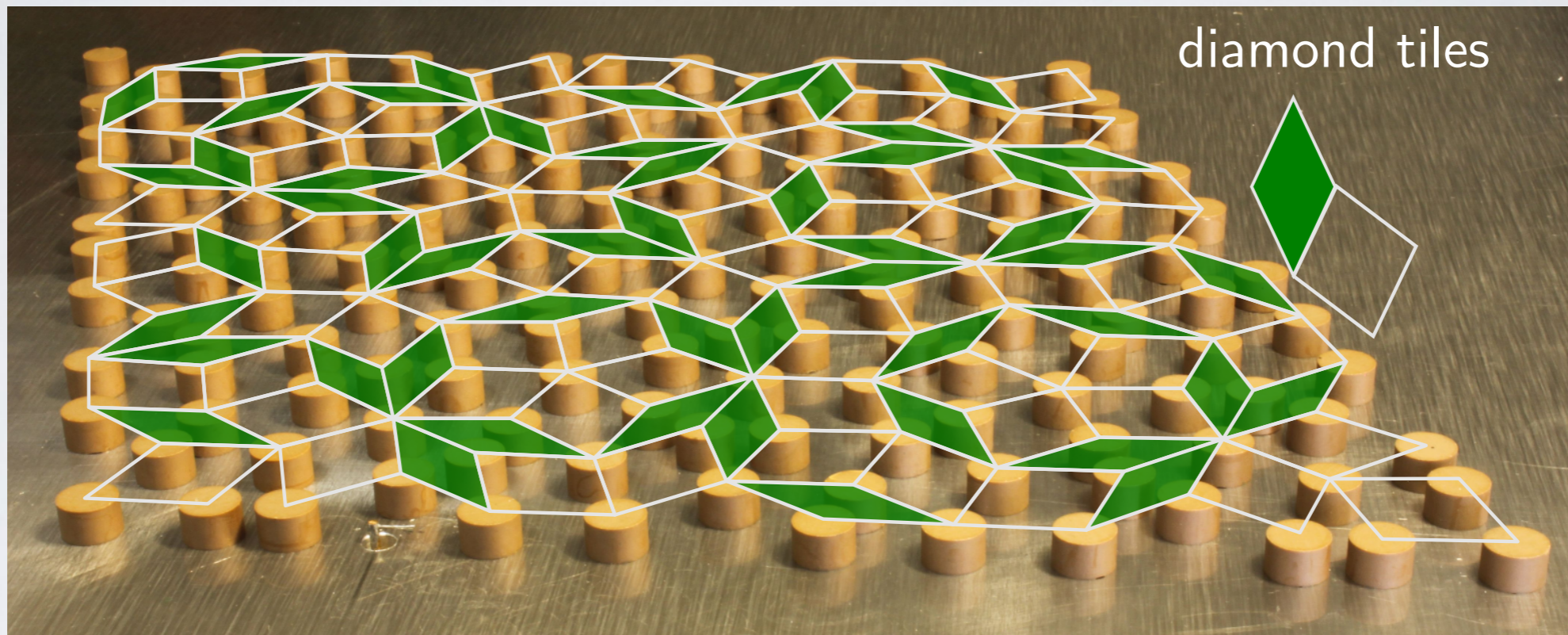
Diffraction pattern with 5-fold symmetry !



Integrated density of states with a staircase structure:

- irregular step heights
- smaller steps at higher energy resolution
- footsteps labeled by Chern numbers

Microwave Penrose tiling

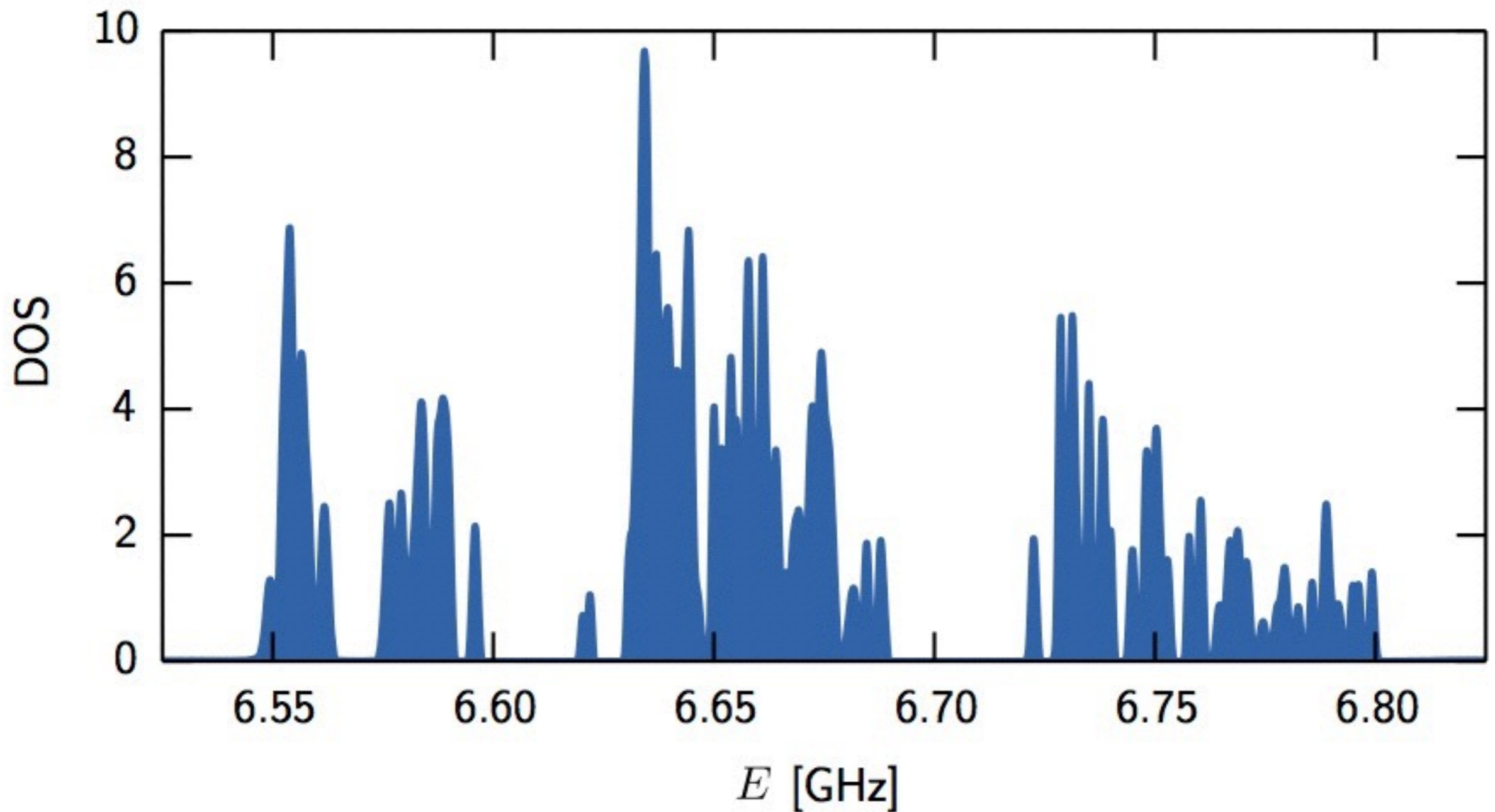


- Penrose lattice with rhombic tiles
- 164 resonators placed at each rhombus vertex

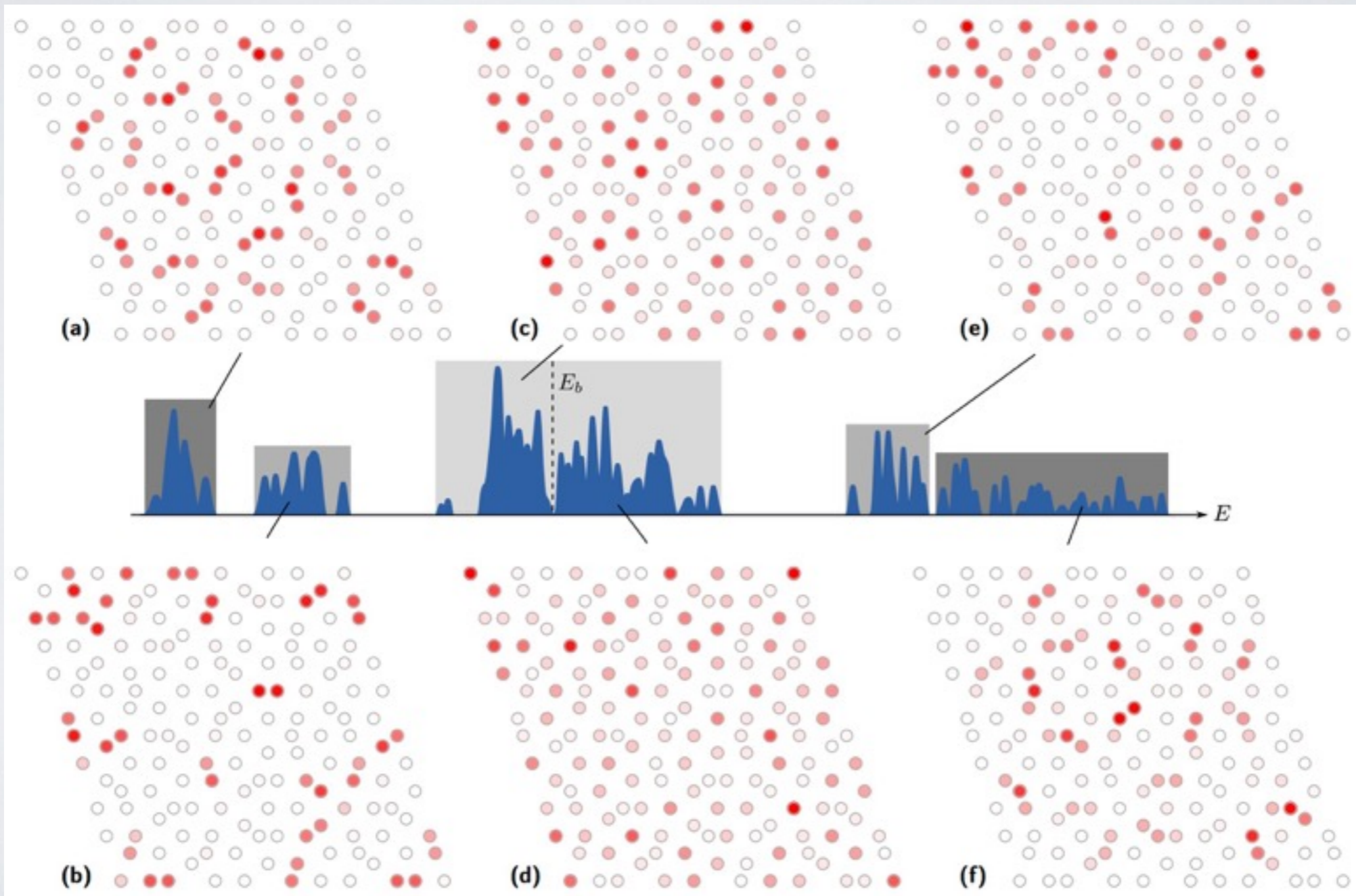
$$H = E_b \sum_i |i\rangle\langle i| + \sum_{i,j,i \neq j} t_{ij} |i\rangle\langle j|$$



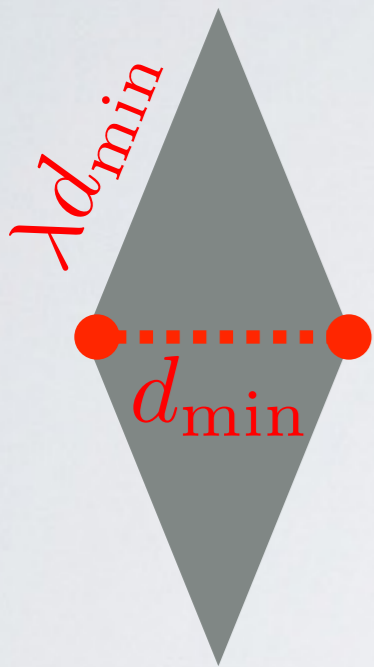
Density of states



Band wavefunctions



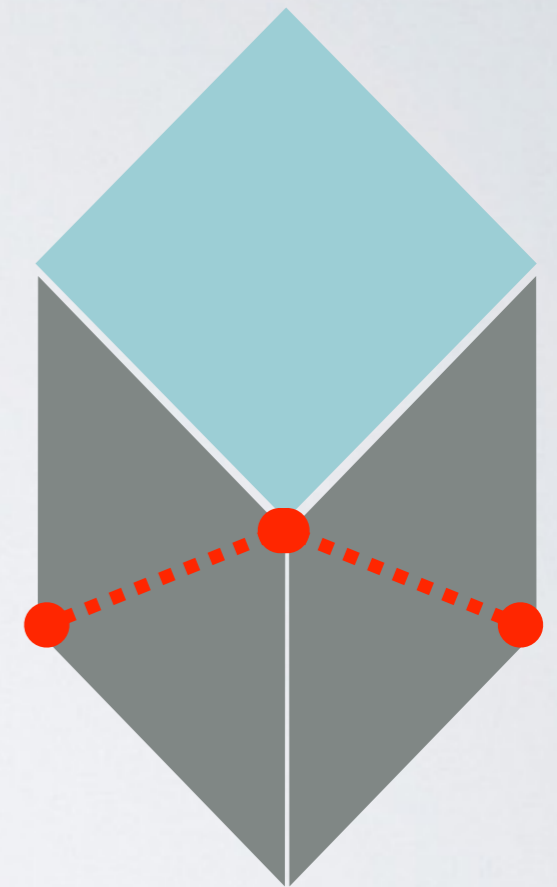
Dominant couplings



dimer

$$d_{\min} = 10 \text{ mm} \Rightarrow t_{\max} \simeq 73 \text{ MHz}$$

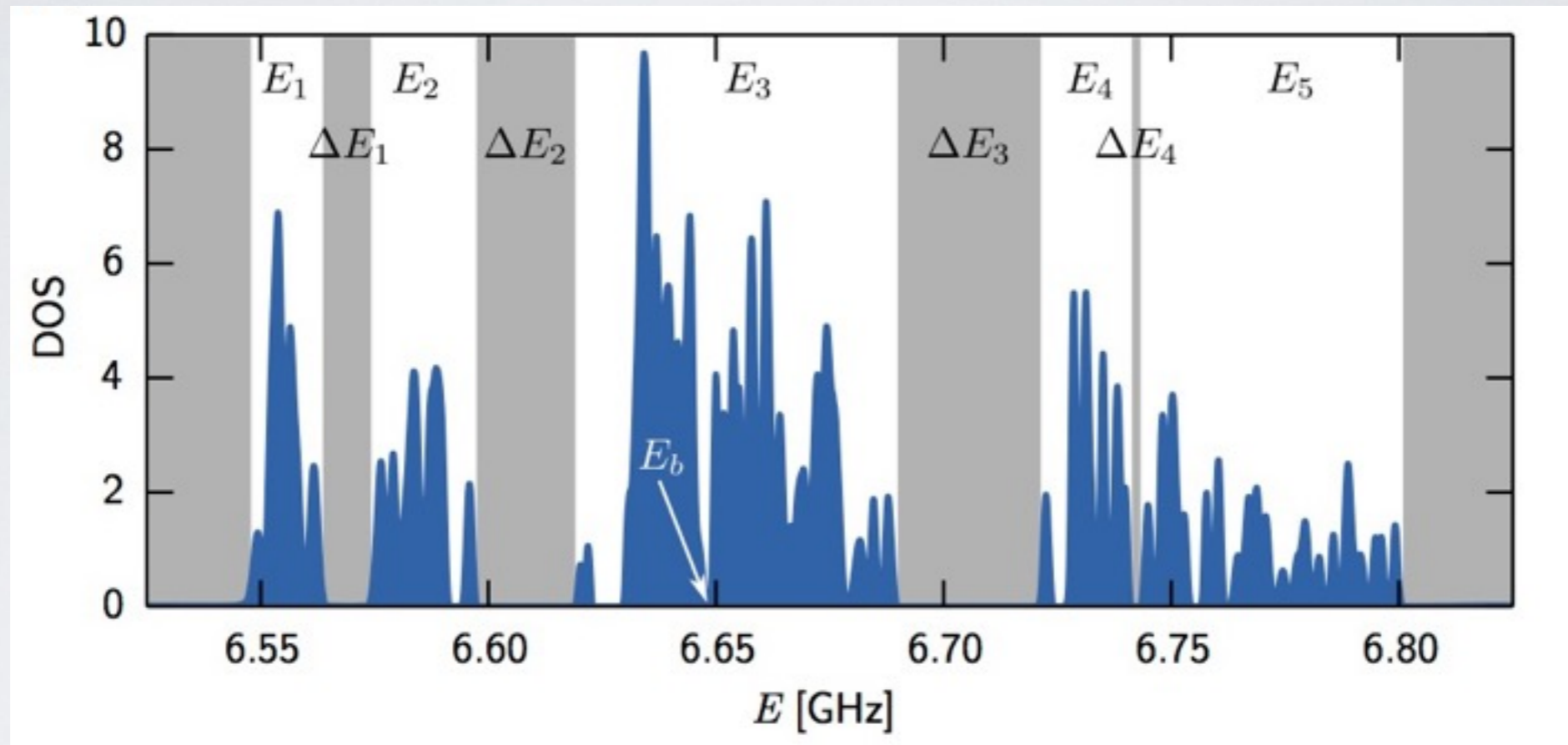
$$\lambda d_{\min} \simeq 16 \text{ mm} \Rightarrow t \simeq 8 \text{ MHz}$$



trimer

dominant coupling along the diagonal of the thin rhombus

Band structure



$$E_1 = E_b - \sqrt{2}t_{\max} \simeq 6.55 \text{ GHz}$$

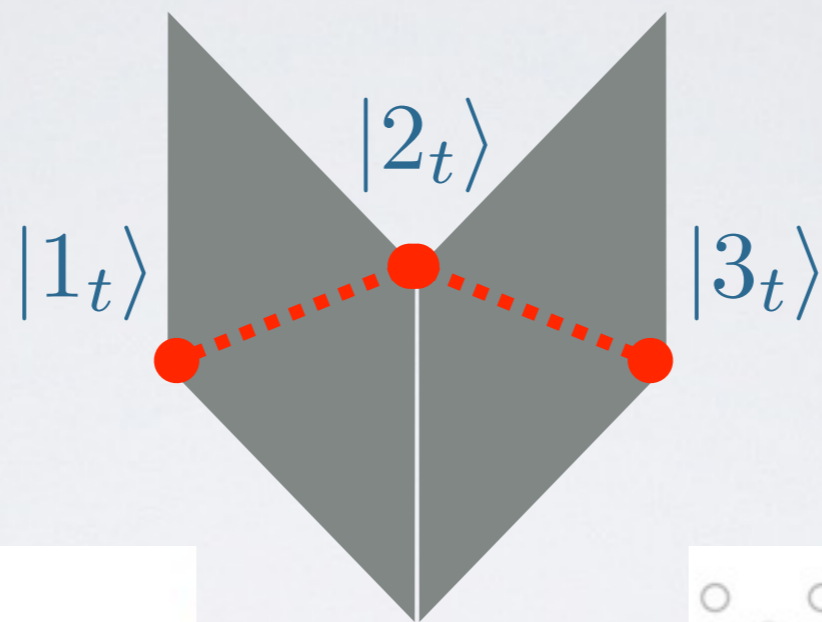
$$E_5 = E_b + \sqrt{2}t_{\max} \simeq 6.75 \text{ GHz}$$

$$E_2 = E_b - t_{\max} \simeq 6.58 \text{ GHz}$$

$$E_4 = E_b + t_{\max} \simeq 6.73 \text{ GHz}$$

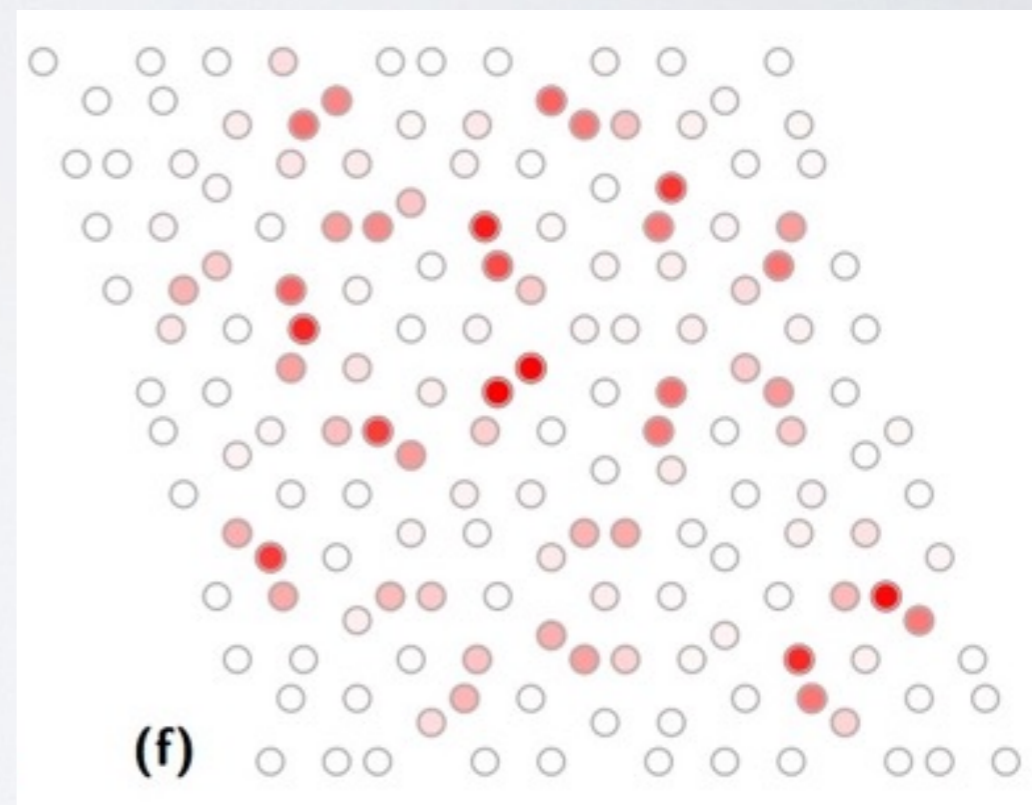
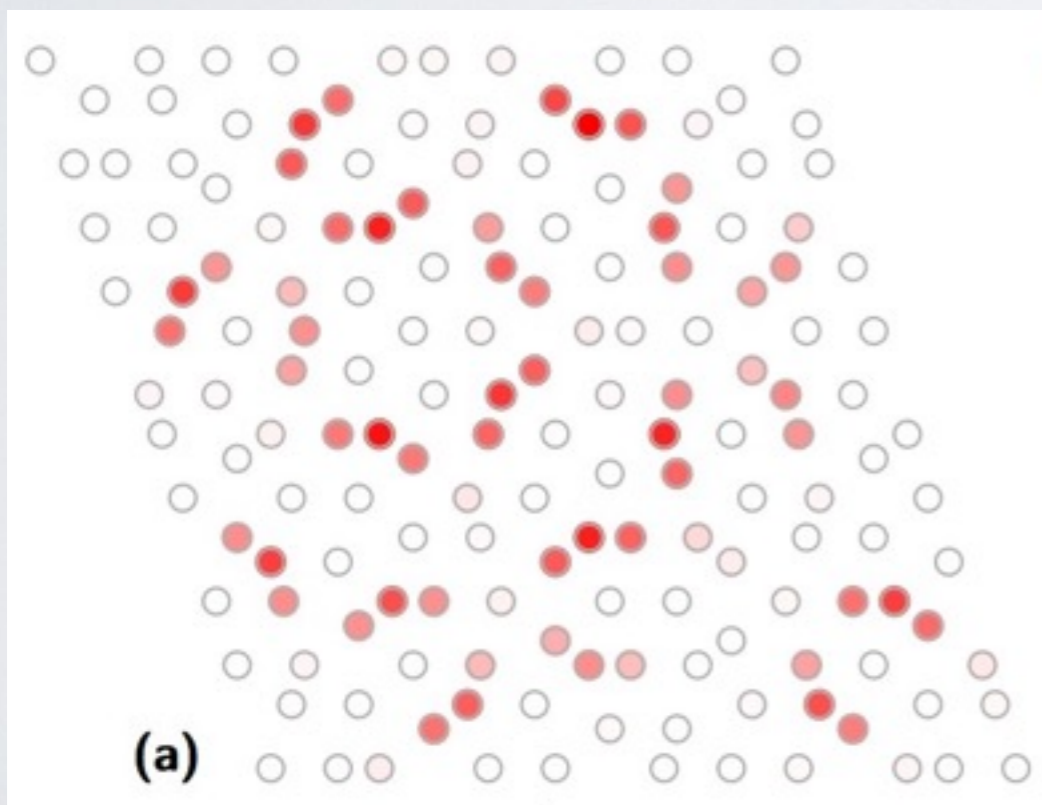
$$E_3 = E_b = 6.65 \text{ GHz}$$

Trimer motif



$$E_1 = E_b - \sqrt{2}t_{\max}$$

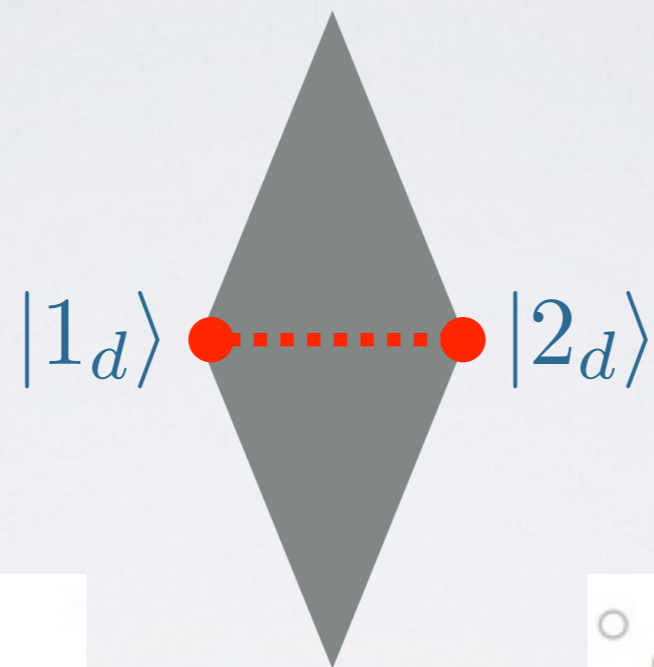
$$E_5 = E_b + \sqrt{2}t_{\max}$$



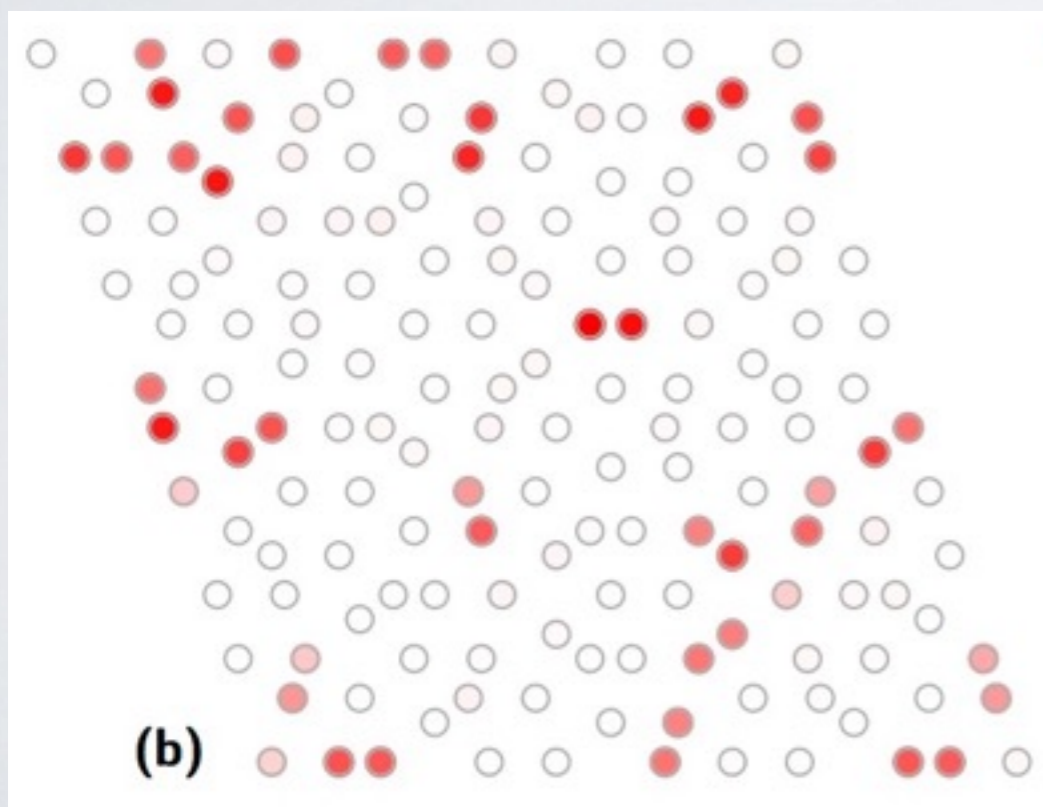
$$|\phi_1\rangle = |1_t\rangle - \sqrt{2}|2_t\rangle + |3_t\rangle$$

$$|\phi_5\rangle = |1_t\rangle + \sqrt{2}|2_t\rangle + |3_t\rangle$$

Dimer motif

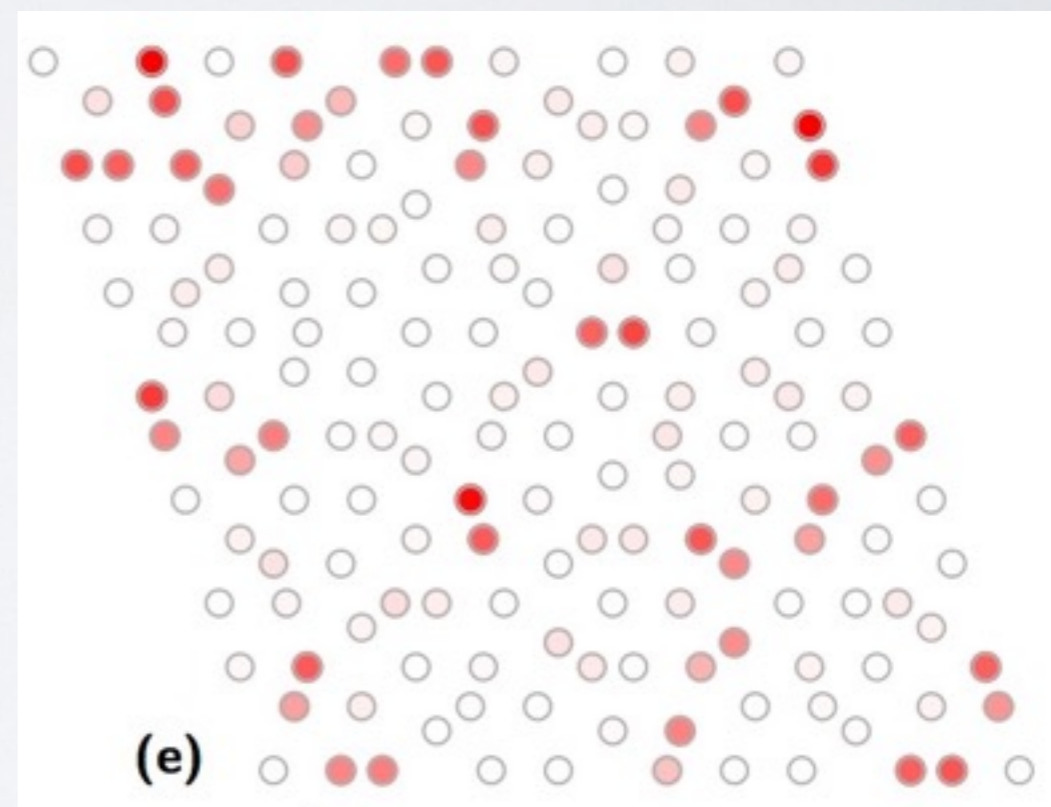


$$E_2 = E_b - t_{\max}$$



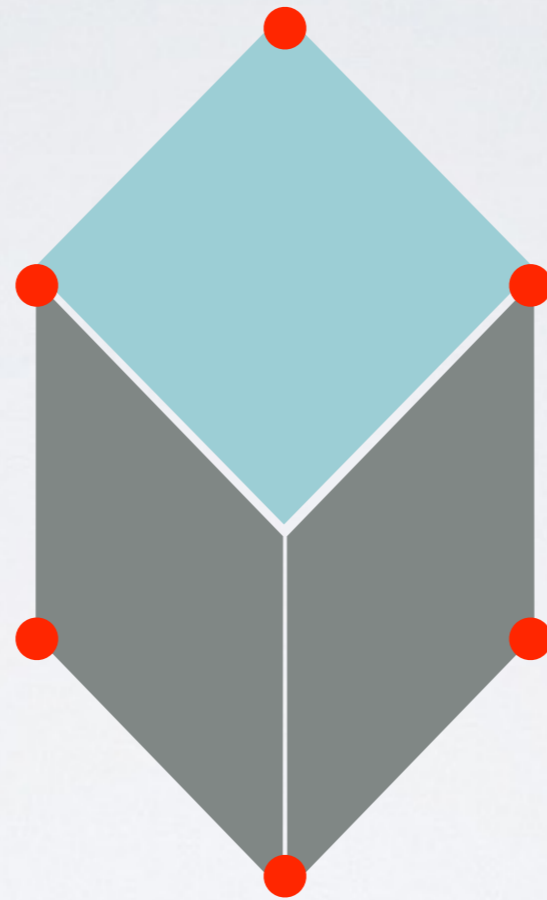
$$|\phi_2\rangle = |1_d\rangle - |2_d\rangle$$

$$E_4 = E_b + t_{\max}$$

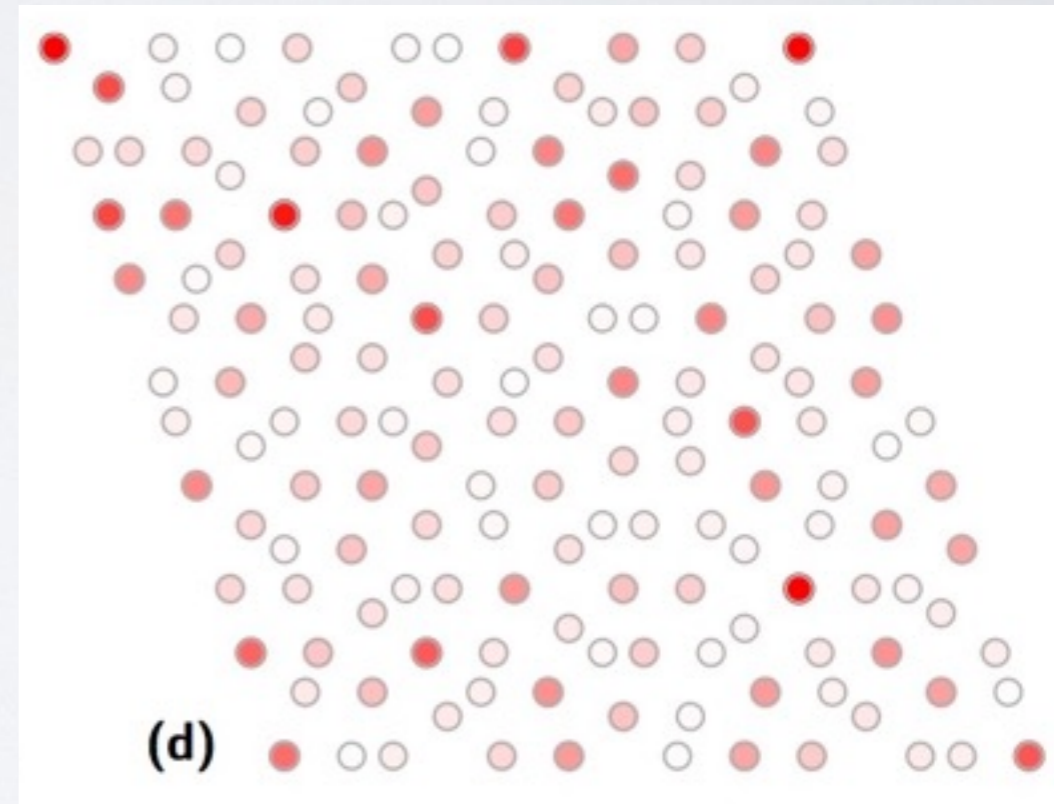
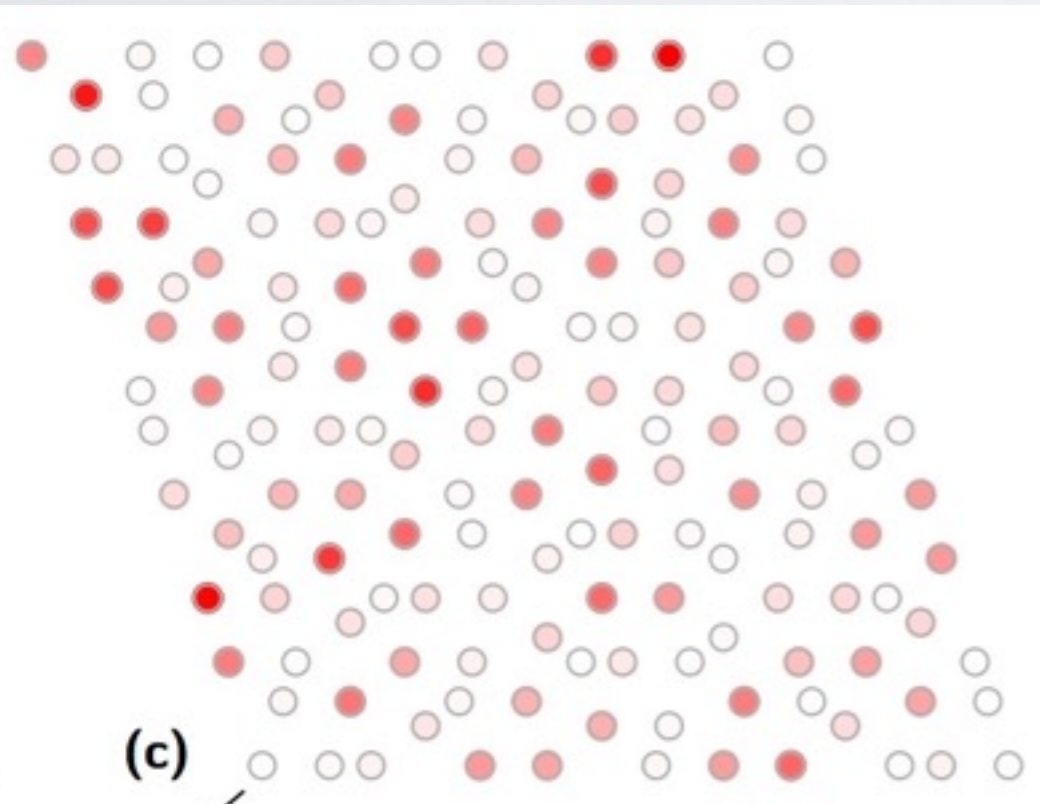


$$|\phi_4\rangle = |1_d\rangle + |2_d\rangle$$

Isolated sites



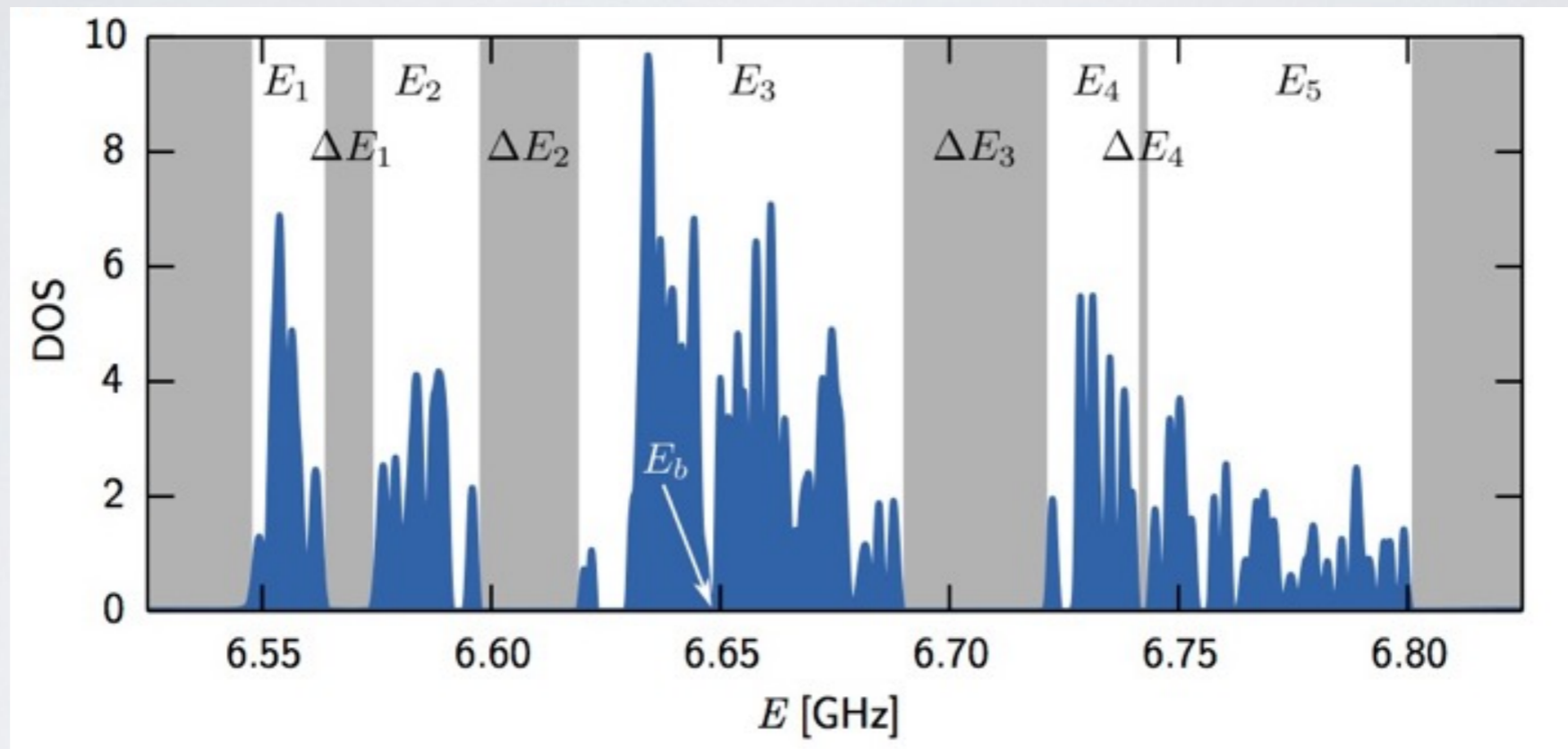
$$E_3 = E_b$$



$$|\phi_{3,a}\rangle = |1_t\rangle - |3_t\rangle$$

$$|\phi_{3,b}\rangle = |1_s\rangle$$

Band populations

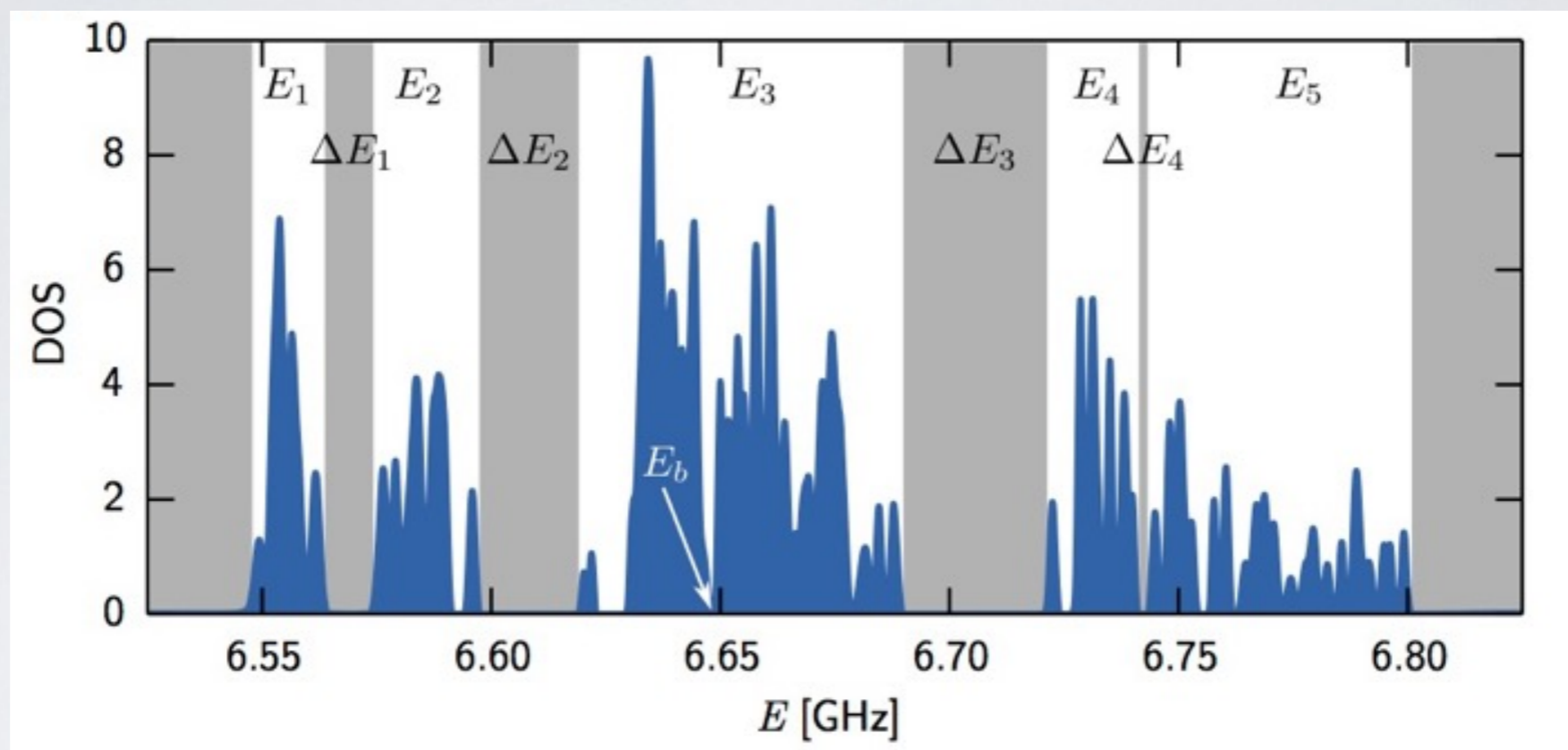


of dimers: $\beta_1 = \beta_5 = 5 - 3\lambda$

of trimers: $\beta_2 = \beta_4 = 5\lambda - 8$

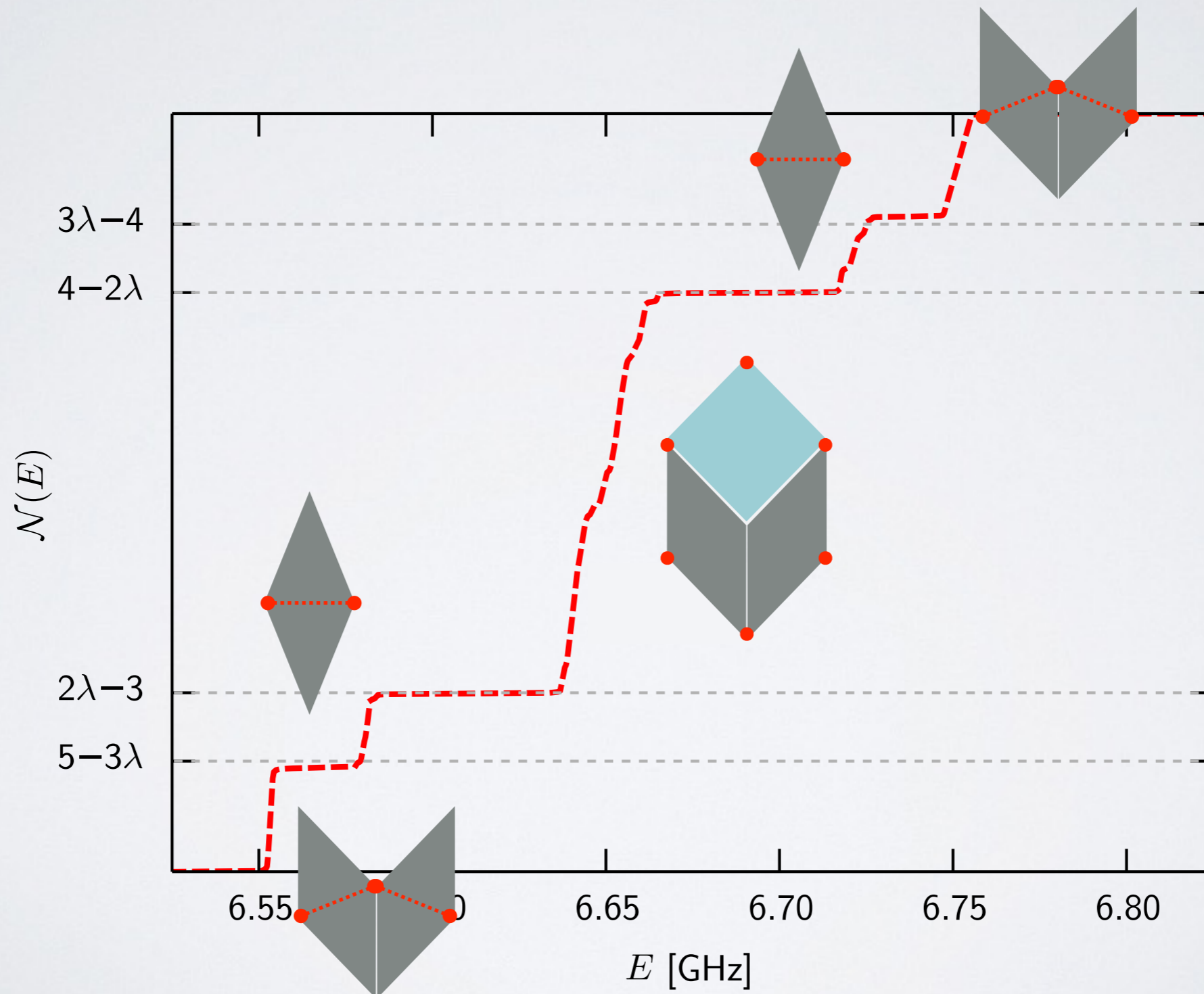
of others: $\beta_3 = 1 - 2\beta_1 - 2\beta_2 = 7 - 4\lambda$

Band populations

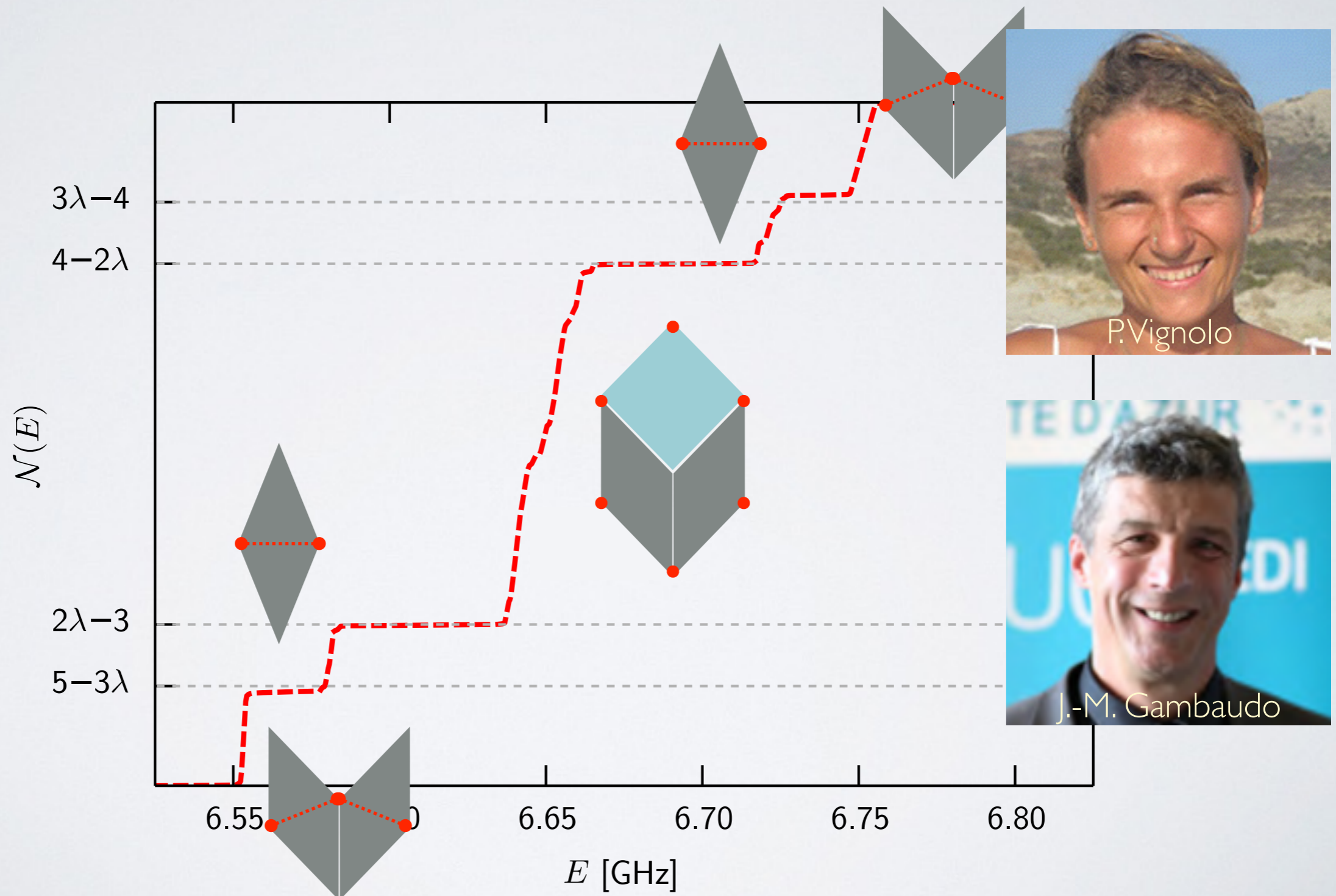


$$\mathcal{N}(E) = \begin{cases} \beta_1 = 5 - 3\lambda, & E \in \Delta E_1 \\ \beta_1 + \beta_2 = 2\lambda - 3, & E \in \Delta E_2 \\ \beta_1 + \beta_2 + \beta_3 = 4 - 2\lambda, & E \in \Delta E_3 \\ \beta_1 + \beta_2 + \beta_3 + \beta_4 = 3\lambda - 4, & E \in \Delta E_4, \end{cases}$$

Physical picture of the gap labeling



Physical picture of the gap labeling



Nice physics

2D Materials

2D Mater. **4** (2017) 025008

PAPER

Partial chiral symmetry-breaking as a route to spectrally isolated topological defect states in two-dimensional artificial materials

Charles Poli¹, Henning Schomerus¹, Matthieu Bellec², Ulrich Kuhl² and Fabrice Mortessagne²

Microwave emulations and tight-binding calculations of transport in polyacetylene

Thomas Stegmann^a, John A. Franco-Villafañe^{b,a}, Yenni P. Ortiz^a, Ulrich Kuhl^c, Fabrice Mortessagne^c, Thomas H. Seligman^{a,d}

PHYSICAL REVIEW B **95**, 035413 (2017)

Transport gap engineering by contact geometry in graphene nanoribbons: Experimental and theoretical studies on artificial materials

Thomas Stegmann,^{1,*} John A. Franco-Villafañe,^{1,2,†} Ulrich Kuhl,³ Fabrice Mortessagne,³ and Thomas H. Seligman^{1,4}

PHYSICAL REVIEW B **95**, 121409(R) (2017)

Waveguide photonic limiters based on topologically protected resonant modes

U. Kuhl,¹ F. Mortessagne,¹ E. Makri,² I. Vitebskiy,³ and T. Kottos²

RAPID COMMUNICATIONS

ARTICLE

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OPEN

Selective enhancement of topologically induced interface states in a dielectric resonator chain

Charles Poli¹, Matthieu Bellec², Ulrich Kuhl², Fabrice Mortessagne² & Henning Schomerus¹

PRL **110**, 033902 (2013)

PHYSICAL REVIEW LETTERS

week ending
18 JANUARY 2013

Topological Transition of Dirac Points in a Microwave Experiment

Matthieu Bellec,¹ Ulrich Kuhl,¹ Gilles Montambaux,² and Fabrice Mortessagne^{1,*}

PHYSICAL REVIEW B **93**, 075141 (2016)

Energy landscape in a Penrose tiling

Patrizia Vignolo,^{1,*} Matthieu Bellec,² Julian Böhm,² Abdoulaye Camara,¹ Jean-Marc Gambaudo,¹ Ulrich Kuhl,² and Fabrice Mortessagne^{2,†}

PRL **111**, 170405 (2013)

PHYSICAL REVIEW LETTERS

week ending
25 OCTOBER 2013



First Experimental Realization of the Dirac Oscillator

J. A. Franco-Villafañe,¹ E. Sadurní,² S. Barkhofen,³ U. Kuhl,⁴ F. Mortessagne,⁴ and T. H. Seligman^{1,5}

Manipulation of edge states in microwave artificial graphene

Matthieu Bellec¹, Ulrich Kuhl¹, Gilles Montambaux² and Fabrice Mortessagne¹